

CMSC724: Access Methods; Indexes; GiST

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Outline

Access Methods

Some Examples

B+-Tree

Beyond B+-Trees

R-Tree and Variants

GiST: Generalized Search Trees

Access Methods

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R-Tree and
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GiST: Generalized
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Access Methods: Why ?

- ▶ Most queries have predicates in them
 - ▶ Accessing only the needed records key in performance
- ▶ How relations are stored ?
 - ▶ Heap files: **sequential** scans, very very fast
 - ▶ Index structures: **random** accesses to the needed data
 - ▶ Scan performance increasing much faster than seeks
 - ▶ **Must perform *much better* than Scan**
 - ▶ No point in building indexes on small relations
- ▶ Note the emphasis on “queries”
 - ▶ Utility depends more on query workload than data
- ▶ Why not use in-memory indexes ?
 - ▶ Data exchange with disks in units of “blocks”

Access Methods

- ▶ Support iterator interface:
 - ▶ open (possibly with selection condition)
 - ▶ get_next, close, insert, delete, update_field
- ▶ Performance goals:
 - ▶ Disk I/O (or time) for lookups, inserts, deletes
 - ▶ cold vs hot lookups
 - ▶ Compare to sequential (seek times improving much slower)

Access Methods

- ▶ At a high level:
 - ▶ *partition*: partition a dataset or domain into buckets
 - ▶ *label*: provide a label for each bucket
 - ▶ Sometimes hierarchically (trees), sometimes not (hashing)
- ▶ Partitioning is critical for good performance
 - ▶ In B+-Trees, we take the sorted order as a given since natural
 - ▶ For all other cases, unclear how to “pack”

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B+-Tree

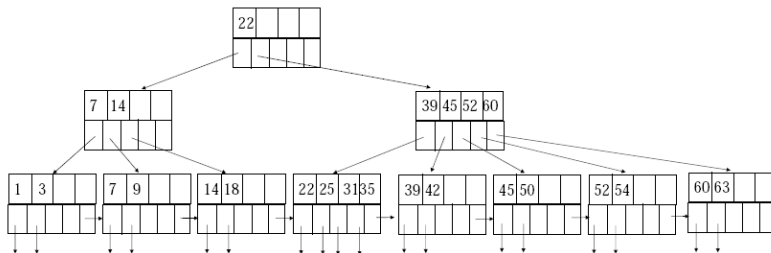
Beyond B+-Trees

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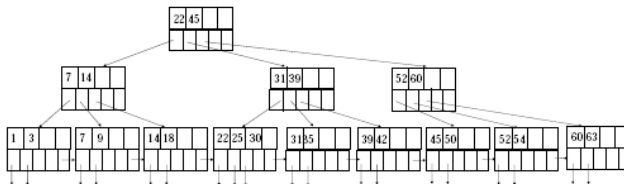
B+ Trees

- ▶ Balanced; Optimal for 1-d ($O(\log_B n)$ search/update) ($B = 100-500$)
- ▶ Utilization kept around 70% or so
- ▶ In practice, deletes do not result in merging of siblings

