# CMSC 330: Organization of Programming Languages

#### Logic Programming with Prolog

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#### Background

- ▶ 1972, University of Aix-Marseille
- Original goal: Natural language processing
- At first, just an interpreter written in Algol
  - Compiler created at Univ. of Edinburgh

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More Information On Prolog



- Various tutorials available online
- Links on webpage
- We will use SWI Prolog
   <u>http://www.swi-prolog.org/</u>
   swipl, on Grace

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# Logic Programming

- At a high level, logic programs model the relationship between "objects"
  - 1. Programmer specifies relationships at a high level

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- 2. Language builds a database
- 3. Programmer then queries this database
- 4. Language searches for answers

#### **Features of Prolog**

- Declarative
  - Specify what goals you want to prove, not how to prove them (mostly)
- Rule based
- Dynamically typed
- Several built-in datatypes
  - Lists, numbers, records, ... but no functions
- Several other logic programming languages
  - Datalog is simpler; CLP and  $\lambda Prolog$  more feature-ful

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Erlang borrows some features from Prolog

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#### A Small Prolog Program – Things to Notice



#### Running Prolog (Interactive Mode)

Navigating location and loading program at top level

?- working\_directory(C,C). Find current directory
C = 'c:/windows/system32/'.

?- working\_directory(C,'c:/Users/me/desktop/p6'). Set directory
C = 'c:/Users/me/desktop/'.

?- ['01-basics.pl']. Load file 01-basics.pl
% 01-basics.pl compiled 0.00 sec, 17 clauses
true.

?- make. Reload modified files; replace rules true.

# Running Prolog (Interactive Mode)



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#### **Style**



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# Prolog Syntax and Terminology



# Outline

- Syntax, terms, examples
- Unification
- Arithmetic / evaluation
- Programming conventions
- Goal evaluation
  - · Search tree, clause tree
- Lists
- Built-in operators
- Cut, negation

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# Prolog Syntax and Terminology (cont.)

- Clauses
  - Facts: define predicates, terminated by a period bigger(horse, duck). bigger(duck, gnat). Intuitively: "this particular relationship is true" • Rules: Head :- Body
  - is bigger(X,Y) := bigger(X,Y). is\_bigger(X,Y) :- bigger(X,Z), is\_bigger(Z,Y). Intuitively: "Head if Body", or "Head is true if each of the subgoals can be shown to be true"
- A program is a sequence of clauses

#### Without which, nothing Unification – The Sine Qua Non of Prolog Prolog Syntax and Terminology (cont.) Two terms unify if and only if Queries To "run a program" is to submit gueries to the · They are identical interpreter ?- gnat = gnat. true. • Same structure as the body of a rule They can be made identical by substituting variables > Predicates separated by commas, ended with a period ?- is\_bigger(X, gnat) = is\_bigger(horse, gnat). Prolog tries to determine whether or not the X = horse. This is the substitution: what X must be predicates are true for the two terms to be identical. (X, 2, 2) = pred(1, Y, X)?- is bigger(horse, duck). false ?- is bigger(horse, X). ?- pred(X, 2, 2) = pred(1, Y, \_) Sometimes there are multiple "Does there exist a substitution for X such that possible substitutions; Prolog can X = 1, is\_bigger(horse,X)?" be asked to enumerate them all Y = 2.

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# The = Operator

- For unification (matching)
- ▶ ?- 9 = 9. true.

?- 7 + 2 = 9. false.

- Why? Because these terms do not match
  - 7+2 is a compound term (e.g., +(7,2))
- Prolog does not evaluate either side of =
  - Before trying to match

# The is Operator

- For arithmetic operations
- "LHS is RHS"

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- First evaluate the RHS (and RHS only!) to value V
- Then match: LHS = V
- Examples

?- 9 is 7+2.	?- 7+2 is 9.
true.	false.
?- X = 7+2.	?- X is 7+2.
X = 7+2.	X = 9.

