

CMSC 498M: Chapter 8

Artificial Intelligence for Games

Reading:

- Artificial Intelligence: Agents, Architecture and Techniques, by S. Rabin (Chapt. 5.3 in "Introduction to Game Development" by S. Rabin)
- Gamasutra tutorial:
http://www.gamasutra.com/features/19990212/sm_01.htm
- Boids page (<http://www.red3d.com/cwr/boids/>) by Craig Reynolds

Overview:

- Basic AI concepts
- Motion
- Planning and coordination

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What is AI?

What is Artificial Intelligence?

- "The study of computational systems that **exhibit intelligence**"
- Theories and computational models

What is Intelligence?

"It's whatever people do"

- Leads to the "**Turing Test**": If a person can't distinguish its behavior from a human, then it is intelligent
- This is **not rigorous**—"I know intelligence when I see it"

Behaving in a rational manner:

- Use available knowledge to maximize **goal achievement**
- Often leads to **optimization** techniques

Demonstrating complex capabilities:

- Problem solving
- Learning
- Planning, ...



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Roles of AI in Computer Games

Roles of Game AI: Complex behaviors not specified by player

Nonplayer Opponents: Realistic attack behavior

Nonplayer Teammates: Coordinated supportive behavior

Support and Autonomous Characters: Crowd/flock behavior

Commentators/Instruction: Does the player need a hint?

Camera Control: Finding the best viewpoint



What AI is not: There is not a clear distinction, but...

Determined by physical laws: E.g., path of a tennis ball

Purely random: E.g., which block falls next in Tetris

Direct response to game rules/user inputs: E.g., shoot gun when space-bar hit, scripted instruction sequences



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AI versus Animation

AI System: AI determines what to do and the animation does it

AI drives animation: AI system decides what **action** to take.
Animation **renders** the result.

Scenario 1: AI system issues **orders**: "move from A to B"
and animation system does the rest

Scenario 2: AI system controls **everything**, down to the
animation clip to play

Which scenario?

- Depends on the nature of the AI system and the nature of the animation system
- Is the animation system based on **motion capture**, or **physics**, or something else?
- Does the AI perform **collision avoidance**? Does it do detailed **planning**?



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Properties of a Good AI System

Goals:

Goal driven: AI system decides **what** to do, and then figures out **how** to do it

Responsive: AI system responds **immediately** to changes in the world

Smart: (knowledge intensive) AI system **knows** a lot about the world and how it behaves, and **uses** this knowledge in its own behavior

Consistent: Embodies a **believable, consistent** character

Efficient: Low CPU and memory usage

Practical: Fast and **easy development**

Tradeoffs:

- Unfortunately, many of these goals **conflict** fundamentally

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Part I - Basic AI Concepts

- **AI Basics**
- Agents
- Rule-based Approaches
- Finite-State Machines

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General Structure: AI Update Step

Sensing:

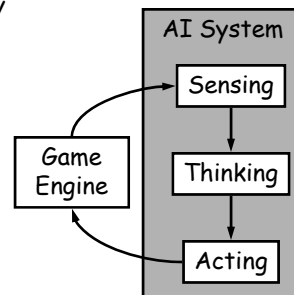
- Determines the **state** of the world
- **May be simple**: State changes all come by **message passing**
- **Or complex**: Figure out what is visible, where your team is, etc.

Thinking:

- What to do **next**, given world state/goals
- The **core** of the AI system

Acting:

- Tells the **animation system** what to do
- Translate low-level goals into **specific motion** (velocities, joint-angles)
- Can be messy/tedious



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General Structure: Polling or Event Driven?

Polling:

- The AI gets called at **fixed time** intervals
- **Senses**: Look to see what has **changed** in the world. For instance:
 - Queries what it can see
 - Acts on it

Event Driven:

- Acts in response to **world events**
 - Events sent by **messages** (E.g. invoke a callback function)
- **Examples**:
 - You heard a sound
 - A threat just entered your field of view
 - You have just been hit



Real systems are a mix:

- Something just changed (event)...so do some sensing (polling)

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AI Techniques in Games

Basic problem:

- Given the **state of the world**, what should the agent **do next**?

Range of (real-time) solutions in games:

- Rule-based systems
- Finite-state machines
- Decision trees
- Neural networks
- Fuzzy logic

Wider range of solutions in the academic world:

- Planning systems
- Logic programming
- Genetic algorithms
- Bayes nets
- Currently, too slow for games (but this may change in time)

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Two Measures of Complexity

Execution Complexity:

- How **fast** does it run as more knowledge is added?
- How much **memory** is required as more knowledge is added?
- Determines the run-time cost of the AI

Specification Complexity:

- How hard is it to **write** the code?
- As more knowledge is added, how much more code needs to be added?
- Determines the **development cost**, and risk

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Agents: Goals of an Opponent

Provide a challenging (but flawed) opponent:

- Should be **beatable** (but not too easily)
- Should be **entertaining** and fun

Not too challenging:

- Should **not be superhuman** in accuracy, precision, sensing, ...



No unintended weaknesses:

- No "**golden path**" to defeating opponent every time
- Must not fail miserably or look **dumb** (e.g., getting lost)

Not be too predictable:

- Through **randomness**
- Through **multiple**, fine-grained **responses**
- Through **adaptation** and **learning**



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Agents: What are They?

Definition:

"An **autonomous agent** is a system situated within and a part of an environment that **senses** that environment and **acts** on it, over time, in pursuit of its **own agenda** and so as to effect what it senses in the **future**." (Stan Franklin and Art Graesser)

Structure of Agent Action:

Sensing: perceive features of the environment

Thinking: decide what action to take to achieve its goals, given the current situation and its knowledge

Acting: doing things in the world

Issues:

- **Thinking** can make up for **limitations** in sensing and acting (e.g., extrapolating future motion)
- The more **accurate** the models of sensing and acting, the more **realistic** the behavior



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Agents: Sensing Limitations & Complexities

Sensing Issues:

Limited sensor distance/field of view: Can sense local environment

Obstacles: Agent cannot see through walls

Improving the view: Detecting and computing paths to doors

Realistic behavior: Sensitivity to motion, fooled by camouflage

Reaction time: Sensed information is not processed instantly

Random noise in sensors:

- Mimicking human limitations

Different Sensors:

Sound: Omni-directional, gives direction, distances, speech, ...

Vision: Limited field of view, 2.5D, color, texture, motion, ...