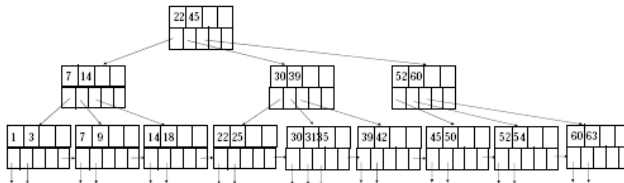


B+ Tree Inserts

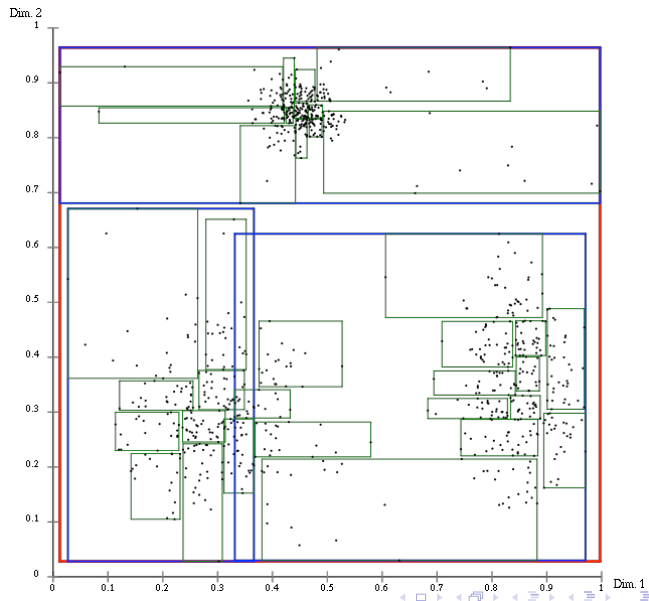
alternative 1



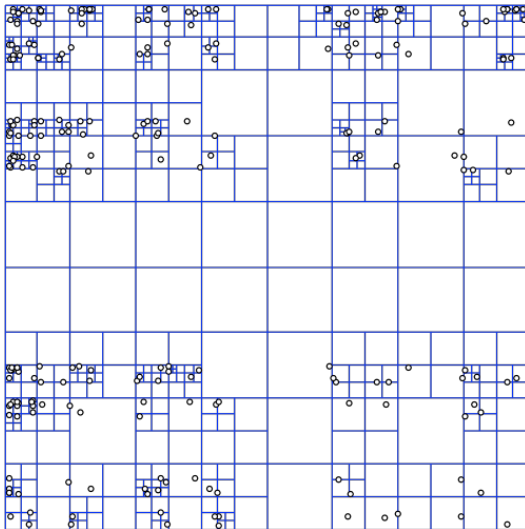
alternative 2



R-Tree (Points)



Quad Tree



Access Methods

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B+-Tree

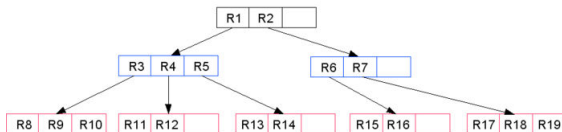
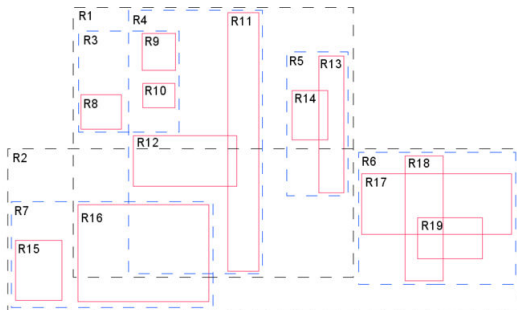
Beyond B+-Trees

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R-Tree (Rectangles)

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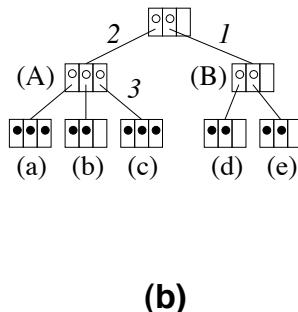
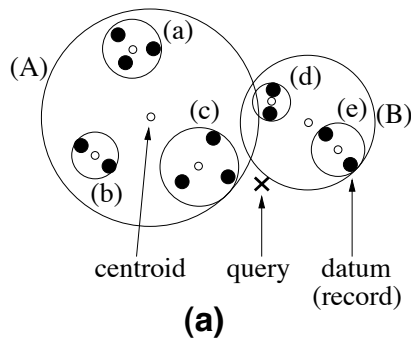


Figure 1. Similarity search using an SS-tree.
(a) Spatial coverage diagram.
(b) Tree structure diagram.

▶ Key Differentiating Factors

- ▶ Data (1-d vs 2-d vs n-d, points vs intervals vs spatial objects vs images etc...)
- ▶ Query types (equality, range, nearest-neighbor etc..)
- ▶ Balanced (B+-tree, R-Tree) vs Unbalanced (Quad-tree)
 - ▶ Balanced $\rightarrow$ predictable, uniform performance, but hard to guarantee
 - ▶ Typically requires rearranging of labels, splits etc..

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▶ Key Differentiating Factors

- ▶ Data- vs Space-partitioning
- ▶ Data-partitioning: the buckets are disjoint, but the labels may not be
 - ▶ May have to follow down the tree along multiple paths (e.g. R*-tree)
- ▶ Space-partitioning: the labels are disjoint, buckets may not be
 - ▶ e.g. Quad-trees, K-D-B trees
 - ▶ May have to duplicate pointers to data items in the leaves (e.g. R+-tree)
- ▶ B+-trees: disjoint buckets and disjoint labels

Access Methods

- ▶ Imagine:
 - ▶ The data is already stored on disk in some arbitrary order and you are not allowed to change it
 - ▶ How would you best build a hierarchical index structure on top for **equality** queries ?
 - ▶ Use BloomFilters ?
 - ▶ No option is going to work well if the data is really arbitrary and you can't find something to order by
 - ▶ But an interesting thought exercise
 - ▶ E.g. you might discover the third byte is different across blocks, but same within a block
 - ▶ Clustering of data is critical
 - ▶ Obvious for 1-d data, not so clear otherwise
- ▶ Not academic question: Imagine building an index over a distributed Grid/P2P data