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# No Variable Assignment

- and is operators do not perform assignment
- Example
  - foo(...,X) :- ... X = 1,... % true only if X = 1
  - foo(...,X) :- ... X = 1, ..., X = 2, ... % always fails
  - foo(...,X) :- ... X is 1,... % true only if X = 1
  - foo(...,X) :- ... X is 1, ..., X is 2, ... % always fails

#### X can't be unified with 1 & 2 at the same time

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#### Function Parameter & Return Value

Code example



#### **Function Parameter & Return Value**



#### Recursion

► Code example addN(X,0,X). Base case addN(X,N,Y) :- Inductive step X1 is X+1, N1 is N-1, addN(X1,N1,Y). Recursive call ?- addN(1,2,Z). Z = 3.

#### Factorial

#### Code

factorial(0,1). factorial(N,F) :-N > 0, N1 is N-1, factorial(N1,F1), F is N\*F1.

#### Tail Recursive Factorial w/ Accumulator

Code

 $\label{eq:constraint} \begin{array}{l} \mbox{tail}_factorial(0,F,F).\\ \mbox{tail}_factorial(N,A,F):-\\ N > 0,\\ A1 \mbox{ is } N^*A,\\ N1 \mbox{ is } N -1,\\ \mbox{tail}_factorial(N1,A1,F). \end{array}$ 

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# AND and OR

- And
  - To implement X &&Y (use , in body of clause)
  - Example
    - Z :- X,Y.
- OR
  - To implement X || Y (use two clauses)
  - Example
    - Z :- X.
    - Z :- Y.

# **Goal Execution**

- When submitting a query, we ask Prolog to substitute variables as necessary to make it true
- Prolog performs goal execution to find a solution
  - Start with the goal
  - Try to unify the head of a rule with the current goal
  - The rule hypotheses become subgoals
    - > Substitutions from one subgoal constrain solutions to the next
  - If it reaches a dead end, it backtracks
    - > Tries a different rule
  - When it can backtrack no further, it reports false
- More advanced topics later cuts, negation, etc.

# Goal Execution (cont.)

- Consider the following:
  - "All men are mortal" mortal(X) :- man(X).
  - "Socrates is a man" man(socrates).
  - "Is Socrates mortal?" ?- mortal(socrates). true.
- How did Prolog infer this?

- 1. Sets mortal(socrates) as the initial goal
- Sees if it unifies with the head of any clause: mortal(socrates) = mortal(X).
- man(socrates) becomes the new goal (since X=socrates)
- 4. Recursively scans through all clauses, backtracking if needed ...

# **Clause Tree**

- Clause tree
  - Shows (recursive) evaluation of all clauses
  - Shows value (instance) of variable for each clause
  - Clause tree is true if all leaves are true
- ► Factorial example factorial(3,6)



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Tracing

- trace lets you step through a goal's execution
  - notrace turns it off



#### Goal Execution – Backtracking

- Clauses are tried in order
- If clause fails, try next clause, if available
- ► Example ?- fight(A,B).
   jedi(luke). A=luke,
   jedi(yoda). B=vader;
   sith(vader). A=luke,
   sith(maul). B=maul;
   fight(X,Y) :- jedi(X), sith(Y). A=yoda,
   B=vader;
   A=yoda,

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B=maul.

# Prolog (Search / Proof / Execution) Tree



#### Lists In Prolog

- ▶ [a, b, 1, 'hi', [X, 2] ]
- But really represented as compound terms
  - [] is an atom
  - [a, b, c] is represented as .(a, .(b, .(c, [])))
- Matching over lists

?- [X, 1, Z] = [a, \_, 17] X = a, Z = 17.

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#### List Deconstruction

Syntactically related to OcamI: [H|T] like h::t

```
?- [Head | Tail] = [a,b,c].
Head = a,
Tail = [b, c].
```

?-[1,2,3,4] = [\_, X |\_]. X = 2

- This is sufficient for defining complex predicates
- Let's define concat(L1, L2, C) ?- concat([a,b,c], [d,e,f], X).

X = [a,b,c,d,e,f].

#### **Example: Concatenating Lists**

- To program this, we define the "rules" of concatenation
  - If L1 is empty, then C = L2 concat( [], L2, L2 ).
  - Prepending a new element to L1 prepends it to C, so long as C is the concatenation of L1 with some L2

```
concat( [E | L1], L2, [E | C] ) :-
concat(L1, L2, C).
```

... and we're done

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# Why Is The Return Value An Argument?

