Symbolic Execution
Introduction

• Static analysis is great
  ▪ Lots of interesting ideas and tools
  ▪ Commercial companies sell, use static analysis
  ▪ It all looks good on paper, and in papers

• But can developers use it?
  ▪ Our experience: Not easily
  ▪ Results in papers describe use by static analysis experts
  ▪ Commercial tools have a huge code mass to deal with developer confusion, false positives, warning management, etc
One Issue: Abstraction

• Abstraction lets us scale and model all possible runs
  - But it also introduces conservatism
  - *-sensitivities attempt to deal with this
    - * = flow-, context-, path-, field-, etc
  - But they are never enough

• Static analysis abstraction ≠ developer abstraction
  - Because the developer didn’t have them in mind
Symbolic Execution

• Testing works
  - But, each test only explores one possible execution
    - `assert(f(3) == 5)`
  - We hope test cases generalize, but no guarantees

• Symbolic execution generalizes testing
  - Allows unknown symbolic variables in evaluation
    - `y = α; assert(f(y) == 2*y-1);`
  - If execution path depends on unknown, conceptually fork symbolic executor
    - `int f(int x) { if (x > 0) then return 2*x - 1; else return 10; }`
Symbolic Execution Example

1. int a = α, b = β, c = γ;
2. // symbolic
3. int x = 0, y = 0, z = 0;
4. if (a) {
5.   x = -2;
6. }
7. if (b < 5) {
8.   if (!a && c) { y = 1; }
9.   z = 2;
10.}
11. assert(x+y+z!=3)
Insight

• Each symbolic execution path stands for *many* actually program runs
  ▪ In fact, exactly the set of runs whose concrete values satisfy the path condition
• Thus, we can cover a lot more of the program’s execution space than testing can
Early work on symbolic execution


The problem

• Computers were small (not much memory) and slow (not much processing power) then
  ▪ Apple’s iPad 2 is as fast as a Cray-2 from the 1980’s

• Symbolic execution is potentially extremely expensive
  ▪ Lots of possible program paths
  ▪ Need to query solver a lot to decide which paths are feasible, which assertions could be false
  ▪ Program state has many bits
Today

• Computers are much faster, memory is cheap

• There are very powerful SMT/SAT solvers today
  ▪ SMT = Satisfiability Modulo Theories = SAT++
  ▪ Can solve very large instances, very quickly
    - Lets us check assertions, prune infeasible paths
  ▪ We’ve used Z3, STP, and Yices

• Recent success: bug finding
  ▪ Heuristic search through space of possible executions
  ▪ Find really interesting bugs
Symbolic Execution for IMP

\[ a ::= n \mid X \mid a_0+a_1 \mid a_0-a_1 \mid a_0 \times a_1 \]
\[ b ::= bv \mid a_0=a_1 \mid a_0\leq a_1 \mid \neg b \mid b_0 \land b_1 \mid b_0 \lor b_1 \]
\[ c ::= \text{skip} \mid X:=a \mid \text{goto pc} \mid \text{if } b \text{ then } pc \mid \text{assert } b \]
\[ p ::= c; \ldots; c \]

- \( n \in \mathbb{N} \) = integers, \( X \in \text{Var} \) = variables, \( bv \in \text{Bool} = \{\text{true, false}\} \)
- This is a typical way of presenting a language
  - Notice grammar is for ASTs
    - Not concerned about issues like ambiguity, associativity, precedence
- Syntax stratified into commands (\( c \)) and expressions (\( a,b \))
  - Expressions have no side effects
- No function calls (and no higher order functions)
Interpretation for IMP

• See main.ml

• How to extend this to be a symbolic executor?
Symbolic Variables

- Add a new kind of expression

```ocaml
type aexpr = ... | ASym of string
type bexpr = ... | BSym of string
```

- The string is the variable name
- Naming variables is useful for understanding the output of the symbolic executor
Symbolic Expressions

• Now change `aeval` and `beval` to work with symbolic expressions

```ocaml
let rec aeval sigma = function
  | ASym s -> new_symbolic_variable 32 s (* 32-bit *)
  | APlus (a1, a2) ->
    symbolic_plus (aeval sigma a1) (aeval sigma a2)
  | ...

let rec beval sigma = function
  | BSym s -> new_symbolic_variable 1 s (* 1 bit *)
  | BLeq (a1, a2) ->
    symbolic_leq (aeval sigma a1) (aeval sigma a2)
  | ...
```
Symbolic State

