

CMSC 330: Organization of Programming Languages

Logic Programming with Prolog

CMSC 330

1

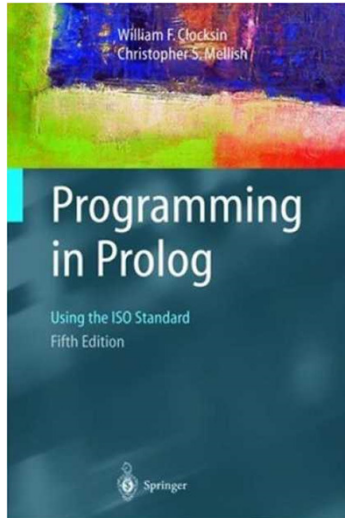
Background

- ▶ 1972, University of Aix-Marseille
- ▶ Original goal: Natural language processing
- ▶ At first, just an interpreter written in Algol
 - Compiler created at Univ. of Edinburgh

CMSC 330

2

More Information On Prolog



- ▶ Various tutorials available online
- ▶ Links on webpage

CMSC 330

3

Logic Programming

- ▶ At a high level, logic programs model the relationship between “objects”
 1. Programmer specifies relationships at a high level
 2. Language builds a database
 3. Programmer then queries this database
 4. Language searches for answers

CMSC 330

4

Features of Prolog

- ▶ Declarative
 - Specify what goals you want to prove, not how to prove them (mostly)
- ▶ Rule based
- ▶ Dynamically typed
- ▶ Several built-in datatypes
 - Lists, numbers, records, ... but no functions
- ▶ Several other logic programming languages
 - Datalog is simpler; CLP and λ Prolog more feature-ful
 - Erlang borrows some features from Prolog

CMS3 330

5

A Small Prolog Program – Things to Notice

Use `/* */` for comments, or `%` for 1-liners

Period ends statements

Lowercase logically terminates

Program consists of facts and rules

Uppercase denotes variables

```
/* A small Prolog program */  
female(alice).  
male(bob).  
male(charlie).  
father(bob, charlie).  
mother(alice, charlie).  
  
% "X is a son of Y"  
son(X, Y) :- father(Y, X), male(X).  
son(X, Y) :- mother(Y, X), male(X).
```

6

Running Prolog (Interactive Mode)

Navigating location and loading program at top level

```
?- working_directory(C,C). ← Find current directory
C = 'c:/windows/system32/'.

?- working_directory(C,'c:/Users/me/desktop/p6'). ← Set directory
C = 'c:/Users/me/desktop/'.

?- ['01-basics.pl']. ← Load file 01-basics.pl
% 01-basics.pl compiled 0.00 sec, 17 clauses
true.

?- make. ← Reload modified files; replace rules
true.
```

CMSC 330

7

Running Prolog (Interactive Mode)

Listing rules and entering queries at top level

```
?- listing(son). ← List rules for son
son(X, Y) :-
    father(Y, X),
    male(X).
son(X, Y) :-
    mother(Y, X),
    male(X).
true.

?- son(X,Y).
X = charlie,
Y = bob;
X = charlie,
Y = alice.
```

Multiple answers

User types ; to request additional answer

User types return to complete request

CMSC 330

8

Style

One predicate per line

```
blond(X) :-  
    father(Father, X),  
    blond(Father),      % father is blond  
    mother(Mother, X),  
    blond(Mother).      % and mother is blond
```

Descriptive variable names

Inline comments with % can be useful

CMSC 330

9

Outline

- ▶ Syntax, terms, examples
- ▶ Unification
- ▶ Arithmetic / evaluation
- ▶ Programming conventions
- ▶ Goal evaluation
 - Search tree, clause tree
- ▶ Lists
- ▶ Built-in operators
- ▶ Cut, negation

CMSC 330

10

Prolog Syntax and Terminology

► Terms

- **Atoms:** begin with a lowercase letter
horse underscores_ok numbers2
- **Numbers**
123 -234 -12e-4
- **Variables:** begin with uppercase or _ “don't care” variables
X Biggest_Animal _the_biggest1 
- **Compound terms:** functor(arguments)
bigger(horse, duck)
bigger(X, duck)
f(a, g(X, _), Y, _)
No blank spaces between functor and (arguments)

CMS3 330

11

Prolog Syntax and Terminology (cont.)

