Project 6
Due 11:59:59pm Tue, May 10, 2016

Updates
• None yet.

Introduction
In this project, you will add a static type checking system to the Rube programming language. Recall the formal syntax for Rube programs, shown in Figure ?? . In this project, we will extend this grammar to include static types, and then build a type checker for the resulting language.

To keep everything simpler, this project does not build directly on your project 5 code. But, it does use the same lexer and parser, and it should be easy for you to see how you might incorporate type checking into your compiler.

Project Structure
The project skeleton code is divided up into the following files:

- Makefile
- lexer.mll Rube lexer
- parser.mly Rube parser
- ast.mli Abstract syntax tree type
- rubet.ml The main type checker logic
- main.ml Parse the specified input file and call type checker
- r1.ru Hello world example

You will only change rubet.ml, lexer.mll, and parser.mly, and write part5.txt; you should not edit any of the other files. The file main.ml includes code to run the parser and then dispatch to the type checker. Right now, the “type checker” implementation just unparses the input file to standard output, e.g., after running make you can run:

```
$ ./main.byte r1.ru
"Hello, world!".print()
yes
```

to parse r1.ru and print the parsed result to standard out. You’ll change this code so that the parsed input is no longer printed to standard output. The yes indicates that this program type checks. In fact, the current implementation will always print yes, until you implement your type checker.

Part 1: Adding Type Annotations to Rube
Next, we are going to add type annotations to Rube. Figure ?? shows the necessary changes to the source language. In the revised language, classes begin with field definitions, which include types, followed by method definitions, which include type annotations on arguments and the method return (this type is to the left of the method name). We also introduce a new expression \((E : T)\) that performs a dynamic type cast to check at run time that \(E\) has type \(T\).
\[
P ::= \quad \text{Rube program}
\]
\[
C ::= \text{class } \text{id} < \text{id} \text{ begin } M^* \text{ end} \quad \text{Class definition}
\]
\[
M ::= \text{def } \text{id} (\text{id}, \ldots, \text{id}) \text{ begin } E \text{ end} \quad \text{Method definition}
\]
\[
E ::= \text{n} \quad \text{Integers}
\]
\[
| \quad \text{nil} \quad \text{Nil}
\]
\[
| \quad "\text{str}" \quad \text{String}
\]
\[
| \quad \text{self} \quad \text{Self}
\]
\[
| \quad \text{id} \quad \text{Local variable}
\]
\[
| \quad @\text{id} \quad \text{Field}
\]
\[
| \quad \text{if } E \text{ then } E \text{ else } E \text{ end} \quad \text{Conditional}
\]
\[
| \quad \text{while } E \text{ do } E \text{ end} \quad \text{While loop}
\]
\[
| \quad E; E \quad \text{Sequencing}
\]
\[
| \quad \text{id} = E \quad \text{Local variable write}
\]
\[
| \quad @\text{id} = E \quad \text{Field write}
\]
\[
| \quad \text{new } \text{id} \quad \text{Object creation}
\]
\[
| \quad E.i(\text{id}, \ldots, E) \quad \text{Method invocation}
\]

Figure 1: Rube syntax (without types)

\[
C ::= \text{class } \text{id} < \text{id} \text{ begin } F^* M^* \text{ end} \quad \text{Class definition}
\]
\[
F ::= @\text{id} : T \quad \text{Field type}
\]
\[
M ::= \text{def } T \text{id} (\text{id} : T, \ldots, \text{id} : T) L^* \text{ begin } E \text{ end} \quad \text{Method definition}
\]
\[
E ::= \ldots | (E : T) \quad \text{Type cast}
\]
\[
L ::= \text{id} : T \quad \text{Local variable type}
\]
\[
T ::= \text{id} \quad \text{Types}
\]
\[
MT ::= (T \times \cdots \times T) \to T \quad \text{Method type}
\]

Figure 2: Changes to Rube to add static types

Types \(T\) are simply class names. Our system will include distinguished classes \(\text{Bot}\), the class of \(\text{nil}\) (which can masquerade as an instance of any class) and \(\text{Object}\), the root of the class hierarchy. In other settings we might write \(\bot\) ("bottom") rather than \(\text{Bot}\) and \(\top\) ("top") rather than \(\text{Object}\).