• Previous step function, roughly speaking

\[
cstep : \sigma \to \text{pc} \to (\sigma', \text{pc}')
\]

• Now we have a couple of issues:
  - We need to keep track of the path condition
  - There may be more than one pc if we fork execution

• Convenient to package all this up in a record, and change \textit{cstep} appropriately

\[
\text{type state} = \{
    \sigma : (\text{string} \times \text{symbolic_expr}) \text{ list};
    \text{pc} : \text{int};
    \text{path} : \text{symbolic_expr};
\}
\]

\[
cstep : \text{state} \to \text{state} \times (\text{state option})
\]
Forking Execution

• How to decide which branches are feasible?
  ▪ Combine path condition with branch cond and ask solver!

```ocaml
let cstep st = function
  | CIf (b, pc’) ->
    let b’ = beval st.sigma b in
    let t_path_cond = symbolic_and st.path b’ in
    let f_path_cond = symbolic_and st.path (symbolic_not b’) in
    let maybe_t = satisfiable in
    let maybe_f = satisfiable in
    match maybe_t, maybe_f with
    | true, true -> (* true path *), Some (* false path *)
    | true, false -> (* true path *), None
    | false, true -> (* false path *), None
    | false, false -> (* impossible *)
```
1. create initial state
   - pc = 0, path cond = true, state = empty
2. push state onto worklist
3. while (worklist is not empty)
   3a. st = pull some state from worklist
   3b. st’, st’’ = cstep st
   3c. add st’ to worklist
   3d. add st’’ to worklist if st’’ = Some st’’
Path explosion

- Usually can’t run symbolic execution to exhaustion
  - Exponential in branching structure
    1. int a = α, b = β, c = γ; // symbolic
    2. if (a) ... else ...;
    3. if (b) ... else ...;
    4. if (c) ... else ...;
  - Ex: 3 variables, 8 program paths

- Loops on symbolic variables even worse
  1. int a = α; // symbolic
  2. while (a) do ...;
  3. - Potentially $2^{31}$ paths through loop!
Basic search

• Simplest ideas: algorithms 101
  ▪ Depth-first search (DFS)
  ▪ Breadth-first search (BFS)

• Potential drawbacks
  ▪ Neither is guided by any higher-level knowledge
    - Probably a bad sign
  ▪ DFS could easily get stuck in one part of the program
    - E.g., it could keep going around a loop over and over again
  ▪ Of these two, BFS is a better choice
Search strategies

• Need to prioritize search
  ▪ Try to steer search towards paths more likely to contain assertion failures
  ▪ Only run for a certain length of time
    - So if we don’t find a bug/vulnerability within time budget, too bad

• Think of program execution as a dag
  ▪ Nodes = program states
  ▪ Edge(n1,n2) = can transition from state n1 to state n2

• Then we need some kind of graph exploration strategy
  ▪ At each step, pick among all possible paths
Randomness

• We don’t know a priori which paths to take, so adding some randomness seems like a good idea
  ▪ Idea 1: pick next path to explore uniformly at random (Random Path, RP)
  ▪ Idea 2: randomly restart search if haven’t hit anything interesting in a while
  ▪ Idea 3: when have equal priority paths to explore, choose next one at random
    - All of these are good ideas, and randomness is very effective

• One drawback: reproducibility
  ▪ Probably good to use psuedo-randomness based on seed, and then record which seed is picked
  ▪ (More important for symbolic execution implementers than users)
Coverage-guided heuristics

• Idea: Try to visit statements we haven’t seen before
• Approach
  ■ Score of statement = # times it’s been seen and how often
  ■ Pick next statement to explore that has lowest score
• Why might this work?
  ■ Errors are often in hard-to-reach parts of the program
  ■ This strategy tries to reach everywhere.
• Why might this not work?
  ■ Maybe never be able to get to a statement if proper precondition not set up
• KLEE = RP + coverage-guided
Generational search