► Clauses

- **Facts:** define predicates, terminated by a period
bigger(horse, duck).
bigger(duck, gnat).
Intuitively: “this particular relationship is true”
- **Rules:** Head :- Body
is_bigger(X,Y) :- bigger(X,Y).
is_bigger(X,Y) :- bigger(X,Z), is_bigger(Z,Y).
Intuitively: “Head if Body”, or “Head is true if each of the subgoals can be shown to be true”

- A **program** is a sequence of clauses

CMS3 330

12

Prolog Syntax and Terminology (cont.)

► Queries

- To “run a program” is to submit queries to the interpreter
- Same structure as the body of a rule
 - Predicates separated by commas, ended with a period
- Prolog tries to determine whether or not the predicates are true

?- is_bigger(horse, duck).

?- is_bigger(horse, X).

“Does there exist a substitution for X such that is_bigger(horse,X)?”

CMS 330

13

Unification – The ^{Without which, nothing} Sine Qua Non of Prolog

► Two terms unify **if and only if**

- They are identical
- They can be made identical by **substituting** variables

?- gnat = gnat.

true.

?- is_bigger(X, gnat) = is_bigger(horse, gnat).

X = horse.

} This is the substitution: what X must be for the two terms to be identical.

?- pred(X, 2, 2) = pred(1, Y, X)

false

Sometimes there are multiple possible substitutions; Prolog can be asked to enumerate them all

?- pred(X, 2, 2) = pred(1, Y, _)

X = 1,

Y = 2.

CMS 330

14

The = Operator

- ▶ For unification (matching)
- ▶ `?- 9 = 9.`
`true.`
`?- 7 + 2 = 9.`
`false.`
- ▶ Why? Because these terms do not match
 - `7+2` is a compound term (e.g., `+(7,2)`)
- ▶ Prolog does not evaluate either side of =
 - Before trying to match

CMSC 330

15

The is Operator

- ▶ For arithmetic operations
- ▶ “LHS **is** RHS”
 - First **evaluate** the RHS (and RHS only!) to value V
 - Then match: `LHS = V`
- ▶ Examples

<code>?- 9 is 7+2.</code> <code>true.</code>	<code>?- 7+2 is 9.</code> <code>false.</code>
<code>?- X = 7+2.</code> <code>X = 7+2.</code>	<code>?- X is 7+2.</code> <code>X = 9.</code>

CMSC 330

16

No Assignment

- ▶ `=` and `is` operators do not perform assignment
- ▶ Example
 - `foo(...,X) :- ... X = 1,...` % true only if `X = 1`
 - `foo(...,X) :- ... X = 1, ..., X = 2, ...` % always fails
 - `foo(...,X) :- ... X is 1,...` % true only if `X = 1`
 - `foo(...,X) :- ... X is 1, ..., X is 2, ...` % always fails

X can't be unified with 1 & 2 at the same time

CMS 330

17

Function Parameter & Return Value

- ▶ Code example

Parameter
Return value

```
increment(X,Y) :-  
    Y is X+1.  
?- increment(1,Z).  
Z = 2.  
?- increment(1,2).  
true.  
?- increment(Z,2).  
ERROR: incr/2: Arguments are not sufficiently instantiated
```

Query
Result

Can't evaluate `X+1`
since `X` is not yet
instantiated to int

CMS 330

18

Function Parameter & Return Value

- Code example

`addN(X,N,Y) :-`
`Y is X+N.`

`?- addN(1,2,Z).` ← Query
`Z = 3.` ← Result

Parameters
Return value

CMSC 330

19

Recursion

- Code example

`addN(X,0,X).` ← Base case
`addN(X,N,Y) :-` ← Inductive step
 `X1 is X+1,`
 `N1 is N-1,`
 `addN(X1,N1,Y).` ← Recursive call

