

CMSC 330: Organization of Programming Languages

Prolog Advanced Topic: Cut

Prolog Terminology

- ▶ A query, goal, or term where variables do not occur is called **ground**; else it's **nonground**
 - $\text{foo}(a,b)$ is ground; $\text{bar}(X)$ is nonground
- ▶ A **substitution** θ is a partial map from variables to terms where $\text{domain}(\theta) \cap \text{range}(\theta) = \emptyset$
 - Variables are terms, so a substitution can map variables to other variables, but circularly
- ▶ A is an **instance** of B if there is a substitution such that $A = B\theta$ ← The substitution θ applied to B
- ▶ C is a **common instance** of A and B if it is an instance of A and an instance of B

Quick Quiz

- ▶ Which of these are **ground** terms?

jedi(luke)

ground

jedi(yoda)

ground

sith(X)

not ground

- ▶ Which of these is an **instance** of **fight(A,B)**?

jedi(luke)

no (heads don't match)

fight(C,D)

yes, $\theta = \{ A \rightarrow C, B \rightarrow D \}$

fight(A,luke)

no ($A \rightarrow A$ not allowed)

fight(luke,yoda)

yes, $\theta = \{ A \rightarrow \text{luke}, B \rightarrow \text{yoda} \}$

Prolog's Algorithm Solve()

Starts as empty

Solve(goal **G**, program **P**, substitution θ) =

- ▶ Suppose **G** is A_1, \dots, A_n . Choose goal A_1 .
- ▶ For each clause $A :- B_1, B_2, \dots, B_k$ in **P**,
 - if θ_1 is the **mgu** of A and $A_1\theta$ then
 - ▶ If **Solve**($\{B_1, \dots, B_k, A_2, \dots, A_n\}, P, \theta \cdot \theta_1$) = some θ' then **return** θ'
 - ▶ (else it has failed, so we continue the for loop)
 - (else unification has failed, so try another rule)
- ▶ If loop exits return **fail**
- ▶ **Output**: θ s.t. $G\theta$ can be deduced from **P**, or fail

Chooses goals in order

Most
General
Unifier

Implements backtracking

Example

```
on_vacation(mary).
on_vacation(peter).
has_money(peter).
travel(X) :- on_vacation(X),
             has_money(X).
```

?= travel(Y).

- $\theta = X \rightarrow Y1, Y \rightarrow Y1$
- on_vacation(X), has_money(X)
 - $\theta = X \rightarrow Y1, Y \rightarrow Y1, Y1 \rightarrow \text{mary}$
- has_money(X)
 - $X = \text{mary}$ fails. Backtrack.
- on_vacation(X), has_money(X)
 - $\theta = X \rightarrow Y1, Y \rightarrow Y1, Y1 \rightarrow \text{peter}$
- has_money(X)
 - $X = \text{peter}$ succeeds with
 $\theta = X \rightarrow Y1, Y \rightarrow Y1, Y1 \rightarrow \text{peter}$
 - Output is thus $Y = \text{peter}$.

Some Additional Built-in Predicates

- ▶ “Consulting” (loading) programs
 ?- consult('file.pl') ?- ['file.pl'] ?- [file]
- ▶ Output/Input
 ?- write('Hello world'), nl ?- read(X).
- ▶ (Dynamic) type checking
 ?- atom(elephant) ?- atom(Elephant)
- ▶ help
- ▶ fail and true

! : a.k.a. “cut”

- ▶ When a ! is reached, it succeeds and commits Prolog to all the choices made since the parent goal was unified with the head of the clause the cut occurs in
 - Suppose we have clause C which is $A :- B_1, \dots, B_k, !, \dots, B_n$.
 - If the current goal unifies with A , and B_1, \dots, B_k further succeed, the program is committed to the choice of C for the goal.
 - If any B_i for $i > k$ fail, backtracking only goes as far as the cut.
 - If the cut is reached when backtracking, **the goal fails**

Cut

- ▶ Limits backtracking to predicates to **right** of cut

- ▶ Example

jedi(luke).

jedi(yoda).

sith(vader).

sith(maul).

fight2(X,Y) :- jedi(X), **!**, sith(Y).

fight3(X,Y) :- jedi(X), sith(Y), **!**.