Smell: Omni-directional, chemical makeup

Integration:

- Need to integrate different sources to build complete picture

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Agents: Simple Action Strategies

Random motion: ("unintelligent" AI)

- Roll the dice to select when and where to move

Regular pattern:

- Follow **invisible tracks**: E.g., Galaxian

Tracking/Pursuit Strategies:

Direct Pursuit: Move toward prey's position
(E.g. heat-seeking missile)

Lead Pursuit: Move toward a spot ahead of prey

Interception: Move to where prey is expected to be

Evasion Strategies:

Direct Evasion: Move directly away from (slow) pursuer

Side-step: Head perpendicular to (fast) pursuer's current bearing

Weave: Every N seconds move X degree off pursuer's bearing



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Rule-based approaches

Rule-Based Systems: Popular because:

- Familiar
- Predictable and, hence, testable
- Many game designers don't know much about AI :-)

Rules specify the action depending on circumstances:

Deterministic: One action for each situation

Random: Multiple possible actions in the same situation

Weighted: Certain actions have a higher probability

Based on State/Environment Information:

Take the direction that leads you to the opponent

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Rule-based approaches

Example:

- A simple rule-based system for moving a ghost agent in **Pac-Man**

Ahead	Right	Left	Action
Open	—	—	Go ahead
Blocked	Open	—	Turn Right
Blocked	Blocked	Open	Turn Left
Blocked	Blocked	Blocked	Go backwards



Note:

- Easy to add randomness, if we like
- Does **not** consider the location/state of the player

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Finite-state machines (FSMs)

Finite-State Machines:

- A (finite) set of possible **states** that the agent can be in
- Connected by **transitions** that are triggered by a **events** or **changes** in the world or user input
- Normally represented as a **directed graph**, with the edges labeled with the transition event

Ubiquitous:

- Almost **all** computer game AI systems support FSMs

Déjà vu?

- FSMs are used in **language processing** (regular languages)
- You might have seen them in language theory and compilers

Issues:

- Provide a clean graphical way to describe state transitions/actions
- Uniform table/graph structure

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Quake-Bot Example

Types of behavior to capture:

- If you don't see an enemy, **wander** randomly
- When see enemy, **attack**
- When hear an enemy, **chase** enemy
- On dying, **re-spawn**
- **Extras:** If health is low and seeing an enemy, **retreat**

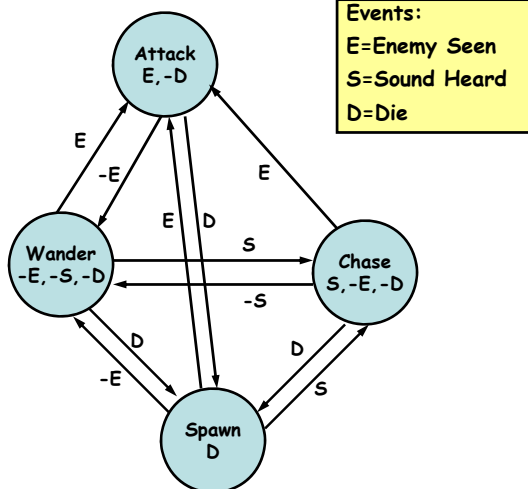


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Finite-state machines (FSMs)

Actions: On entering or exiting a state we invoke a **callback function**

Problem: There is no transition from Attack to Chase



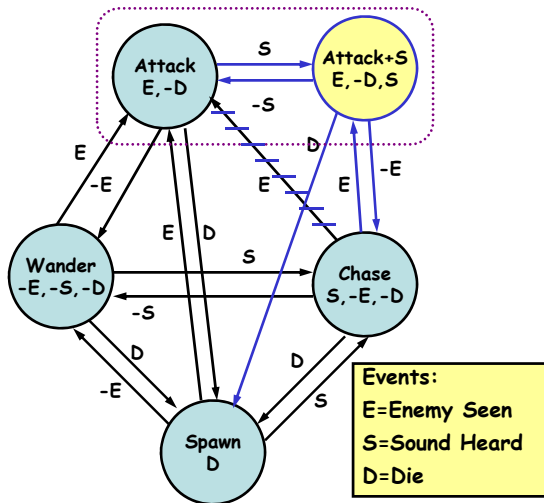
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Finite-state machines (FSMs)

Possible Fix: Create an **extra attack state** if sound is heard

Problem: This can result in the proliferation of a **huge number of states**

Solution: Rather than creating new states, make limited use of **additional variables**

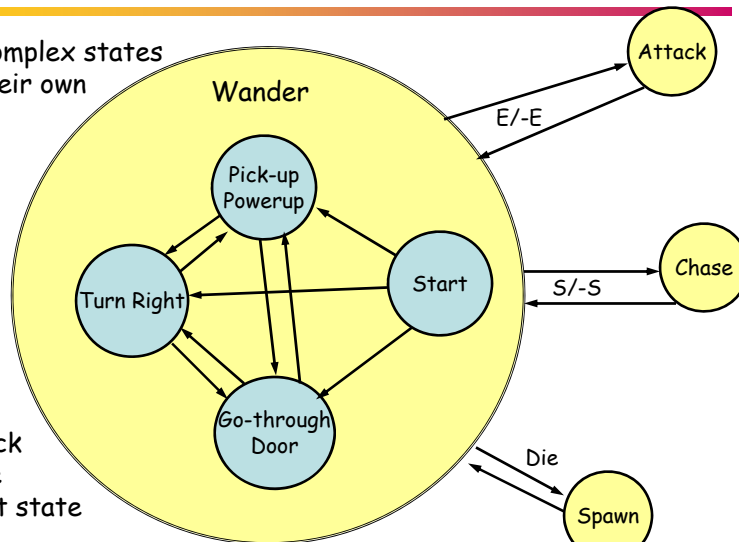


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Hierarchical FSMs

Expand complex states into their own FSM

Use a stack to save current state

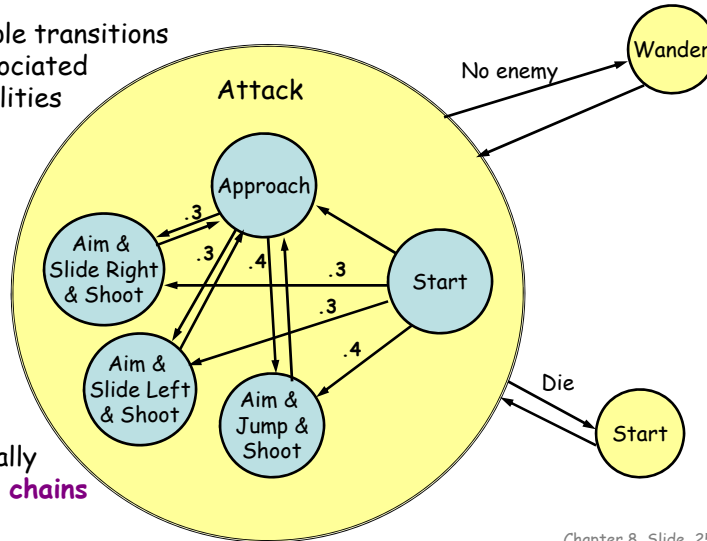


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Nondeterministic FSMs

Add multiple transitions
and associated
probabilities

These are
essentially
Markov chains



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Efficient FSM Implementation

Basic Implementation:

- Compile into an **array** indexed by [state-name, event]
- **Transition**: $\text{state-name}_{i+1} \leftarrow \text{array}[\text{state-name}_i, \text{event}]$
- Switch based on state-name to call execution logic

Hierarchical FSMs:

- Create array for every FSM
- Have **stack** of states:
 - Classify events according to stack
 - Update state which is sensitive to current event

Nondeterministic FSMs:

- Have array of **possible transitions** for every (state-name, event) pair
- Choose one at **random**, based on transition probabilities

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Part II - Motion

- **Motion Planning**
- Configuration spaces
- Waypoints
- Path planning algorithms
- Navigation Interfaces

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Motion Planning

Motion planning: Move an agent from one position to another

- Avoiding (fixed) **obstacles**
- Avoiding other **moving objects**
- **Goals:** Smooth, compact, natural motion. Robustness

Motion planning in games:

First-Person Shooter: How does the AI get from room to room?