Now we can ask what inputs lead to an output



#### More Syntax: Built-in Predicates

- Equality (a.k.a. unification) X = Y f(1,X,2) = f(Y,3,\_)
- fail and true
- "Consulting" (loading) programs ?- consult('file.pl') ?- ['file.pl']
- Output/Input ?- write('Hello world'), nl ?- read(X).
- (Dynamic) type checking
   ?- atom(elephant)
   ?- atom(Elephant)
- ▶ help

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#### The == Operator

- For identity comparisons
- ▶ X == Y
  - Returns true if and only if X and Y are identical
- Examples

?- 9 == 9.	?- 9 == 7+2.
true.	false.
?- X == 9.	?- X == Y.
False.	false.
?- X == X.	?- 7+2 == 7+2.
true.	true.

#### The =:= Operator

- For arithmetic operations
- "LHS =:= RHS"
  - Evaluate the LHS to value V1 (Error if not possible)
  - Evaluate the RHS to value V2 (Error if not possible)
  - Then match: V1 = V2
- Examples

?- 7+2 =:= 9. ?- 7+2 =:= 3+6. true.

?- X =:= 9.

?- X =:= 7+2

Error: =:=/2: Arguments are not sufficiently instantiated

# Example – Towers of Hanoi

- Problem
  - Move full stack of disks to another peg
  - Can only move top disk in stack
  - Only allowed to place disk on top of larger disk



# Example – Towers of Hanoi

- To move a stack of n disks from peg X to Y
  - Base case
    - If n = 1, transfer disk from X to Y
  - Recursive step
    - 1. Move top n-1 disks from X to 3<sup>rd</sup> peg
    - 2. Move bottom disk from X to Y
    - 3. Move top n-1 disks from 3<sup>rd</sup> peg to Y

Iterative algorithm would take much longer to describe!

# Towers of Hanoi

#### Code

#### move(1,X,Y,\_) :-

write('Move top disk from '), write(X),
write(' to '), write(Y), nl.
move(N,X,Y,Z) :-

N>1.

IN- I,

M is N-1,

move(M,X,Z,Y),

move(1,X,Y,\_), move(M,Z,Y,X).

# Prolog Terminology

- A query, goal, or term where variables do not occur is called ground; else it's nonground
  - foo(a,b) is ground; bar(X) is nonground
- A substitution θ is a partial map from variables to terms where domain(θ) ∩ range(θ) = ∅
  - Variables are terms, so a substitution can map variables to other variables, but not to themselves
- A is an instance of B if there is a substitution such that A = Bθ ← The substitution θ applied to B
- C is a common instance of A and B if it is an instance of A and an instance of B



# ! : a.k.a. "cut"

- When a ! is reached, it succeeds and commits Prolog to all the choices made since the parent goal was unified with the head of the clause the cut occurs in
  - Suppose we have clause C which is A :- B1,...,Bk,!,...Bn.
  - If the current goal unifies with A, and B1,...,Bk further succeed, the program is committed to the choice of C for the goal.
    - > If any Bi for i > k fail, backtracking only goes as far as the cut.
    - > If the cut is reached when backtracking, the goal fails

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#### Cut

Limits backtracking to predicates to right of cut

Example	?- fight2(A,B).
jedi(luke).	A=luke,
jedi(yoda).	B=vader;
sith(vader).	A=luke,
sith(maul).	B=maul.
fight2(X,Y) :- jedi(X), !, sith(Y).	?- fight3(A,B).
fight3(X,Y) :- jedi(X), sith(Y), !.	A=luke,
	B=vader.

# Prolog Search Tree Limited By Cut



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# What Exactly Is Cut Doing?