Access Methods

- ▶ Implementation Issues:
 - ▶ Concurrency & recovery
 - ▶ **Very important issue**
 - ▶ Intertwined to a very complex degree
 - ▶ Can't build access methods in vacuum for just querying
 - ▶ Cost estimation
 - ▶ Query optimizer needs this information
 - ▶ Bulk loading
 - ▶ Important – have to be done very often

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B+-Tree

- ▶ Balanced, 50% utilization
 - ▶ In practice, allow getting lower when doing deletes
 - ▶ Inserts are more common, something will get inserted there soon
- ▶ $O(\log_d(n))$ search, update, delete costs
 - ▶ d = order of the tree (number of keys per page)
- ▶ Optimizations
 - ▶ Key compression
 - ▶ Bulk loading algorithms
 - ▶ Faster count queries
 - ▶ Maintain counts of tuples in the subtrees at the inner nodes

B+-Tree

- ▶ Concurrency: not 2PL - too slow
 - ▶ Release locks on upper-level nodes as soon as possible
 - ▶ Too many queries want to access them
 - ▶ Tricky when doing inserts
 - ▶ Higher-level pages may have to be split
 - ▶ One Solution: Do “preparatory” splits when inserting
 - ▶ We will talk about this in detail later
- ▶ B-Trees ?
 - ▶ The inner nodes store pointers to data
 - ▶ B+-Tree – all pointers to data are at the leaves
 - ▶ B+-Trees make many things significantly easier
 - ▶ E.g. Can do a “scan” on the leaves for range queries

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- ▶ B+-tree: Optimal for one-dimensional data (for range/equality queries)
- ▶ Linear hashing, extensible hashing: Only equality queries
- ▶ Multi-dimensional **point** data
 - ▶ Range queries:
 $(20 < \textit{age} < 30) \wedge (10,000 < \textit{salary})$
 - ▶ Space-filling curves: Impose a linear order on the multi-d data (limited applicability)
 - ▶ Grid-files, Quad-trees, K-D-B trees etc. . .
 - ▶ Nearest-Neighbor queries/similarity searches (very common)
 - ▶ Many indexing structures designed, no real consensus
 - ▶ Golden rule: Must beat sequential scans

Indexes

- ▶ Multi-dimensional **spatial** data (*regions, areas etc.*)
 - ▶ Queries: find all objects that contain this point, find objects that overlap this object
 - ▶ R-Tree and variants
- ▶ Intervals (e.g. time periods associated with events)
 - ▶ Queries: Find intervals containing this point, find overlapping intervals etc...
 - ▶ Several optimality results exists (see work by Lars Arge, Jeff Vitter et al.)
- ▶ XML ?
 - ▶ Some work, but generally considered very hard
- ▶ GiST: Generalized Search Tree

Indexes: A Timeline

Multidimensional Access Methods; Gaede, Gunther; ACM Surveys

1998

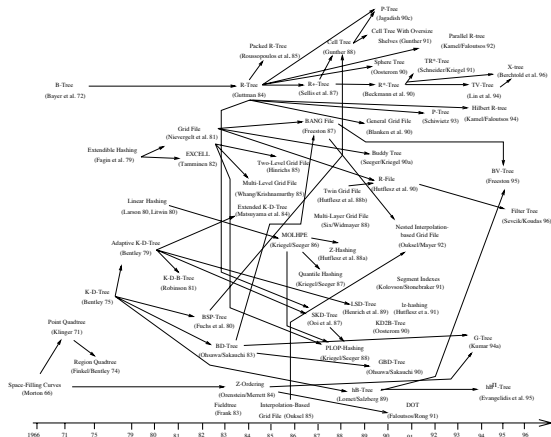


Figure: A Timeline of Indexes (From *Multidimensional Access Methods*; Gaede, Gunther; ACM Surveys 1998)

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Indexes

- ▶ Much work since then as well
- ▶ When reading these papers, ask yourself:
 - ▶ Does it beat sequential scan sufficiently ?
 - ▶ Is the data/workload realistic ?
 - ▶ Are there other natural workloads on which it may not do well ?
- ▶ Little rigor in this area
- ▶ Some theoretical work, but problems not easy
 - ▶ “Curse of Dimensionality”