Real-Time Strategy: User directs an agent to go somewhere. How do they get there?

Many others: Sports, racing, ...

Computational issues:

- Coordinating the motion of **multiple entities** with many **degrees of freedom** is computationally very hard



Call of Duty 3

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Motion Planning

Academic Formulation: Given a start point s and a destination point t , find a path from s to t that avoids obstacles

Minimize cost: Distance, travel time, ...

Travel time may depend on terrain, for instance

Dynamic environments: Paths being blocked or removed

Limited knowledge: No map; just what sensors tell us

Game Formulation: Find a reasonable path from s to t

Need not be optimal: Not shortest, but not too long

Need not be perfect:

- OK to briefly intersect obstacles
- OK to backtrack sometimes

Dynamic environments: But you usually have complete knowledge of the current environment

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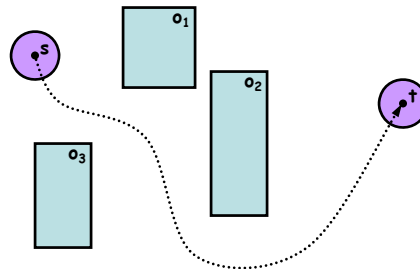
Configuration Space: Simple Example

Point motion planning:

- Much easier to plan the motion of a **point** than a geometric **object**
- Can we **reduce** object motion planning to point motion planning?

Simple example:

- We want to plan the motion of a **circular disk** of radius r from starting point s to destination point t
- Can we convert this into a motion planning problem for a **point**?



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Configuration Space: Simple Example

Equivalent problem:

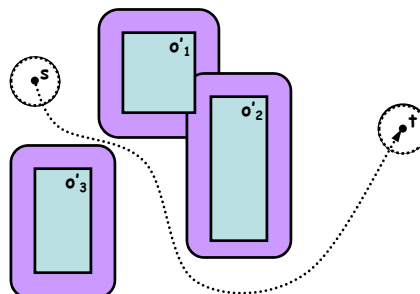
- **Grow** each obstacle o_i by radius r . Call the grown obstacle o'_i .
- **Shrink** the disk down to a point
- Plan the motion of a **point** from s to t

Why this works?

A disk centered at a point p intersects obstacle o

- $\Leftrightarrow p$ is within distance r of o
- $\Leftrightarrow p$ intersects the grown obstacle o'

Can we generalize this idea to more complex objects?



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Configuration Space: Basics

General motion planning:

- How can we reduce the motion of an arbitrary geometric object to **point motion planning**?

Configuration vector:

- The exact position of each moving entity can be described by a **vector** of numbers, e.g.:
 - Position of its center of mass: (x, y, z)
 - 3D rotational orientation (e.g. using Euler angles): (ϕ, θ, ψ)
 - Joint angles: $(\theta_1, \theta_2, \theta_3, \dots, \theta_k)$
- Thus, the position of an object can be modeled as a multi-dimensional **configuration vector**: $(x, y, z, \phi, \theta, \psi, \theta_1, \theta_2, \theta_3, \dots, \theta_k)$

Configuration space:

- Can model location of an **object** in 3-space as a **point** $(6+k)$ -space

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Configuration Space: Free/Forbidden Placement

Free or Forbidden: Each point in configuration space is either:

Free: Intersects no obstacles

Forbidden: Intersects some obstacle

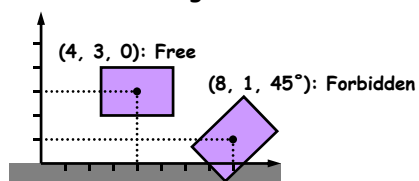
Example: A 3×2 rectangle in 2D that translates and rotates:

Center of Mass Position: (x, y)

Rotation: θ

Configuration point (3D): (x, y, θ)

Suppose that we require the rectangle to lie above the line $y = 0$



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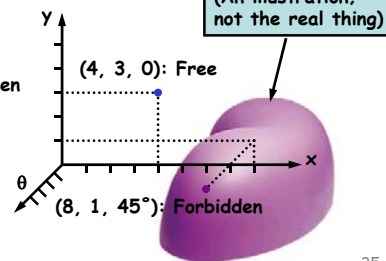
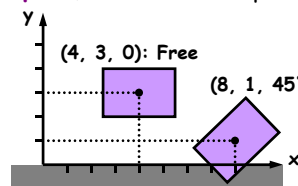
Configuration Space: Configuration Obstacle

Configuration obstacles:

The set of all forbidden points in configuration space defines a **forbidden region**. These regions are called **configuration obstacles**.

Equivalence:

- Computing the motion of an **object** in "**regular space**" from one free placement to another ...is equivalent to...
- Computing the motion of a **point** in **configuration space**, from one free placement to another



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Configuration Space: Issues

Further issues:

Configuration distance: Is **not Euclidean** because configuration coordinates are generally not homogeneous (E.g., x-translation in meters, rotation in radians)

Curse of Dimensionality: Computational **complexity increases exponentially** with the dimension of the configuration space

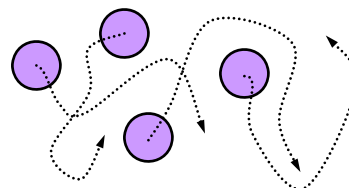
Coordinated Motion: Can be done by **concatenating the configuration vectors** of all moving objects. Very hard !!!

Reducing complexity:

Constrained motion: e.g., no rotation

Simplify models: e.g., bounding boxes

Prioritized planning: e.g., plan object 1's motion first, then object 2, etc.



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Part II - Motion

- Motion Planning
- Configuration spaces
- **Waypoints**
- Path planning algorithms
- Navigation Interfaces

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Path Planning

Point path planning:

- Henceforth we assume (by reduction to configuration space) that we need only plan motion of a point

Common methods:

Discrete (graph-based) search algorithms:

BFS, Dijkstra's algorithm, A* search, ...