#### Why Use Cuts?

- Save time and space, or eliminate redundancy
  - · Prune useless branches in the search tree
  - · If sure these branches will not lead to solutions
  - These are green cuts
- Guide to the search to a different solution
  - Change the meaning of the program
  - Intentionally returning only subset of possible solutions
  - These are red cuts

**Negation As Failure** 

- Cut may be used implement negation (not)
- Example

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```
not(X) :- call(X), !, fail.
not(X).
```

- If X succeeds, then the cut is reached, committing it; fail causes the whole thing to fail
- If X fails, then the second rule is reached, and the overall goal succeeds.
  - FYI, X here refers to an arbitrary goal
  - · Effect of not depends crucially on rule order

#### Not

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Not is tricky to use ?- not(sith(luke)). Does not mean "not true" true. • Just means "not provable ?- not(sith(vader)). at this time" false. Example ?- not(jedi(leia)). jedi(luke). true. jedi(vader). ?- not(sith(leia)). sith(vader). true. Cannot prove either jedi(leia) or sith(leia) are true, so not() returns true

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# Not (cont.)



#### Not – Search Tree



# Not (cont.)

Ordering of clause	s matters	?- true_jedi1(luke).	
Example		true.	
jedi(luke).		?- true_jedi1(X).	
jedi(vader).		X=luke.	
sith(vader).		?- true_jedi2(luke).	
true_jedi1(X) :-		true.	
jedi(X), not(sith(X	)).	?- true_jedi2(X).	
true_jedi2(X) :-		false.	
not(sith(X)), jedi(ک	<).	1	
	X=vader causes not(sith(X)) to fail;		
Will not backtrack to X=luke, since		rack to X=luke, since	
CMSC 330	sith(luke) is n	ot a fact 51	



#### Not and \=

#### Built-in operators Example ?- help2(X,Y). X=luke, • \+ is not jedi(luke). Y=yoda; • X \= Y is same as not(X=Y) jedi(yoda). X=yoda, • X \== Y is same as not(X==Y) help2(X,Y) := jedi(X), jedi(Y), X = Y.Y=luke. help3(X,Y) := jedi(X), X = Y, jedi(Y).So be careful using \= ?- help3(X,luke). help4(X,Y) := X = Y, jedi(X), jedi(Y).X=yoda. • Ordering of clauses matters ?- help3(X,Y). • Try to ensure operands of \= are instantiated false. After selecting X, / can choose Y=X and fail X = Y. CMSC 330 53 CMSC 330 54

Help3 – Search Tree help3(X,Y) :not(X=Y) :- X=Y, !, fail. ?- help3(X,Y). jedi(X), not(X=Y). X \= Y. jedi(luke). ?- jedi(X), X \= Y, jedi(Y). jedi(Y). jedi(yoda). X=luke X=yoda ?- jedi(yoda), yoda \= Y, jedi(Y). ?- jedi(luke), luke \= Y, jedi(Y) Y=yoda Y=luke ?- yoda\=yoda ?- luke\=luke luke=luke.!.fail yoda=yoda,!,fail

#### Using \=

In fact, given X \= Y

Example Using \=

• will always fail if X or Y are not both instantiated

X \= a // fails for X=a a \= Y // fails for Y=a X \= Y // fails for X=Y

# Example Using \=

Example	?- help4(X,luke).
<pre>jedi(luke). jedi(yoda). help2(X,Y) :- jedi(X), jedi(Y), X \= Y. help3(X,Y) :- jedi(X), X \= Y, jedi(Y). help4(X,Y) :- X \= Y, jedi(X), jedi(Y).</pre>	false. ?- help4(yoda,luke). true.

#### **Built-in List Predicates**

- length(List,Length) ?- length([a, b, [1,2,3]], Length). Length = 3.
- member(Elem,List)

?- member(duey, [huey, duey, luey]).
true.
?- member(X, [huey, duey, luey]).

- X = huey; X = duey; X = luey.
- append(List1,List2,Result) ?- append([duey], [huey, duey, luey], X). X = [duey, huey, duey, luey].

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#### **Built-in Predicates**

sort(List,SortedList)

?- sort([2,1,3], R). R= [1,2,3].

findall(Elem,Predicate,ResultList)

?- findall(E,member(E,[huey, duey, luey]),R). R=[huey,duey,luey].

setof(Elem,Predicate,ResultSortedList)

?- setof(E,member(E,[huey, duey, luey]),R). R=[duey,huey,luey].

See documentation for more

http://www.swi-prolog.org/pldoc/man?section=builtin

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# **Prolog Summary**

- General purpose logic programming language
  - Associated with AI, computational linguistics
  - Also used for theorem proving, expert systems
- Declarative programming
  - Specify facts & relationships between facts (rules)
  - Run program as queries over these specifications
- Natural support for
  - Searching within set of constraints
  - Backtracking