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R-Tree

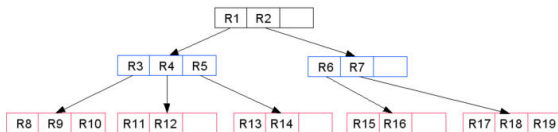
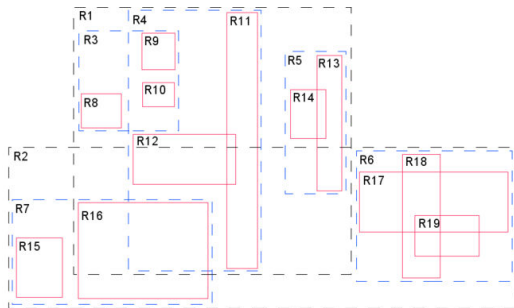


Figure: R-Tree

R-Tree

- ▶ Multi-dimensional, spatial data (points, rectangles)
- ▶ Queries: point in polygon, polygon in polygon, overlaps polygon, contains polygon
- ▶ *labels*: bounding rectangles
- ▶ Bulk loading ? Hard...
- ▶ Search: Follow all paths.
- ▶ Insert: Driven by minimizing *area enlargement*
- ▶ Split algorithms: exhaustive, quadratic, linear
- ▶ Delete: re-insert if too small (why ?)

R*-Tree

- ▶ R*-Tree: An improvement over R-Tree
- ▶ Analysis: four optimization metrics ?
 - ▶ Minimize area covered by a directory rectangle.
 - ▶ Minimize overlap
 - ▶ Minimize margin
 - ▶ Maximize storage *utilization*
- ▶ Conflict with each other
 - ▶ E.g., minimizing area covered conflicts with maximizing storage utilization.

R*-Tree

- ▶ Changes:
 - ▶ Insertion algorithm slightly different (minimizes “overlap” at leaf level)
 - ▶ Aggressive re-insertion (30% entries re-inserted at the same level)
 - ▶ Causes headaches with concurrency
- ▶ Lots of heuristics. . . backed by experimental analysis. . .
- ▶ Shown to outperform R-Trees in many experimental studies

R+-Tree

- ▶ R+-Tree
 - ▶ Space-partitioning version of R*-Tree
 - ▶ Forces non-overlapping keys
 - ▶ So same data item must be inserted into multiple leaf nodes
 - ▶ BUT don't need to follow all paths down to the leaves

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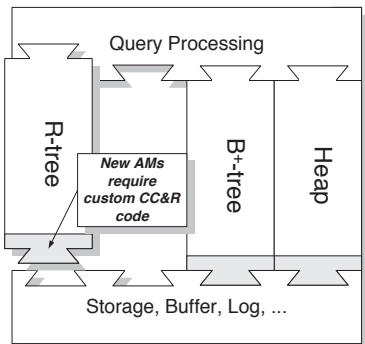
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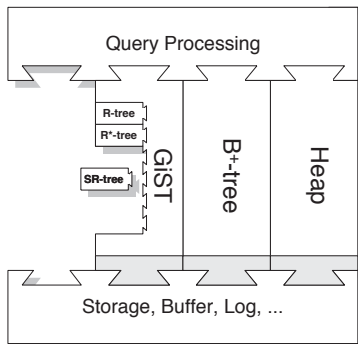
R-Tree and
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**GiST: Generalized
Search Trees**

- ▶ Motivation: Extensibility
 - ▶ New applications: GIS, multimedia (e.g. pictures), CAD, libraries, sequence datasets (Bioinformatics) etc...
 - ▶ Object-relational systems allow defining new data types
 - ▶ What about querying over them ?
- ▶ Two proposed solutions:
 - ▶ Option 1: Design new index structures
 - ▶ Option 2: **Try to use** an existing index structure
 - ▶ E.g. Can use space-filling curves and B+-Trees to support querying multi-dimensional data
 - ▶ Limited applicability (only equality/range queries)
 - ▶ What if the app needs new type of query ?
- ▶ Postgres paper had an initial discussion



(a) Standard ORDBMS



(b) ORDBMS with GiST

Figure 1: Access method interfaces – the database extender's perspective.

Figure: From: High-Performance Extensible Indexing;
Kornacker; VLDB 1999

- ▶ Generalized Search Tree
 - ▶ Allows extending data types as well as queries
 - ▶ **A single data structure** that can handle many different index structures
 - ▶ So a single code-base
 - ▶ How to use ?
 - ▶ Register six methods with the database system
 - ▶ Start inserting/deleting/querying
- ▶ Allows indexing arbitrary types of data
- ▶ Question: *Is it always a good idea to use a GiST ?*
 - ▶ No
 - ▶ Some data and query workloads not amenable to indexing (scan preferred)
 - ▶ Ideas later further developed in