Potential fields:

Put a "force field" around obstacles, and follow the "potential valleys"

Pre-computed plans with dynamic re-planning:

Pre-compute answer and modify as required

Special purpose algorithms:

E.g., Given a fixed start point, fast ways to find paths around polygonal obstacles

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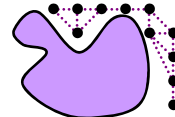
Discrete (Graph-Based) Algorithms

Curved surfaces and curved paths:

- Generally obstacles (especially in configuration space) are **curved**
- Generally optimal paths are **curved** (Imagine running around a corner)

Discretize the search space:

- Restrict the start and goal points to a finite set of **waypoints**
- Restrict the path to lie on **line segments** connecting waypoints



Graph search:

- Waypoints are **nodes**
- Connecting segments are the **edges**
- Distance/cost modeled as **edge weights**
- Search reduces to the well studied problem of computing **shortest paths in a graph**

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Waypoints

Waypoint:

- In navigation this is a mapped reference point used for navigation. (E.g. a buoy or radio beacon)

Where to put waypoints?

- There are many possibilities, as we shall see

How to connect them?

- Depends on what paths you are willing to accept - almost always assume straight lines (e.g., along line of sight)

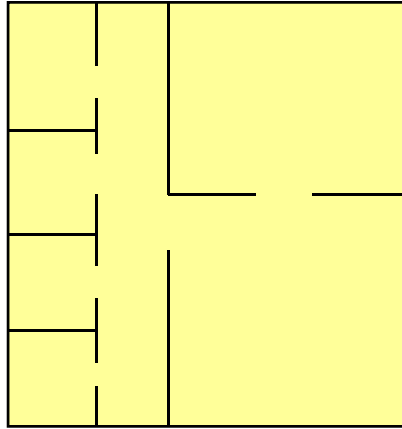
Answers depend on the game:

Environment: open fields, enclosed rooms, etc...

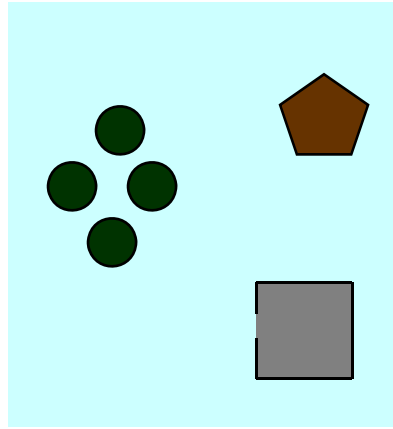
Game Style: covert hunting, open warfare, friendly romp, ...

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Where would you place Waypoints?



Room Structured



Open Terrain

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Strategies for Placing Waypoints

By hand:

- Best control, but most time consuming

Heuristics:

- In **doorways**, because characters have to go through doors and straight lines joining rooms always go through doors
- Along **walls**, for characters seeking cover
- At other **discontinuities** in the environments (edges of rivers, for example)
- At **corners**, because shortest paths go through corners

Importance of good waypoints:

- Good waypoint selection results in more **natural**, varied motion
- Automatic **obstacle avoidance** (by providing sufficient clearance)

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Grid-Based Placement

Grid-based waypoints:

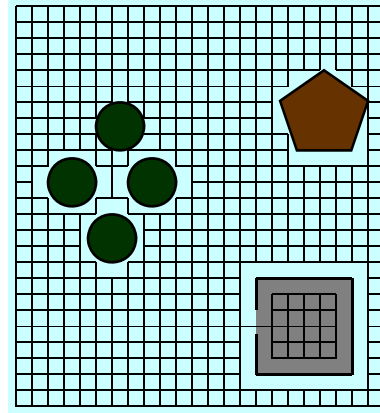
- Place a **grid** over the world
- Put a waypoint at every **grid point** that is **obstacle-free**

Joining waypoints:

- Join waypoints if the segment between them hits no obstacle
- Only check immediate neighboring grid points
E.g., **4-neighbors** (N,E,S,W) or diagonal **8-neighbors**

Pros & Cons:

- **Easy** to implement
- Insensitive to variations in **resolution**
- Problems with **tight spaces**



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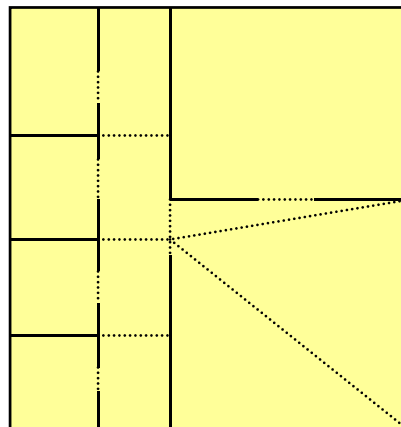
Polygon-Based Placement

Polygon-based waypoints:

- Choose waypoints based on the floor polygons in your world
- Further **subdivide** large/complex polygons into smaller, convex regions for more complete waypoint placement

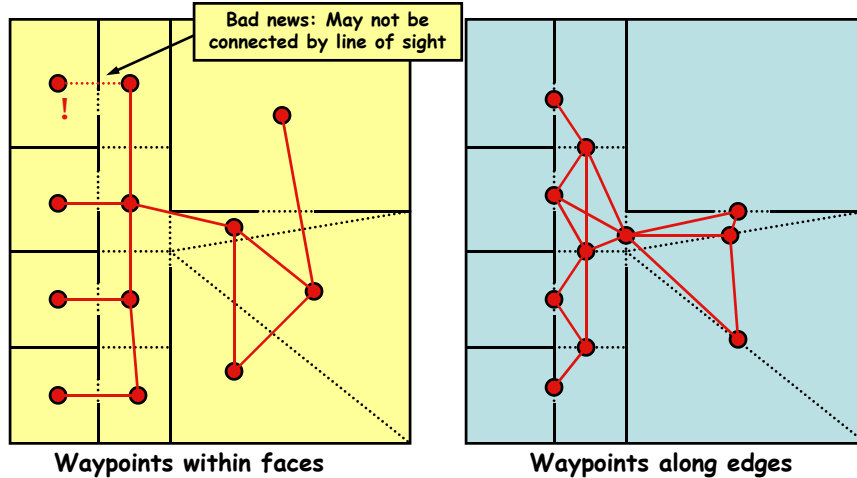
Where to place waypoints?