?- fight2(A,B).

A=luke,

B=vader;

A=luke,

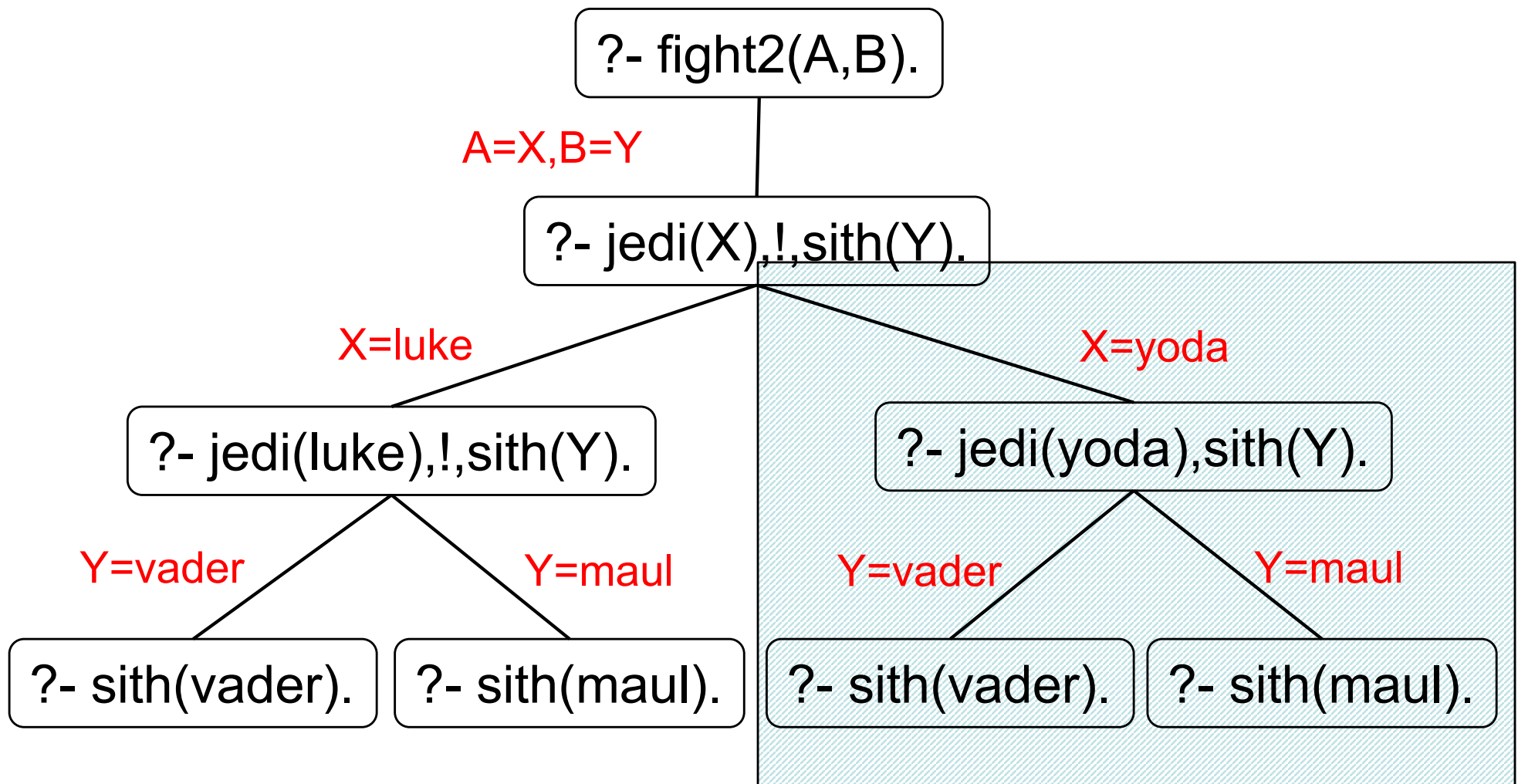
B=maul.