- Hybrid of BFS and coverage-guided
- Generation 0: pick one program at random, run to completion
- Generation 1: take paths from gen 0, negate one branch condition on a path to yield a new path prefix, find a solution for that path prefix, and then take the resulting path
  - Note will semi-randomly assign to any variables not constrained by the path prefix
- Generation n: similar, but branching off gen n-1
- Also uses a coverage heuristic to pick priority
Combined search

- Run multiple searches at the same time
- Alternate between them
  - E.g., Fitnext

- Idea: no one-size-fits-all solution
  - Depends on conditions needed to exhibit bug
  - So will be as good as “best” solution, which a constant factor for wasting time with other algorithms
  - Could potentially use different algorithms to reach different parts of the program
SMT solver performance

• SAT solvers are at core of SMT solvers
  - In theory, could reduce all SMT queries to SAT queries
  - In practice, SMT and higher-level optimizations are critical

• Some examples
  - Simple identities \( x + 0 = x, x \times 0 = 0 \)
  - Theory of arrays \( \text{read}(42, \text{write}(42, x, A)) = x \)
    - \( 42 = \) array index, \( A = \) array, \( x = \) element
  - Caching (memoize solver queries)
  - Remove useless variables
    - E.g., if trying to show path feasible, only the part of the path condition related to variables in guard are important
Libraries and native code

- At some point, symbolic execution will reach the “edges” of the application
  - Library, system, or assembly code calls
- In some cases, could pull in that code also
  - E.g., pull in libc and symbolically execute it
  - But glibc is insanely complicated
    - Symbolic execution can easily get stuck in it
  - ⇒ pull in a simpler version of libc, e.g., newlib
    - libc versions for embedded systems tend to be simpler
- In other cases, need to make models of code
  - E.g., implement ramdisk to model kernel fs code
  - This is a lot of work!
Concolic execution

- Also called *dynamic symbolic execution*
- Instrument the program to do symbolic execution as the program runs
  - i.e., shadow concrete program state with symbolic variables
- Explore one path, from start to completion, at a time
  - Thus, always have a concrete underlying value to rely on
Concretization

• Concolic execution makes it really easy to concretize
  ▪ Replace symbolic variables with concrete values that satisfy the path condition
    - Always have these around in concolic execution

• So, could actually do system calls
  ▪ But we lose symbolic-ness at such calls

• And can handle cases when conditions too complex for SMT solver
  ▪ But can do the same in pure symbolic system
Resurgence of symbolic exection

- Two key systems that triggered revival of this topic:
  - DART — Godefroid and Sen, PLDI 2005
    - Godefroid = model checking, formal systems background
  - EXE — Cadar, Ganesh, Pawlowski, Dill, and Engler, CCS 2006
    - Ganesh and Dill = SMT solver called “STP” (used in implementation)
      - Theory of arrays
    - Cadar and Engler = systems
Recent successes

• SAGE
  ▪ Microsoft internal tool
  ▪ Symbolic execution to find bugs in file parsers
    - E.g., JPEG, DOCX, PPT, etc
  ▪ Cluster of $n$ machines continually running SAGE

• KLEE
  ▪ Open source symbolic executor
  ▪ Runs on top of LLVM
  ▪ Has found lots of problems in open-source software
KLEE: Coverage for Coreutils

Figure 6: Relative coverage difference between KLEE and the COREUTILS manual test suite, computed by subtracting the executable lines of code covered by manual tests ($L_{man}$) from KLEE tests ($L_{klee}$) and dividing by the total possible: $(L_{klee} - L_{man})/L_{total}$. Higher bars are better for KLEE, which beats manual testing on all but 9 applications, often significantly.
KLEE: Coreutils crashes

Figure 7: KLEE-generated command lines and inputs (modified for readability) that cause program crashes in COREUTILS version 6.10 when run on Fedora Core 7 with SELinux on a Pentium machine.
Research tools at UMD

• Otter — symbolic executor for C
  ▪ Better library model than KLEE, support for multiprocess symbolic execution

• RubyX — symbolic executor for Ruby

• SymDroid — symbolic executor for Dalvik bytecode
Other symbolic executors

• Cloud9 — parallel symbolic execution, also supports threads
• Pex — symbolic execution for .NET
• jCUTE — symbolic execution for Java
• Java PathFinder — a model checker that also supports symbolic execution