`?- addN(1,2,Z).`
`Z = 3.`

CMSC 330

20

Factorial

- Code

```
factorial(0,1).  
factorial(N,F) :-  
    N > 0,  
    N1 is N-1,  
    factorial(N1,F1),  
    F is N*F1.
```

Tail Recursive Factorial w/ Accumulator

- Code

```
tail_factorial(0,F,F).  
tail_factorial(N,A,F) :-  
    N > 0,  
    A1 is N*A,  
    N1 is N -1,  
    tail_factorial(N1,A1,F).
```

And and OR

- ▶ And
 - To implement $X \text{ \&\& } Y$ (use $,$ in body of clause)
 - Example
 - $Z \text{ :- } X, Y.$
- ▶ OR
 - To implement $X \text{ || } Y$ (use two clauses)
 - Example
 - $Z \text{ :- } X.$
 - $Z \text{ :- } Y.$

CMSC 330

23

Goal Execution

- ▶ When submitting a query, we ask Prolog to substitute variables as necessary to make it true
- ▶ Prolog performs **goal execution** to find a solution
 - Start with the goal
 - Try to unify the head of a rule with the current goal
 - The rule hypotheses become subgoals
 - Substitutions from one subgoal constrain solutions to the next
 - If it reaches a dead end, it **backtracks**
 - Tries a different rule
 - When it can backtrack no further, it reports **false**
- ▶ More advanced topics later – cuts, negation, etc.

CMSC 330

24

Goal Execution (cont.)

- ▶ Consider the following:
 - “All men are mortal”
`mortal(X) :- man(X).`
 - “Socrates is a man”
`man(socrates).`
 - “Is Socrates mortal?”
`?- mortal(socrates).`
`true.`
 - ▶ How did Prolog infer this?
1. Sets `mortal(socrates)` as the initial goal
 2. Sees if it unifies with the head of any clause:
`mortal(socrates) = mortal(X).`
 3. `man(socrates)` becomes the new goal (since `X=socrates`)
 4. Recursively scans through all clauses, **backtracking** if needed ...

CMS 330

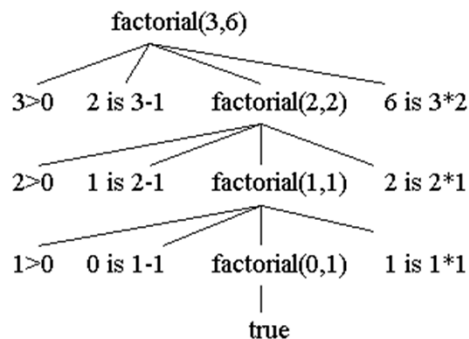
25

Clause Tree

- ▶ Clause tree
 - Shows (recursive) evaluation of all clauses
 - Shows value (instance) of variable for each clause
 - Clause tree is true if all leaves are true

Factorial example

```
factorial(0,1).
factorial(N,F) :-
    N > 0,
    N1 is N-1,
    factorial(N1,F1),
    F is N*F1.
```



CMS 330

26

Tracing

- ▶ `trace` lets you step through a goal's execution
 - `notrace` turns it off

```
1 my_last(X, [X]).  
2 my_last(X, [_|T]) :-  
  my_last(X, T).  
  
?- trace.  
true.  
  
[trace] ?- my_last(X, [1,2,3]).  
2 Call: (6) my_last(_G2148, [1, 2, 3]) ? creep  
2 Call: (7) my_last(_G2148, [2, 3]) ? creep  
1 Call: (8) my_last(_G2148, [3]) ? creep  
Exit: (8) my_last(3, [3]) ? creep  
Exit: (7) my_last(3, [2, 3]) ? creep  
Exit: (6) my_last(3, [1, 2, 3]) ? creep  
X = 3
```