Theory of Indexability

- ▶ Key insight:
 - ▶ An index structure partitions the input data hierarchically
 - ▶ GiST associates a “predicate” with each subtree, that is true for all data items in the subtree
 - ▶ Predicates on a single path from root to a leaf may not agree with each other, but must agree with the leaf
 - ▶ Nodes contain between 2 to M entries (except root)
 - ▶ Leaf nodes: (p, ptr)
 - ▶ ptr : pointer to actual record
 - ▶ p : predicate satisfied by the record
 - ▶ Non-leaf nodes: (p, ptr)
 - ▶ ptr : pointer to another node
 - ▶ p : predicate satisfied by **all records in the subtree** below

- ▶ Need to define 6 functions for a new search tree
 - ▶ Consistent(E, q): given a $E = (ptr, p)$, might q be satisfied by some tuple in the subtree below ptr
 - ▶ **search/querying** (search also done when inserting)
 - ▶ Union: Find new keys
 - ▶ **inserts** (when add a new E to a page)
 - ▶ Compress, Decompress: used for compressing the keys
 - ▶ Required to implement common optimizations
 - ▶ Penalty, PickSplit: Used for deciding where to **insert** a new object, and how to **split** a page if needed
- ▶ Very similar to R-Tree in many regards

GiST Algorithms

- ▶ Search: Query q
 - ▶ Find all pairs $E = (p, ptr)$ such that $consistent(E, q)$
 - ▶ Follow down all the pointers
 - ▶ Somewhat inefficient, can do better for linear orders
- ▶ Insert/Delete: Keep the tree balanced
 - ▶ Use the methods Penalty, PickSplit etc, to decide where to insert/delete, how to rearrange
- ▶ Discussion of how to support R*-Tree illustrates the difficulties simulating an index precisely
 - ▶ But as with all generalized/extensible approaches, you gain in simplicity what you sacrifice in performance

- ▶ Why an index might perform poorly ?
 - ▶ **Predicates at inner nodes not effective → traverse down unnecessarily**
 - ▶ Reason 1: Too much overlap between the data items themselves (e.g. spatial data)
 - ▶ Reason 2: Key compression not good, ie., the predicates can't approximate the subtree well (e.g. homework question)
 - ▶ Predicates too large in size in number of bytes
 - ▶ If predicates are allowed to be large, then search will be more efficient (fewer paths travelled)
 - ▶ BUT **large predicates → tree height increases**
 - ▶ Trade-off between key compression and search effectiveness

GiST: Analysis;

- ▶ Why an index might perform poorly ?
 - ▶ Poor storage utilization (too much wasted space)
 - ▶ Trade-off between this and above factors
 - ▶ Better storage utilization increases key overlap
 - ▶ Since we may have to force items together that shouldn't be
 - ▶ BUT **poor storage utilization → tree height increases**
- ▶ Complex trade-offs that can only be answered given a dataset and a query workload

GiST: Using Bloom Filters as Predicates

- ▶ The predicates are Bloom filters of the items in the subtree (as in homework)
 - ▶ Only supports equality queries
- ▶ $\text{Consistent}(E, q)$: Check if $q \in$ the Bloom filter
- ▶ Union: Bit-wise union etc...
- ▶ Why bad ?
 - ▶ If the Bloom Filter size is small (say 10 bits):
 - ▶ Too much key overlap
 - ▶ All bits in the higher level nodes likely to be set to 1
 - ▶ Many predicates will satisfy $\text{Consistent}(E, q)$
 - ▶ If the Bloom Filter size large (say 1000 bits):
 - ▶ Number of keys per page too low
 - ▶ The height of the tree will be large
- ▶ Not sure if anybody has formally analyzed this

GiST: Other issues

- ▶ Much later work at [Berkeley: GiST Project Website](#)
 - ▶ Indexability theory
 - ▶ Formalisms for analysis: different types of inefficiencies
- ▶ AmDB: A visual debugger and profiler
- ▶ Concurrency, recovery etc: Not addressed in this paper
 - ▶ See [High-Performance Extensible Indexing](#)

GiST: How extensible is it ?

- ▶ Generalizes many ideas, but some limitations
 - ▶ Recall the discussion of R*-Trees in the paper
- ▶ From: [Generalizing “Search”...; P. Aoki; ICDE 98](#)
- ▶ SS-Tree: [Similarity search tree](#)
 - ▶ For nearest-neighbor queries
 - ▶ Records organized in hierarchical clusters
 - ▶ For each cluster: *store centroid, bounding sphere radius*
 - ▶ Search: Traverse down the tree looking for the sphere closest to the query point
- ▶ Several Issues: e.g. Search is not depth-first
- ▶ Need a few modifications (see the paper above)