Finally, we give a definition of \textit{method types} \(MT\) of the form \((T_1 \times \cdots \times T_n) \to T\), which is a method such that its \(i\)th argument has type \(T_i\) and it returns type \(T\). Method types are not allowed to appear in the surface syntax, so you don’t need to parse them; however, they are handy to have during type checking.

\textbf{Abstract syntax trees} Figure ?? shows the OCaml abstract syntax tree data types for programs with type annotations. It is quite similar to the grammar for the untyped variant of the language; we’ll highlight the differences next. \textbf{Important:} Don’t modify these constructors or types. Otherwise our grading scripts won’t work.

\(\text{EInvoke}(e, s, el)\) corresponds to calling method \(s\) of object \(e\) with the arguments given in \(el\). (The arguments are in the same order in the list as in the program text, and may be empty.) The argument list is a sequence of pairs containing an optional string and the expression passed as an argument. The string is ignored for now. Thus, you may safely assume it is \texttt{None} for parts 1–4. Finally, \(\text{ECast}(e, t)\) represents a type cast.

A type \(\texttt{typ}\) is just a string, wrapped in the constructor \(\texttt{TClass}\), e.g., \(\texttt{TClass "Bot"}\) is the type of \(\text{nil}\). We added a constructor here to make it slightly harder to mix up strings corresponding to types with other strings. We also define \(\texttt{mtyp}\) for method types; we’ll use this as the return type of a key function below.

A method \(\texttt{meth}\) is a record containing the method name, return type, arguments (with types), local variable definitions, and method body. Method arguments also have an optional expression and an optional
string, denoting a default value and a name. You can assume these last two fields are always None. A class cls is a record containing the class name, superclass, fields, and methods. Finally, a program prog is a record containing the list of classes and the top-level expression.

What to Do For this part of the project, you must extend the Rube lexer and parser to support the grammar extensions just described: fields with types; method type annotations; locals with types; and type casts. (As mentioned earlier, method types (with arrows) will never appear in the surface syntax.) Right now the parser does produce ASTs of the form just described, but it puts type Bot wherever a type is needed, and uses empty lists for the locals and fields.

Part 2: Typing Utilities

To implement type checking for Rube with type annotations, we’ll need the following utility functions. You should write these functions in rubet.ml. Important: We will test your code by calling these functions directly, so it’s important you put them in the right file.

In the following functions, you should assume the existence of five built-in classes: Object, Integer, String, Map, and Bot, where Object is the root of the inheritance hierarchy, Integer, String, and Map extend Object. The class Bot is the bottom type, and it also has all the methods of Object. Figure ?? gives type signatures for built-in methods of these classes; you should assume these built-in methods exist.

1. Write a function defined_class p c : prog -> string -> bool that returns true if and only if class c is defined in program p. This function should return true if asked whether Object, Integer, String, Map, or Bot are defined.

2. Write a function lca_class p c1 c2 : prog -> string -> string -> string that, given classes c1 and c2, returns the lowest common ancestor of classes c1 and c2 in the inheritance hierarchy. For example, lca_class p "String" "Integer" would return "Object". Note that if A is a subclass of B, then lca_class p "A" "B" would return "B". Also, lca_class p "A" "A" should return "A". Finally, for purposes of this function, Bot should be a descendent of every other class, e.g., lca_class p "String" "Bot" would return "String".
3. Write a function `castable p t1 t2 : prog -> typ -> typ -> bool` that returns true if and only if a cast from type `t1` to type `t2` could potentially succeed at runtime, meaning that either `t1` is an ancestor of `t2` in the inheritance hierarchy (downcast), `t2` is an ancestor of `t1` (upcast), or `t1 = t2`. For example, `castable p (TClass "Object") (TClass "String")` would return true, but `castable p (TClass "String") (TClass "Integer")` would return false. Because of the odd nature of `nil`, `castable p (TClass x) (TClass "Bot")` should always succeed, for any `x`.

4. Write a function `no_builtin_redef : prog -> bool` that returns true if the program does not try to define classes `Object`, `String`, `Integer`, `Map`, or `Bot`. (Note that we have not specified what to do for programs that redefine user classes; our test cases will never do so, and so it’s up to you how to handle such cases.)