CMSC 330

27

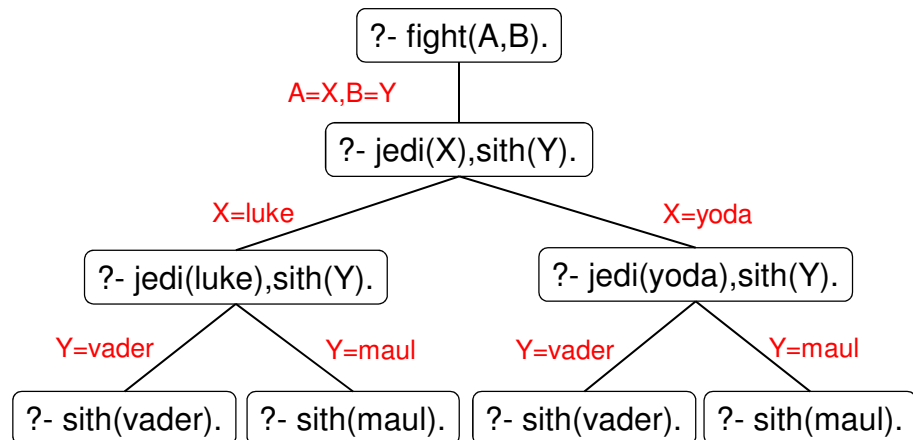
Goal Execution – Backtracking

- ▶ Clauses are tried in order
 - ▶ If clause fails, try next clause, if available
 - ▶ Example
- | | |
|--|-----------------------------|
| <code>jedi(luke).</code> | <code>?- fight(A,B).</code> |
| <code>jedi(yoda).</code> | <code>A=luke,</code> |
| <code>sith(vader).</code> | <code>B=vader;</code> |
| <code>sith(maul).</code> | <code>A=luke,</code> |
| <code>fight(X,Y) :- jedi(X), sith(Y).</code> | <code>B=maul;</code> |
| | <code>A=yoda,</code> |
| | <code>B=vader;</code> |
| | <code>A=yoda,</code> |
| | <code>B=maul.</code> |

CMSC 330

28

Prolog (Search / Proof / Execution) Tree



CMSC 330

29

Lists In Prolog

- ▶ `[a, b, 1, 'hi', [X, 2]]`
- ▶ But really represented as compound terms
 - `[]` is an atom
 - `[a, b, c]` is represented as `.(a, .(b, .(c, [])))`
- ▶ Matching over lists
 - `?- [X, 1, Z] = [a, _, 17]`
 - `X = a,`
 - `Z = 17.`

CMSC 330

30

List Deconstruction

- ▶ Syntactically similar to Ocaml: `[H|T]` like `h::t`
 ?- [Head | Tail] = [a,b,c].
 Head = a,
 Tail = [b, c].

 ?- [1,2,3,4] = [_, X | _].
 X = 2
- ▶ This is sufficient for defining complex predicates
- ▶ Let's define `concat(L1, L2, C)`
 ?- concat([a,b,c], [d,e,f], X).
 X = [a,b,c,d,e,f].

CMSC 330

31

Example: Concatenating Lists

- ▶ To program this, we define the “rules” of concatenation
 - If L1 is empty, then $C = L2$
 `concat( [], L2, L2 ).`
 - Prepending a new element to L1 prepends it to C, so long as C is the concatenation of L1 with some L2

`concat([E | L1], L2, [E | C]) :-
 concat(L1, L2, C).`

- ▶ ... and we're done

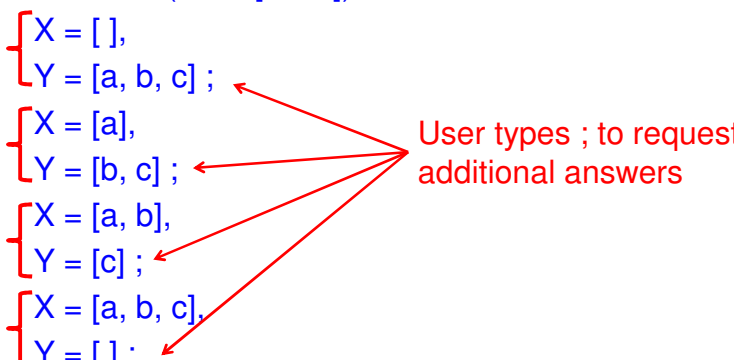
CMSC 330

32

Why Is The Return Value An Argument?