?- fight3(A,B).

A=luke,

B=vader.

Prolog Search Tree Limited By Cut



What Exactly Is Cut Doing?

Prunes all clauses below it

Prunes alternative solutions to its left

Does *not* affect the goals to its right

Note: Cut only affects **this** call to merge. Does not affect backtracking of functions calling merge, or later recursive call to merge past cut

```
merge([X|Xs], [Y|Ys], [X|Zs]) :-  
X < Y, !, merge(Xs, [Y|Ys], Zs).
```

```
merge([X|Xs], [Y|Ys], [X,Y|Zs]) :-  
X == Y, !, merge(Xs, Ys, Zs).
```

```
merge([X|Xs], [Y|Ys], [Y|Zs]) :-  
X > Y, !, merge([X|Xs], Ys, Zs).
```

```
merge(Xs, [], Xs) :- !.
```

```
merge([], Ys, Ys) :- !.
```

Quiz 1: What does this query return?

s(c).

s(m).

s(d).

solve(X) :- s(X), !.

solve(other_solution).

?- solve(X).

A. X = c; X=m; X = d; X = other_solution.

B. X = c

C. X = c; X=m; X = d;

D. true

Quiz 1: What does this query return?

s(c).

s(m).

s(d).

solve(X) :- s(X), !.

solve(other_solution).

?- solve(X).

A. X = c; X=m; X = d; X = other_solution.

B. X = c

C. X = c; X=m; X = d;

D. true

Quiz 2: What does this query return?

`check(_, []) :- !.`

`check(E, [H|T]) :- E > H, check(E, T).`

`?- check(10, [4, 3, 2]).`

- A. false.
- B. true; false.
- C. true.
- D. false; true.

Quiz 2: What does this query return?

`check(_, []) :- !.`

`check(E, [H|T]) :- E > H, check(E, T).`

`?- check(10, [4, 3, 2]).`

- A. false.
- B. true; false.
- C. true.
- D. false; true.

Why Use Cuts?

- ▶ Save time and space, or eliminate redundancy
 - Prune useless branches in the search tree
 - If sure these branches will not lead to solutions
 - These are **green cuts**

- ▶ Guide the search to a different solution
 - Change the meaning of the program
 - Intentionally returning only subset of possible solutions
 - These are **red cuts**

Quiz 3: Is this a green or red cut?

s(c).

s(m).

s(d).

solve(X) :- s(X), !.

solve(other_solution).

?- solve(X).

A. Green

B. Red

Quiz 3: Is this a green or red cut?

s(c).

s(m).

s(d).

solve(X) :- s(X), !.

solve(other_solution).

?- solve(X).

A. Green

B. Red

Quiz 4: Is this a green or red cut?

`check(_, []) :- !.`

`check(E, [H|T]) :- E > H, !, check(E, T).`

`?- check(10, [4, 3, 2]).`

A. Green

B. Red

Quiz 4: Is this a green or red cut?

`check(_, []) :- !.`

`check(E, [H|T]) :- E > H, !, check(E, T).`

`?- check(10, [4, 3, 2]).`

A. Green

B. Red

Quiz 5: Is this a green or red cut?

if_then_else(P,Q,_) :- P, !, Q.
if_then_else(_,_,R) :- R.

- A. Green
- B. Red

Quiz 5: Is this a green or red cut?

if_then_else(P,Q,_) :- P, !, Q.
if_then_else(_,_,R) :- R.