5. Write a function `lookup_meth p c m : prog -> string -> string -> mtyp` that returns the type (an `mtyp`) of method `m` in class `c` or, if that method is not defined, it should return the type from `c`’s superclass (and so on, recursively up the class hierarchy). This function should `raise Not_found` if no such method exists in `c` or in any superclass. **Note:** Don’t forget about the types of built-in and inherited methods in `Object`, `String`, `Integer`, `Map`, and `Bot`; they should be returned by this function. (Note that we have not specified any particular behavior if the same method is defined twice within one class; our test cases will never do so.)

6. Write a function `lookup_field p c f : prog -> string -> string -> typ` that returns the type of field `f` in class `c`. As with `lookup_meth`, it should recursively explore superclasses to find field definitions if necessary. This function should `raise Not_found` if `f` is not defined in `c` or in any of its superclasses. (Note that we have not specified any particular behavior if the same field is defined twice within one class; our test cases will never do so.)

### Part 3: Subtyping

Since our language includes subclassing, we will need to define a subtyping relationship as part of type checking. Figure 4 shows the subtyping rules for this language. In words, the rules are as follows:

- **BOT** states that the bottom type `Bot` is a subtype of any other type.
- **OBJ** states that any type is a subtype of `Object`.

![Figure 4: Built-in objects and methods](image-url)
• Class says that \(id_1\) is a subtype of \(id_2\) if \(id_1\) is a subclass of \(id_2\) in the program text.

• Trans says that subtyping of classes is transitive, and Refl says that subtyping is reflexive.

For convenience, we also define method subtyping in this figure. Meth says that for one method type to be a subtype of another, the arguments and return types must have the correct subtyping relationships. Refer to the class notes for an explanation.

Write a function `is_subtype p t1 t2 : prog -> typ -> typ -> bool` that returns true if and only if type \(t1\) is a subtype of \(t2\) according to this definition. Also write a function `is_msubtype p mt1 mt2 : prog -> mtyp -> mtyp -> bool` that returns true if and only if method type \(mt1\) is a subtype of method type \(mt2\) according to this definition.

Next, notice that the subtyping functions you wrote assume that subclasses are actually subtypes (rule Class); but a programmer could violate this assumption. For example, a programmer could create a class that overrides a method from a parent class and changes the type of that method in an unsafe way:

```latex
class A < Object begin def int m() 42 end end
class B < A begin def string m() "oops!" end end
```

Thus, the next step is to write a function `check_class p c : prog -> string -> bool` that checks whether the type annotations in \(c\) make that class a valid subtype of its superclass, according to the following rules:

• For every method \(m\) defined in \(c\), the type of \(m\) in \(c\) must be a subtype of \(m\) in its superclass, or \(m\) must not be defined (or inherited) by its superclass. (Use `lookup_meth` to help you here, so that you handle the case that the superclass inherits its type for \(m\), and to handle the built-in methods of Object, String, Integer, Map, and Bot.)

• For every field \(f\) defined in \(c\), there is no definition of \(f\) in any superclass (including transitively). In other words, shadowing fields in subclasses is not allowed in this language.

• Except for Object, class \(c\) may not be an ancestor of itself in the inheritance hierarchy.

• No class may extend Bot.

• Any type mentioned in a method or field signature must exist in the program, or be a built-in class.

Put `is_subtype`, `is_msubtype`, and `check_class` in `rubet.ml`.

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**Figure 5: Subtyping**

\[
\begin{align*}
\text{Bot} & \quad \text{Obj} & \quad \text{Class} \\
P \vdash \text{Bot} & \leq T & P \vdash T & \leq \text{Object} & (\text{class } id_1 & < id_2 \text{ begin } \ldots \text{ end}) & \in P \\
\text{Trans} & \quad \text{Refl} \\
P \vdash id_1 & \leq id_2 & P \vdash id_2 & \leq id_3 & P \vdash id_1 & \leq id_3 \\
& \quad P \vdash id_1 & \leq id_3 & & P \vdash id_1 & \leq id_3 \\
\text{Meth} \\
T_1' & \leq T_1 & \ldots & T_n' & \leq T_n & T & \leq T' \\
P \vdash (T_1 \times \ldots \times T_n) & \rightarrow T & \leq (T_1' \times \ldots \times T_n') & \rightarrow T'
\end{align*}
\]
Part 4: Type Checking