- There are two obvious options (next slide)



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Polygon-based Placement

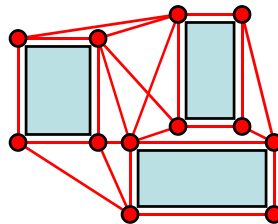


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Waypoints around Obstacles

Obstacles:

- Place waypoints a small distance from **obstacle corners**
- Nearby waypoints are connected if they are **mutually visible**



Pros & Cons:

- Tends to produce the **shortest paths**
- Motion "**scraping**" along walls is not very natural. Real people tend to find maximum clearance paths

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Getting On and Getting Off

Problem:

- Characters may not start and end at waypoints

Solution:

- When the character starts, find the **closest** visible waypoint and move to that first

Better:

- Find the visible waypoint **closest to the direction** you think you need to go

Even Better:

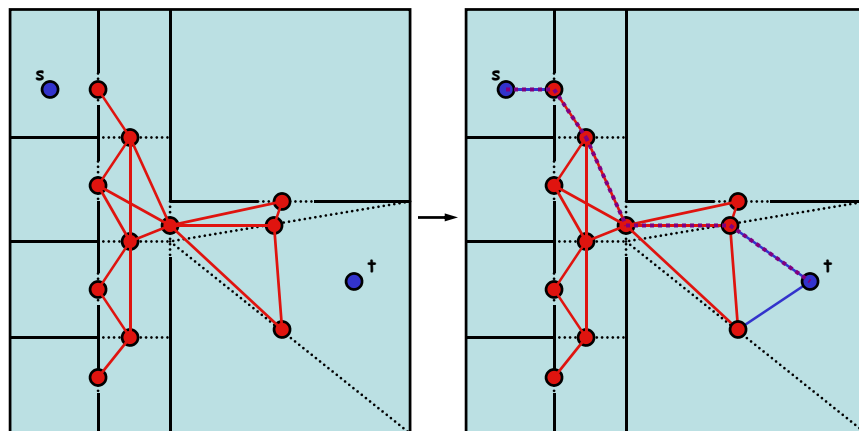
- **Try all** visible waypoints and see which gives the shortest path, most direct path

Best option:

- Add a new, **temporary waypoint** at the precise start and goal point, and join it to nearby waypoints. Then invoke path planning algorithm.

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Getting On and Getting Off



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Search Algorithms

Generic search algorithm: From source s to destination t

- **Initialization:**
 - Mark s as discovered, and mark all other nodes as undiscovered
 - $\text{dist}[s] \leftarrow 0$, and $\text{dist}[u] \leftarrow \infty$ for all other nodes
 - Create a priority queue containing only s
- Repeat until reaching t :
 - **Extract:** Remove the node u of highest priority from the priority queue
 - **Process:** For each unfinished neighbor v of u :
 $\text{dist}[v] \leftarrow \min(\text{dist}[v], \text{dist}[u] + \text{weight}(u, v))$
Mark v as discovered and add to/update priority queue
 - **Finish:** Mark u as finished

Algorithm invariant: At any time there are three types of nodes:

Undiscovered: Haven't seen this node yet

Discovered: A neighbor has seen you. You are in the queue.

Finished: You have completed processing. dist value will not change.

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Search Algorithms

Obtaining the shortest path:

- Store a pointer for each node u to the **previous** node along the shortest path to u
- Update pointers as nodes are added to the visited set and as nodes are processed (whenever the dist changes)
- To find path to goal, trace pointers **back** from goal nodes

Making the generic algorithm concrete:

- The only element that has not been spelled out is how **priorities** are assigned to the discovered but unfinished nodes
- The choice of priority affects the **correctness** and **efficiency** of the search algorithm

Common Search Algorithms:

- Breadth-First Search and Dijkstra's Algorithm
- Best-first (Local Greedy) Search
- A* Search

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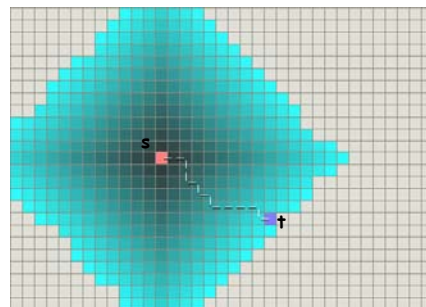
Dijkstra's Algorithm

Dijkstra's Algorithm:

- The **priority** of node u is the **distance estimate**, $\text{dist}[u]$
- The unvisited node u with the smallest **$\text{dist}[u]$** is processed next
- Under the (reasonable) assumption that edge weights are non-negative, this **correctly** finds the shortest path
- The order in which vertices are visited is **independent** of the location of the **destination** node

Breadth-First Search:

- When there are **no edge weights**, can replace the priority queue with a simple **FIFO queue**



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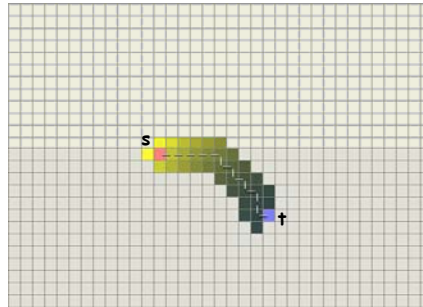
Best-First Search: A Greedy Heuristic

Best-First Search:

- The priority of a node is its **Euclidean distance** from t
- Next node to process is the discovered node that is **closest** to t
- This heads straight to t , and so is potentially much **faster** than Dijkstra's algorithm or Breadth-First Search

Bad news:

- This heuristic may **fail** when obstacles are present



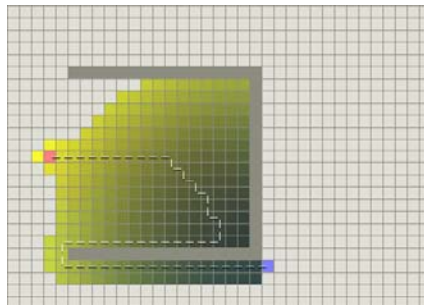
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Best-First Search: Getting Caught

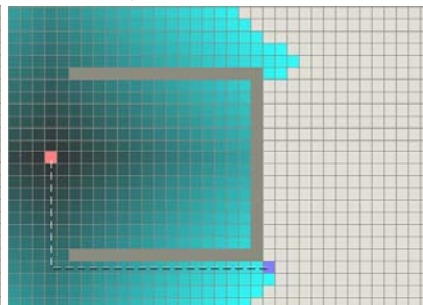
Best-First Search vs Dijkstra:

- When obstacles are present, best-first search may get **trapped**, and will need to **backtrack**. The result is a suboptimal path.
- Dijkstra's algorithm visits more nodes, but gets the **correct** path

Best-first Search



Dijkstra's Algorithm



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A* Algorithm

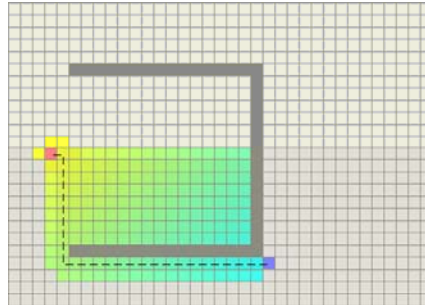
A* Algorithm:

- Combines the **best aspects** of Best-First Search and Dijkstra
- The priority of a node is the **sum** of two functions:
 $f(u) = g(u) + h(u)$, where:
 $g(u) = \text{dist}[u]$ (current **distant estimate** to u)
 $h(u) = \|u - t\|$ (**Euclidean distance** from u to t)
- Like Best-First, it **seeks the destination** first
- Like Dijkstra, it computes the **correct shortest path**

Key:

- $h(u)$ should be a **lower bound** on the remaining distance to t

This is the algorithm of choice



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Summary of Graph-Based Search Methods

Summary:

Dijkstra:

- Always correct
- Does not seek the destination
- Efficient in the worst-case, but not on average

Breadth-First Search:

- Simplified version of Dijkstra for when edges have uniform weight (Cost of a path is number of edges on the path)
- As with Dijkstra, does not seek the destination

Best-First Search:

- Greedily seeks the destination
- Very fast when few objects are present
- May not produce the shortest path

A* Search:

- Always correct
- Seeks the destination, and so is efficient on average
- Method of choice for game programming

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Part II - Motion

- Motion Planning
- Configuration spaces
- Waypoints
- Path planning algorithms
- **Navigation Interfaces**

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Navigation Interfaces

Motivation:

- Agent AI has a certain level of complexity in its **objectives and goals**
- Creating intelligent movement involves **transmitting** these objectives and goals to the **navigation system**

Navigation Interface:

- Provides a **structure for conveying** information about agent **objectives and goals**

Design Choices:

Tradeoffs: Choosing an interface involves making a compromise between focus and flexibility

Highly focused: Can be better tuned to a specific problem

Flexible: Can have the expressiveness to handle a wider variety of scenarios

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Navigation Interfaces

Levels of Expressiveness:

Single Pair: (Lowest level)

- A **origin point** and **destination point** are given
- Return the **lowest cost path** between them

Weighted Destinations:

- Instead of a single destination, provide **multiple goals**, each with its own **reward**
- Optimal path **maximizes the net pay-off**, (reward – cost)

Goals: (Highest level)

- Specify the movement in terms of the **agent's goals**
- May **not** involve **spatial specifications** (e.g., find armor or a weapon)

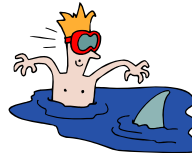
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Navigation Interfaces

AI Paradigms for Movement:

Reactive Behaviors:

- Maps **sensory input** directly to **motion** (e.g., Danger! Run away!)
- Fine for **simple situations**: obstacle avoidance, seeking, fleeing
- Cannot handle **traps** or **complex environments** (e.g., running into a closet)



Deliberative Planning:

- Provably **optimal** paths (e.g., Dijkstra or A* search)
- Higher-level of **spatial intelligence**
- Plans based on an **environmental model**



Hybrid Systems:

- Combine "**common sense**" of reactive behaviors with "**intelligence**" of planning

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Navigation Interfaces: Implementation

Reactive Behaviors:

- Steering behaviors based on **explicit mathematical formulas**
- Two problems:
 - **Integration** of multiple behaviors
 - **Realism**
- **Prioritize behaviors** and use **fuzzy logic** to simulate realism

Deliberative Planning:

- Not necessarily a search. Other techniques can be more efficient.
 - **Precompute** everything (like look-up tables)
 - **Reactive approximation** techniques to build near optimal paths without a search
- **Dynamic environments** make things tricky
 - Trigger a re-plan when the conditions have changed sufficiently
- **"Quality of service"** algorithms

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Part III - Planning and Coordination

- **Dynamic planning**
- Potential-based path planning
- Flocking
- Particle systems

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Dynamic Path Planning

Dynamic path planning: What happens when the environment changes after the plan has been made?

- The **player** alters the environment (e.g., blows up a bridge)
- Other **agents** get in the way
- Moving **objects** (e.g., falling debris) blocks the way

Possible approaches:

- Try to **avoid** the problem. (e.g. control your agents/world better)
- **Re-plan** when something goes wrong
- **Reactive** planning

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Avoiding Plan Changes

Partial planning: Only plan **short segments** of path at a time

- Stop A* after a path of some **length** is found, even if the goal is not reached - use best estimated path found so far
 - Extreme:** Use **greedy** search and only plan one step at a time
 - Common:** **Hierarchical planning** and only plan low level when needed
- Underlying idea is that a **short** path is **less likely** to change than a **long** path
- Optimality will be sacrificed
- **Side Benefit:** more uniform frame rates

Re-Planning: If your plan has gone **wrong**, create a **new** one,

- Assumes that the dynamic changes are now **permanent**,
- Usually used in conjunction with **avoidance** strategies:
 - Re-planning is **expensive**, so try to avoid having to do it
 - No point in generating a plan that will be **redone**

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Part III - Planning and Coordination

- Dynamic planning
- Potential-based path planning
- Flocking
- Particle systems

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Reactive Planning

Reactive Agent:

- Plans **one step at a time**
- Use only **local information** (not globally optimal)

Example: Potential-field path planning

- Set up a **repulsive field** around obstacles (and other agents)
- Set up an **attractive field** toward the goal
- The agent follows the gradient **downhill** to the goal, while the force field **pushes** it away from obstacles
- Can also model velocity and momentum - potential field defines a **force**

Why is this reactive?

- Agent's behavior depends only the **local gradient** at any instant

Widely used in low-level robotics navigation

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Potential Field Navigation

Key:

Red: Start point

Blue: Goal point

Green: Obstacles

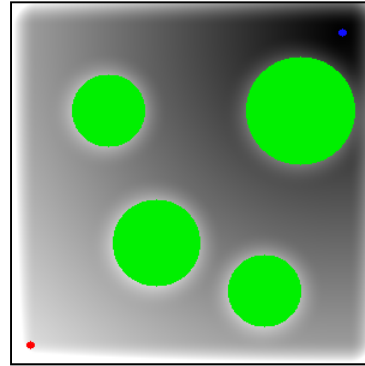
Field Strength: (Shown in gray scale)

Dark: Attractive

Light: Repulsive

Potential Function: is the sum of:

- **Repulsive force** around the obstacles (including the world boundary)
- **Attractive force** at the goal point



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Path Planning with Potential Fields

Potential-Field Navigation:

Intuition: Moving in 2D space, the potential field is a **terrain**. It is **hard** to move **uphill**, and **easy** to slide **downhill**.

Path Plan: Agent follows laws of **physics** and rolls downhill

More Formally: Your agent is moving subject to a **potential field** $U(p)$, that is defined at every point p of the environment. $U(p)$ defines the **strength** of the field (**height** of the terrain) at point p .