- Now we can ask **what inputs lead to an output**

```
?- concat(X, Y, [a,b,c]).
```



- `X = [ ],`
`Y = [a, b, c] ;`
- `X = [a,`
`Y = [b, c] ;`
- `X = [a, b,`
`Y = [c] ;`
- `X = [a, b, c],`
`Y = [ ] ;`

CMS3 330

33

Built-in List Predicates

- **length**
`?- length([a, b, [1,2,3] ], Length).`
`Length = 3.`
- **member**
`?- member(duey, [huey, duey, luey]).`
`true.`
- **select**
`?- select(duey, [huey, duey, luey], X).`
`X = [huey, luey].`
- See documentation for more
 - <http://www.swi-prolog.org/pldoc/man?section=builtin>

CMS3 330

34

More Syntax: Built-in Predicates

- ▶ Equality (a.k.a. **unification**)
 $X = Y$ $f(1,X,2) = f(Y,3,_)$
- ▶ **fail** and **true**
- ▶ “Consulting” (loading) programs
 $?- \text{consult('file.pl')}$ $?- [\text{'file.pl'}]$
- ▶ Output/Input
 $?- \text{write('Hello world'), nl}$ $?- \text{read(X)}.$
- ▶ (Dynamic) type checking
 $?- \text{atom(elephant)}$ $?- \text{atom(Elephant)}$
- ▶ **help**

CMSC 330

35

The **==** Operator

- ▶ For identity comparisons
- ▶ $X == Y$
 - Returns true if and only if X and Y are identical
- ▶ Examples

$?- 9 == 9.$	$?- 9 == 7+2.$
true.	false.
$?- X == 9.$	$?- X == Y.$
False.	false.
$?- X == X.$	$?- 7+2 == 7+2.$
true.	true.

CMSC 330

36

The $==$ Operator

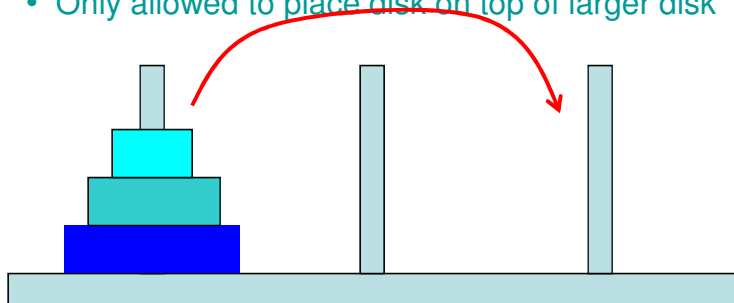
- ▶ For arithmetic operations
- ▶ “LHS $==$ RHS”
 - Evaluate the LHS to value V1 (Error if not possible)
 - Evaluate the RHS to value V2 (Error if not possible)
 - Then match: $V1 = V2$
- ▶ Examples
 - ?- 7+2 $==$ 9. ?- 7+2 $==$ 3+6.
true. true.
 - ?- X $==$ 9. ?- X $==$ 7+2
Error: $==/2$: Arguments are not sufficiently instantiated

CMS3 330

37

Example – Towers of Hanoi

- ▶ Problem
 - Move stack of disks between pegs
 - Can only move top disk in stack
 - Only allowed to place disk on top of larger disk



Example – Towers of Hanoi

- ▶ To move a stack of n disks from peg X to Y
 - Base case
 - If $n = 1$, move disk from X to Y
 - Recursive step
 1. Move top $n-1$ disks from X to 3rd peg
 2. Move bottom disk from X to Y
 3. Move top $n-1$ disks from 3rd peg to Y

Iterative algorithm would take much longer to describe!