Finally, you must write a function tc_prog p : prog -> unit that returns successfully if and only if p type checks, and otherwise it raises an exception. Put this function in rubet.ml. Figure 6 gives the static type checking rules that you will translate into OCaml. Here A is a type environment, which as discussed in class is an associative list mapping local variables to their types. Most of the rules have the form P; A ⊢ E : T, meaning that in program P with environment A, expression E has type T. We’ll explain the other kinds of rules as we encounter them. We’ve labeled the rules so we can refer to them in the discussion:

- The rules INT, NIL, and STR all say that an integer, nil, or string have the obvious types.
- The local variables of a method include the parameters of the current method, locals defined at the top of the method, and self, which refers to the object whose method is being invoked. The rules SELF and ID say that self or the identifier id has whatever type is assigned to it in the environment A. If self or id is not bound in the environment, then this rule doesn’t apply—and hence your type checker would signal an error.
- The rule FIELD-R says that when a field is accessed, it has whatever type we get by looking it up in the program according to the lookup_field function you already wrote, finding the current class by looking up the type of self. Notice that unlike in untyped Rube, it is an error to refer to fields that have not been pre-defined. Also notice that like Ruby, only fields of self are accessible, and it is impossible to access a field of another object.
• The rule If says that to type a conditional, the three sub-expressions must all be well-typed, and the type of the whole if is the least-common ancestor of the types of the then and else branches.

• The rule While says that to type a while look, the two sub-expressions must be while-typed, and the type of the whole while is Bot.

• The rule Seq says that the type of $E_1; E_2$ is the type of $E_2$. Notice that this rule requires $E_1$ to be well typed, but it doesn’t matter what that type is.

• The rule Id-W says that a write to a local variable is well-typed if the type of the right-hand side of the assignment is a subtype of the variable type. Notice that unlike untyped Rube, it is an error to write to a variable that hasn’t been defined as either a parameter or local. Notice also that it is an error to write to the local variable self (which is implicitly syntactically distinct from the non-terminal id), and your implementation should signal an error in this case.

• Similarly, the rule Field-W says that a field write is well-typed if the type of the right-hand side is a subtype of the field type. Again, unlike untyped Rube, fields must be defined with types prior to writing to them.

• The rule New says that a new expression is well-typed if the class being constructed exists in the program according to the defined_class function you wrote earlier. Notice that, as in Java, the class can appear anywhere in the program—it could be listed before the current class definition or after.

• The rule Cast says that an expression can be type cast if it is well typed and its type is castable to the type of the cast (using the castable function you wrote earlier). The resulting type of the cast is the cast-to type.

• The rule Invoke says that for a method invocation to be well-typed, the receiver object expression and all arguments must be well-typed. Also, the types of the arguments must be subtypes of the method type we find by looking up id_m in whatever class corresponds to the receiver object, using the lookup_meth function you wrote earlier.

Notice that we don’t need to do anything else here, e.g., we don’t need to look inside the method body. That’s because we’ll separately check that the method actually has the type the lookup_meth function says it has. Neat!

• The rule Method says that for a method definition to be well typed inside of class id_c, it must be that if we typecheck the method body with locals assigned their types as given, parameters assigned their types as given, and self given type id_c, the body of the method has a type $T'$ that is a subtype of the declared method return type. Note the order here says that locals may shadow parameters, which may shadow self; however, we will not test whether you implement this shadowing.

• The rule Class says that for a class definition to be well typed, all its method definitions must be well-typed, and the class’s type annotations must be consistent with its superclasses, according to the check_class function you wrote above. There must also be no definitions of Object, Integer, String, or Bot.

• Finally, rule Program says that for a program to be well-typed, all of its classes must be well-typed, and its top-level expression must be well-typed under the empty environment. Notice this means the top-level expression cannot even refer to self!

When you’re writing tc_prog, you’ll probably want to write several other functions, including

val tc_expr : prog -> environment -> expr -> typ
that type checks an expression. It’s up to you to choose the type for `environment`, but something simple like `(string * typ) list` should work just fine. (Functions like `List.assoc` will be handy in working with this type.)

Your type checking functions can raise any exception to signal that a program is ill-typed. We’ve supplied the exception `Type_error` as a convenient exception to throw, but you’re not required to use it. In `main.ml`, there’s code that calls your `tc_prog` function and either prints `yes` or `no`, depending on whether `tc_prog` type checked the input or found a type error (i.e., raised an exception), respectively.

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