Gradient: Is a vector that points in the direction of **steepest descent**:

$$-\nabla U(p) = \left(-\frac{\partial U}{\partial x}, -\frac{\partial U}{\partial y} \right)^T$$

Force: The gradient behaves like a **force vector** $F(p) = -\nabla U(p)$, impelling the agent to steer downhill

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Defining the Fields

Attraction towards Goal:

Naïve: Simple **linear potential** based on the **distance** from the goal:

$$U_{\text{goal}}(p) = c \cdot \|p - p_{\text{goal}}\|$$

Where c is an adjustment parameter. Potential function is a cone.
The gradient is constant vector directed towards the goal.

Smarter: Use a **parabolic well potential**:

$$U_{\text{goal}}(p) = \frac{c}{2} \cdot \|p - p_{\text{goal}}\|^2$$

The gradient still points towards the goal, but the magnitude of the gradient vector **increases** linearly with the **distance** from the goal

$$\begin{aligned}\nabla U_{\text{goal}}(p) &= \nabla \frac{c}{2} \cdot \|p - p_{\text{goal}}\|^2 = \frac{c}{2} \cdot \nabla (\|p - p_{\text{goal}}\|^2) \\ &= c \cdot \|p - p_{\text{goal}}\| \left(\nabla \|p - p_{\text{goal}}\| \right)\end{aligned}$$

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Defining the Fields

Repulsion from Obstacles:

- Obstacle i contributes a field strength based on the distance from its boundary: $U_i(p) = f(\|p - \text{obst}_i\|)$, where f is an decreasing function of distance
- Typical **potential functions**: (c is adjustment parameter)
 - Quadratic/Polynomial**: $f(d) = c/d^2$, or generally $f(d) = c/d^p$
 - Negative Exponential**: $f(d) = c \cdot e^{-d}$
- **Taper** so that field at some distance is zero. Why?
- **Strength** determines how likely the agent is to **avoid** it

Total Field Strength: Add the sub-fields together

(Does this remind you of a modeling technique we discussed?)

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Following the Field

Steepest Descent:

- At each step, the agent needs to know which direction is "downhill"

Total field gradient:

Compute: Gradients of each sub-field and sum

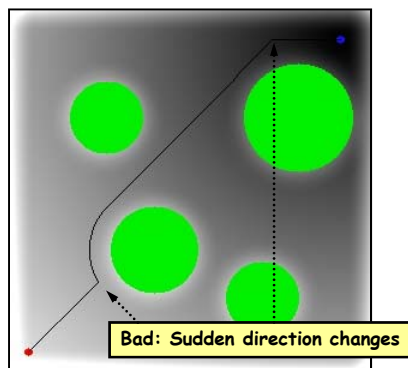
Gradient: The vector of **partial derivatives** in x, y, and z

Gradient induces a Force: (and hence, acceleration)

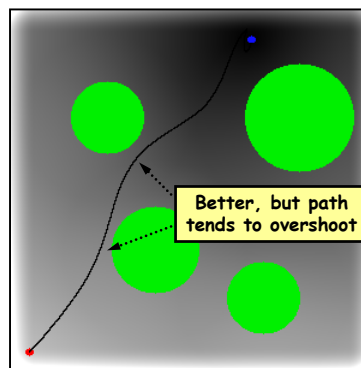
- Automatically **avoids sharp turns** and provides **smooth motion**
- Higher mass can make large objects turn more **slowly**
- Easy to make **frame-rate independent**
- But, high velocities can cause **collisions** if field is not **strong enough** to turn the object in time
- One solution is to **limit velocity** - want to do this anyway because the field is only a guide, not a true force

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Following the Field: Examples



No momentum - Go in direction of lowest field strength



Momentum - but with linear obstacle field strength and moved goal

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Discrete Approximation

Discretization: Compute the field on a grid

- Can **precompute** fixed sub-fields, e.g., for **fixed obstacles**
- Sub-fields for moving obstacles computed with each time step

Flow:

- Go to **neighboring node** with **smallest** field value

Pros & Cons:

- **Faster**
- Requires more **space** for grid
- Only **approximate**

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Potential Problems with Potential Fields

Requires lots of Tuning:

- **Strength** of the field around each obstacle
- **Function** for field strength around obstacle (quadratic, exp, etc)
- **Steepness** of force toward the goal
- **Maximum velocity** limit

Goals can conflict:

High field strength: Avoids collisions, but produces big forces and hence jerky motion

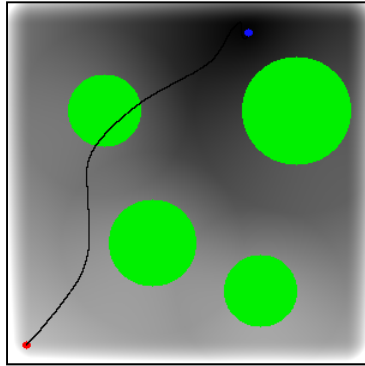
Low field strength: Smoother paths, but increases likelihood of collisions due to overshooting

Local minima:

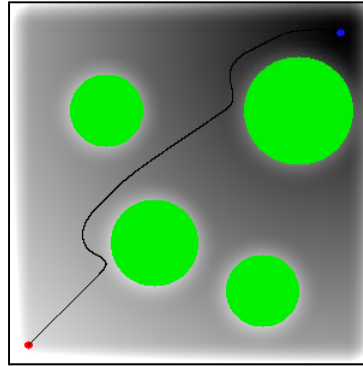
- Cannot see the "**big picture**." All decisions are **purely local**.
- May be arbitrarily far from optimal.
- Easy to get **trapped** in concavities

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Potential-Field Problems: Examples



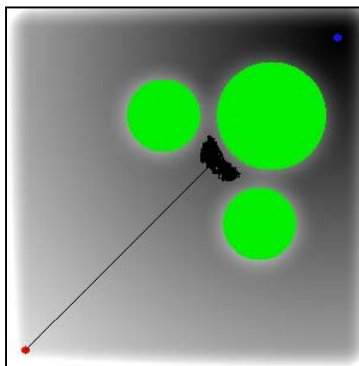
Field too weak:
Obstacle collision



Field too strong:
Jerky motion

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Potential-Field Problems: Examples



Getting stuck in local minima

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Local Minima Problem

Problem Source:

- Path planning is an **optimization** problem, typically with many **local minima**
- Potential field planning is a form of **gradient descent** optimization
- Gradient descent methods seek **local minima**, and will get stuck unless other techniques are applied

Possible Solutions:

Virtual Obstacles: Created at the point where the search gets stuck

Virtual Sub-Goals: Backtrack along the path and attract it in a new direction

Randomized Potential Field: Add a random noise to potential field values and try again. (Mixture of random walk and potential field.)