Towers of Hanoi

- ▶ Code

```
move(1,X,Y,_) :-  
    write('Move top disk from '), write(X),  
    write(' to '), write(Y), nl.  
move(N,X,Y,Z) :-  
    N>1,  
    M is N-1,  
    move(M,X,Z,Y),  
    move(1,X,Y,_),  
    move(M,Z,Y,X).
```

Prolog Terminology

- ▶ A query, goal, or term where variables do not occur is called **ground**; else it's **nonground**
 - foo(a,b) is **ground**; bar(X) is **nonground**
- ▶ A **substitution** θ is a partial map from variables to terms where $\text{domain}(\theta) \cap \text{range}(\theta) = \emptyset$
 - Variables are terms, so a substitution can map variables to other variables, but not to themselves
- ▶ A is an **instance** of B if there is a substitution such that $A = B\theta$ ← The substitution θ applied to B
- ▶ C is a **common instance** of A and B if it is an instance of A and an instance of B

CMSC 330

41

Prolog's Algorithm Solve()

Solve(goal G , program P , substitution θ) =

- ▶ Suppose G is $A_1, \dots, A_n$. Choose goal A_1 . ← Starts as empty
- ▶ For each clause $A :- B_1, B_2, \dots, B_k$ in P ,
 - if θ_1 is the **mg**u of A and $A_1\theta$ then ← Chooses goals in order
 - ▶ If **Solve**($\{B_1, \dots, B_k, A_2, \dots, A_n\}, P, \theta \cdot \theta_1$) = some θ' then **return** θ'
 - ▶ (else it has failed, so we continue the for loop)
 - (else unification has failed, so try another rule)
- ▶ If loop exits return **fail** ← Implements backtracking
- ▶ **Output**: θ s.t. $G\theta$ can be deduced from P , or fail

Most
General
Unifier

CMSC 330

42

! : a.k.a. “cut”

- ▶ When a **!** is reached, it succeeds and commits Prolog to all the choices made since the parent goal was unified with the head of the clause the cut occurs in
 - Suppose we have clause **C** which is
 $A :- B_1, \dots, B_k, !, \dots, B_n.$
 - If the current goal unifies with **A**, and $B_1, \dots, B_k$ further succeed, the program is committed to the choice of **C** for the goal.
 - ▶ If any B_i for $i > k$ fail, backtracking only goes as far as the cut.
 - ▶ If the cut is reached when backtracking, **the goal fails**

CMSC 330

43

Cut

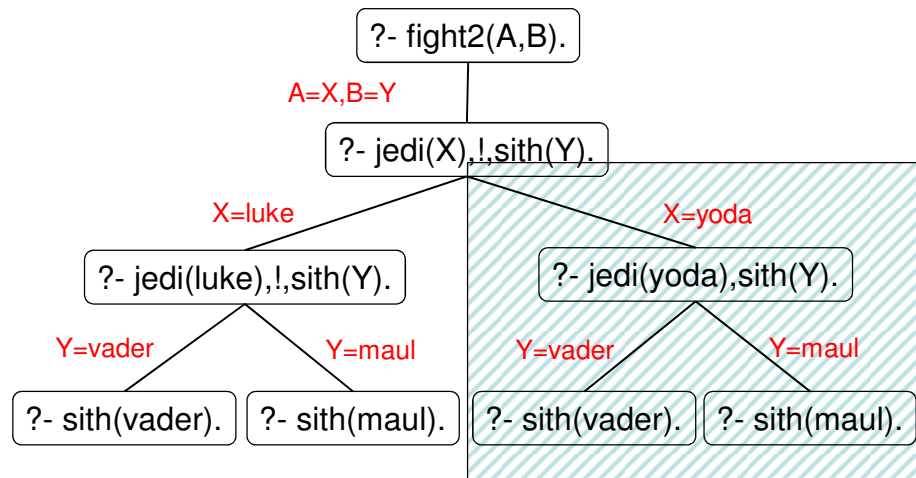
- ▶ Limits backtracking to predicates to **right** of cut
- ▶ Example

jedi(luke).	?- fight2(A,B).
jedi(yoda).	A=luke,
sith(vader).	B=vader;
sith(maul).	A=luke,
fight2(X,Y) :- jedi(X), ! , sith(Y).	B=maul.
fight3(X,Y) :- jedi(X), sith(Y), ! .	?- fight3(A,B).
	A=luke,
	B=vader.

