

1. Consider a sorting algorithm that is exactly like Merge Sort except it splits the list into thirds rather than halves.
 - (a) Write the (recursive) pseudo code for this algorithm. This should work for general size n .
 - (b) How would you merge the three sorted lists together?
 - (c) How many comparisons does it take to merge the three sorted lists together (where n is the total number of elements). Assume n is a multiple of three.
 - (d) Write a recurrence for the exact number of comparisons the entire algorithm uses. Assume n is a power of three.
 - (e) Solve the recurrence using the tree method, as done in class.
 - (f) How does the number of comparisons compare to standard Merge Sort?

2. Design a parallel algorithm analogous to Merge Sort. To keep this simple, you must do each merge sequentially. Obtain the parallelism by doing many merges simultaneously. You may use at most n processors. There are clever ways of doing this. Avoid them. If you want, there is the challenge problem below. In summary design the straightforward algorithm.
 - (a) Give the pseudo code. You may just write something like “do the following in parallel” and list what they are.
 - (b) Analyze the number of comparison steps exactly as possible. Note each comparison step may be doing many comparisons. Assume n is a power of 2. Show your work.
 - (c) CHALLENGE PROBLEM (not part of your grade). Design a more clever algorithm, with the same restriction that you must do each merge sequentially. Analyze the number of comparison steps exactly as possible.