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Part III - Planning and Coordination

- Dynamic planning
- Potential-based path planning
- **Flocking**
- Particle systems

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Flocking

Motion of multiple agents: Objectives:

- **Collision avoidance**
- **Cohesion:**
 - Tendency to stick together
 - **Examples:** School of fish, flock of birds, herd of cattle
- **Common goal?**
 - Yes → Group should seek a common objective: A squadron of soldiers
 - No → Motion is independent: People walking in a crowded street

Emergent behavior:

- Define **simple rules** on individuals based on purely local information
- Each rule induces a **force**. Total force affects acceleration.
- Interesting **global behavior** naturally emerges as a result

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Flocking Rules

Boids: (virtual birds)

- Term coined by Craig Reynolds (1986)
- Behavior determined by the following 4 rules

Separation:

Avoid collisions with nearby boids
E.g., each boid generates a **repulsive potential field** of limited radius

Alignment:

Align flight direction with neighboring boids

Cohesion:

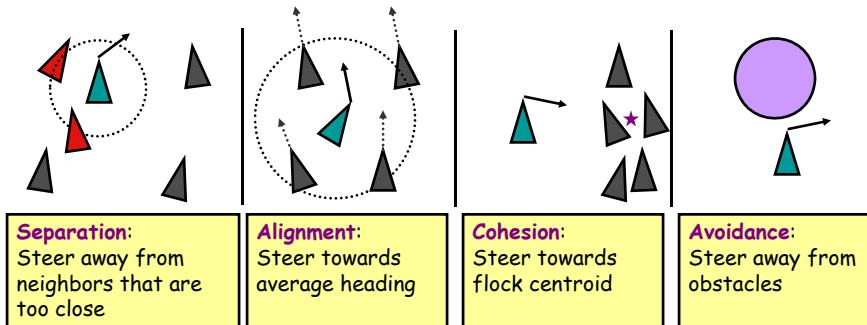
Attraction to centroid (center of mass) of the flock
E.g., flock centroid generates an **attractive potential field**

Avoidance:

Avoid obstacles in the environment
E.g., each obstacles generates a **repulsive potential field**

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Flocking Rules



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Combining Commands

Steering Rule:

- Steering rules act as **forces**; alter acceleration
- Set a **maximum acceleration** to avoid **jerky** behavior

Tuning Behavior:

- Assign a weight to each of the flocking rules
- Avoidance should be high
- Cohesion should be lower

Option 1: Apply rules in decreasing weight order, until max acceleration is reached

Responsive: Ensures that high priority forces are applied

Option 2: Take weighted sum and truncate to max acceleration

Fair: Ensures that all forces affect final motion

Demo: <http://www.red3d.com/cwr/boids/>

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Flocking Evaluation

Advantages:

Simple: Complex behavior from simple rules

Flexible: Many varieties of behavior from a small set of different rules and varying parameter settings

Disadvantages:

Tuning: Can be difficult to set parameters to achieve desired result

Local Minima: All the problems of potential fields regarding strength of forces

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Part III - Planning and Coordination

- Dynamic planning
- Potential-based path planning
- Flocking
- Particle systems

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General Particle Systems

Particle system:

- A variation on the theme of **flocking**
- Particles are **light-weight objects**: E.g., point masses
- Simple rules **control** how particles:
 - are born
 - move, grow/shrink, change appearance
 - die

Flexible: Can model many **complex, distributed phenomena**

- Fireworks
- Waterfalls, spray, foam
- Explosions (smoke, flame, chunks of debris)
- Clouds
- Crowds, flocks, herds

Widely used in movies and games

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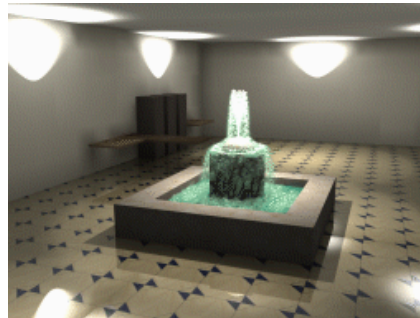
Particle System Demos

Demo source: Flow particle animation application by Mark B. Allan.

<http://users.rcn.com/mba.dnai/software/flow/>

Demos:

- [Kettle](#)
- [Face](#)
- [Smoke Ball](#)
- [Lava2](#)
- [Molten](#)



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Particle System Steps

1. Inject any **new particles** into the system and assign them their initial **attributes**
 - There may be multiple sources
 - Particles might be generated at **random** (clouds), in a **constant stream** (waterfall), or according to a **script** (fireworks)
2. **Remove** (kill) particles that have exceeded their **lifetime**
 - May have a fixed lifetime, or die on some condition
3. **Move** all the current particles according to their **scripts**
 - Script typically refers to the neighboring particles and the environment
4. **Render** all the current particles
 - Many options for rendering

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Particle System Example: Puffs of Smoke

Birth:

- Particles are spawned at a **constant rate**
- They have **zero initial velocity**, or maybe a small velocity away from the rocket

Update Rules:

- Particles rise or fall slowly (drift with the wind)
- Current particle state described by parameter, **size**, that grows quickly then falls over time

Death:

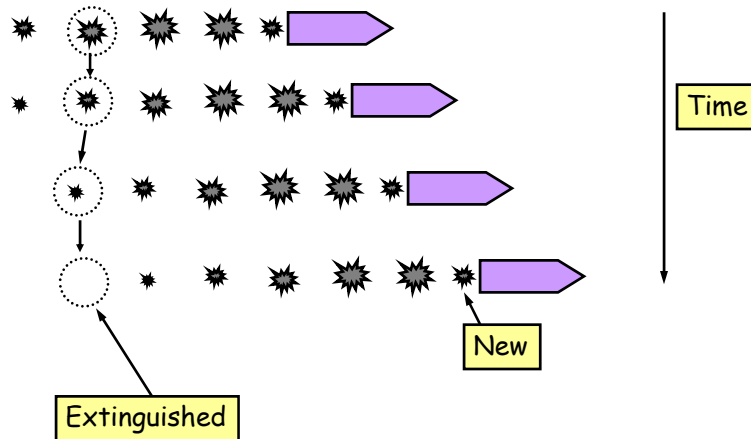
- Kill particle when **size** becomes very small

Render:

- Scale **size** depending on the value of size

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Particle System Example: Puffs of Smoke



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Particle System Example: Explosions

Birth:

- System starts when the target is **explodes**
- Target is broken into **many small pieces**
- One **particle** assigned for **each piece**
- Each particle is assigned an **initial velocity** away from the center of the explosion

Update Rules: Doesn't need to be perfect, just convincing

- Move **continuously** unless there is a **collision**
- Model accurate rigid body rotation, or just do **random rotation**
- Collisions handled as with **colliding balls**

Death: (not applicable)

Rendering:

- Draw the particle at the current position and orientation

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Summary

Part I: Basic AI Concepts

- AI Basics
- Agents
- Rule-based Approaches
- Finite-State Machines

Part II: Motion

- Configuration spaces
- Waypoints
- Path planning algorithms
- Navigation Interfaces

Part III: Planning and Coordination

- Dynamic planning
- Potential-based path planning
- Flocking
- Particle systems

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