A. Green

B. Red

Negation As Failure

- ▶ (**Red**) cut used to implement negation (not)
- ▶ Example
 - `not(X) :- call(X), !, fail.`
 - `not(X).`
- ▶ If `X` succeeds, then the cut is reached, committing it; `fail` causes the whole thing to fail
- ▶ If `X` fails, then the second rule is reached, and the overall goal succeeds.
 - FYI, `X` here refers to an arbitrary goal
 - Effect of `not` depends crucially on rule order

Not

```
not(X) :- X, !, fail.  
not(X).
```

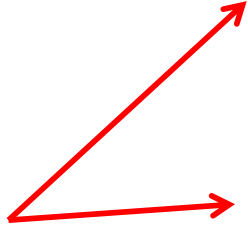
- ▶ Not is tricky to use
 - Does not mean “not true”
 - Just means “not provable”

- ▶ Example

```
jedi(luke).  
jedi(vader).  
sith(vader).
```

Cannot prove either
jedi(leia) or sith(leia)
are true, so not()
returns true

```
?- not(sith(luke)).  
true.  
?- not(sith(vader)).  
false.  
?- not(jedi(leia)).  
true.  
?- not(sith(leia)).  
true.
```



```
not(X) :- X, !, fail.  
not(X).
```

Not (cont.)

▶ Not is tricky to use

- Does not mean “not true”
- Just means “not provable”

```
?- not(sith(X)).
```

```
false.
```



▶ Example

```
jedi(luke).
```

```
jedi(vader).
```

```
sith(vader).
```

Huh? Why not return X=luke?

Because not(sith(X)) does not mean
“Can prove sith(X) is false for some X”

```
not(sith(X)) :- sith(X), !, fail.  
not(sith(X)).
```

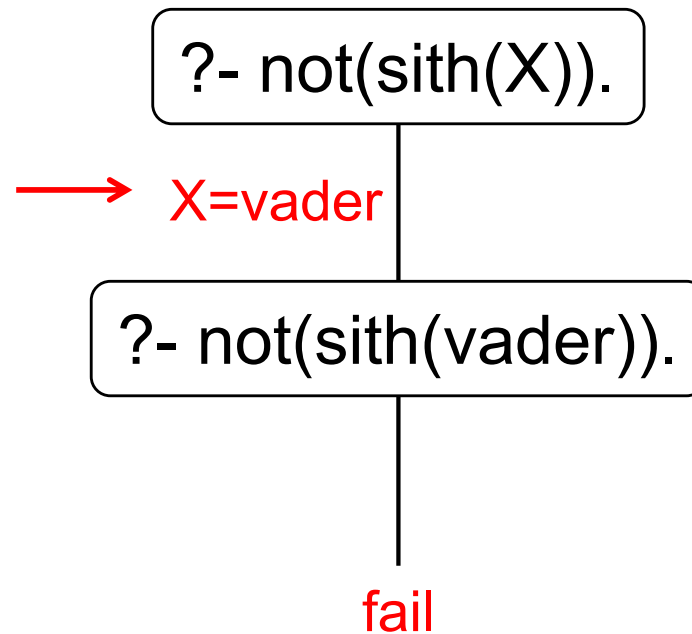
Instead, it means “Cannot prove sith(X)
is true for some X”. So X=vader causes
not(sith(X)) to fail and return false

Not – Search Tree

jedi(luke).
jedi(vader).
sith(vader).

not(sith(X)) :- sith(X), !, fail.
not(sith(X)).

Will search for
all X such that
sith(X) is true.



```
not(X) :- X, !, fail.  
not(X).
```

Not (cont.)

- ▶ Ordering of clauses matters

- ▶ Example

```
jedi(luke).
```

```
jedi(vader).
```

```
sith(vader).
```

```
true_jedi1(X) :-
```

```
    jedi(X), not(sith(X)).
```

```
true_jedi2(X) :-
```

```
    not(sith(X)), jedi(X).
```

```
?- true_jedi1(luke).
```

```
true.
```

```
?- true_jedi1(X).
```

```
X=luke.
```

```
?- true_jedi2(luke).
```

```
true.
```

```
?- true_jedi2(X).
```

```
false.
```



X=vader causes not(sith(X)) to fail;
Will not backtrack to X=luke, since
sith(luke) is not a fact

True_jedi2 – Search Tree

jedi(luke).
jedi(luke).
sith(vader).

not(sith(X)) :- sith(X), !, fail.
not(sith(X)).