CMSC 330

44

Prolog Search Tree Limited By Cut



CMSC 330

45

What Exactly Is Cut Doing?

Prunes all clauses below it

Prunes alternative solutions to its left

Does *not* affect the goals to its right

~~merge([X|Xs], [Y|Ys], [X|Zs]) :-~~

~~X < Y, !,~~
merge(Xs, [Y|Ys], Zs).

~~merge([X|Xs], [Y|Ys], [X,Y|Zs]) :-~~

~~X =:= Y, !,~~
~~merge(Xs, Ys, Zs).~~

~~merge([X|Xs], [Y|Ys], [Y|Zs]) :-~~

~~X > Y, !,~~
~~merge([X|Xs], Ys, Zs).~~

~~merge(Xs, [], Xs) :- !~~

~~merge([], Ys, Ys) :- !.~~

CMSC 330

46

Why Use Cuts?

- ▶ Save time and space, or eliminate redundancy
 - Prune useless branches in the search tree
 - If sure these branches will not lead to solutions
 - These are green cuts
- ▶ Guide to the search to a different solution
 - Change the meaning of the program
 - Intentionally returning only subset of possible solutions
 - These are red cuts

CMSC 330

47

Negation As Failure

- ▶ Cut may be used implement negation (not)
- ▶ Example

```
not(X) :- call(X), !, fail.  
not(X).
```
- ▶ If *X* succeeds, then the cut is reached, committing it; *fail* causes the whole thing to fail
- ▶ If *X* fails, then the second rule is reached, and the overall goal succeeds.
 - FYI, *X* here refers to an arbitrary goal
 - Effect of not depends crucially on rule order

CMSC 330

48

Not

- ▶ Not is tricky to use
 - Does not mean “not true”
 - Just means “not provable at this time”
- ▶ Example

```
jedi(luke).
sith(vader).
```

```
?-
not(jedi(vader)).
true.
?- not(sith(vader)).
false.
?- not(jedi(leia)).
true.
?- not(sith(leia)).
true.
?- not(jedi(X)).
false.
```

CMS3 330

49

Not (cont.)

- ▶ Ordering of clauses matters
- ▶ Example

```
jedi(luke).
sith(vader).
true_jedi1(X) :-
    jedi(X), not(sith(X)).
true_jedi2(X) :-
    not(sith(X)), jedi(X).
```

```
?- true_jedi1(luke).
true.
?- true_jedi1(X).
X=luke.
?- true_jedi2(luke).
true.
?- true_jedi2(X).
false.
```


X=vader causes not(sith(X)) to fail;
Will not backtrack to X=luke, since
sith(Luke) is not a fact

CMS3 330

50

Not and \=

- ▶ Built-in operators
 - \+ is not
 - $X \backslash= Y$ is same as $\text{not}(X=Y)$
 - $X \backslash== Y$ is same as $\text{not}(X==Y)$
- ▶ So be careful using \=
 - Ordering of clauses matters
 - Try to ensure operands of \= are instantiated

CMSC 330

51

Example Using \=

- ▶ Example

```
jedi(luke).
jedi(yoda).
help2(X,Y) :- jedi(X), jedi(Y), X \= Y.
help3(X,Y) :- jedi(X), X \= Y, jedi(Y).
help4(X,Y) :- X \= Y, jedi(X), jedi(Y).
```
- ```
?- help2(X,Y).
X=luke,
Y=yoda;
X=yoda,
Y=luke.
?- help3(X,luke).
X=yoda.
?- help3(X,Y).
false.
?- help4(X,luke).
false.
?- help4(yoda,luke).
true.
```

CMSC 330

52

## Prolog Summary

---

- ▶ General purpose logic programming language
  - Associated with AI, computational linguistics
  - Also used for theorem proving, expert systems
- ▶ Declarative programming
  - Specify facts & relationships between facts (rules)
  - Run program as queries over these specifications
- ▶ Natural support for
  - Searching within set of constraints
  - Backtracking