?- true_jedi2(X).

?- not(sith(X)), jedi(X).

?- not(sith(vader)), jedi(vader).

Will search for
all X such that
sith(X) is true.

→ X=vader

not(sith(vader)) fails

fail

Not and \=

- ▶ Built-in operators
 - \+ is not
 - $X \neq Y$ is same as $\text{not}(X=Y)$
 - $X \neq\equiv Y$ is same as $\text{not}(X\equiv Y)$
- ▶ So be careful using \=
 - Ordering of clauses matters
 - Try to ensure operands of \= are instantiated

not(X) :- X, !, fail.
not(X).

Example Using \=

► Example

jedi(luke).

jedi(yoda).

help2(X,Y) :- jedi(X), jedi(Y), X \= Y.

help3(X,Y) :- jedi(X), X \= Y, jedi(Y).

help4(X,Y) :- X \= Y, jedi(X), jedi(Y).

?- help2(X,Y).

X=luke,

Y=yoda;

X=yoda,

Y=luke.


?- help3(X,luke).

X=yoda.

?- help3(X,Y).

false.

After selecting X,
can choose Y=X
and fail X \= Y.



Help3 – Search Tree

not(X=Y) :- X=Y, !, fail.
not(X=Y).

jedi(luke).
jedi(yoda).

?- help3(X,Y).

help3(X,Y) :-
jedi(X),
X \= Y,
jedi(Y).

?- jedi(X), X \= Y, jedi(Y).

X=luke

X=yoda

?- jedi(luke), luke \= Y, jedi(Y).

?- jedi(yoda), yoda \= Y, jedi(Y).

Y=luke

Y=yoda

?- luke\=luke

?- yoda\=yoda

luke=luke,! ,fail

yoda=yoda,! ,fail

Using \neq

- ▶ In fact, given $X \neq Y$
 - will always fail if X or Y are not both instantiated

$X \neq a$ // fails for $X=a$

$a \neq Y$ // fails for $Y=a$

$X \neq Y$ // fails for $X=Y$

Example Using \neq

- **Example** `jedi(luke).`
`jedi(yoda).`
`help2(X,Y) :- jedi(X), jedi(Y), X \neq Y.`
`help3(X,Y) :- jedi(X), X \neq Y, jedi(Y).`
`help4(X,Y) :- X \neq Y, jedi(X), jedi(Y).`

`?- help4(X,luke).`
`false.`
`?- help4(yoda,luke).`
`true.`

Quiz 6: What does this query return?

jedi(luke).

jedi(vader).

sith(vader).

true_jedi1(X) :- jedi(X), not(sith(X)).

?- true_jedi1(X).

- A. X = luke
- B. false
- C. true
- D. X = vader

Quiz 6: What does this query return?

jedi(luke).

jedi(vader).

sith(vader).

true_jedi1(X) :- jedi(X), not(sith(X)).

?- true_jedi1(X).

A. X = luke

B. false

C. true

D. X = vader

Quiz 7: What does this query return?

jedi(luke).

jedi(vader).

sith(vader).

true_jedi2(X) :- not(sith(X)), jedi(X).

?- true_jedi2(X)

- A. X = vader
- B. X = luke
- C. false
- D. true

Quiz 7: What does this query return?

jedi(luke).

jedi(vader).

sith(vader).

true_jedi2(X) :- not(sith(X)), jedi(X).

?- true_jedi2(X)

A. X = vader

B. X = luke

C. false

D. true

Prolog Summary

- ▶ General purpose logic programming language
 - Associated with AI, computational linguistics
 - Also used for theorem proving, expert systems
- ▶ Declarative programming
 - Specify facts & relationships between facts (rules)
 - Run program as queries over these specifications
- ▶ Natural support for
 - Searching within set of constraints
 - Backtracking