CMSC 330: Organization of Programming Languages

Functional Programming with Lists

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CMSC330 Spring 2018

Lists in OCaml

- The basic data structure in OCaml
 - Lists can be of arbitrary length
 - Implemented as a linked data structure
 - Lists must be homogeneous
 - All elements have the same type
- Operations
 - Construct lists
 - Destruct them via pattern matching

Constructing Lists

Syntax

- [] is the empty list (pronounced "nil")
- e1::e2 prepends element e1 to list e2
 - Operator :: is pronounced "cons" (both from LISP)

- e1 is the head, e2 is the tail

 [e1;e2;...;en] is syntactic sugar for e1::e2::...:en::[]

Examples

- 3::[] (* The list [3] *)
- 2::(3::[]) (* The list [2; 3] *)
- [1; 2; 3] (* The list 1::(2::(3::[])) *)

Constructing Lists

Evaluation

- [] is a value
- To evaluate e1::e2, evaluate e1 to a value v1, evaluate e2 to a (list) value v2, and return v1::v2

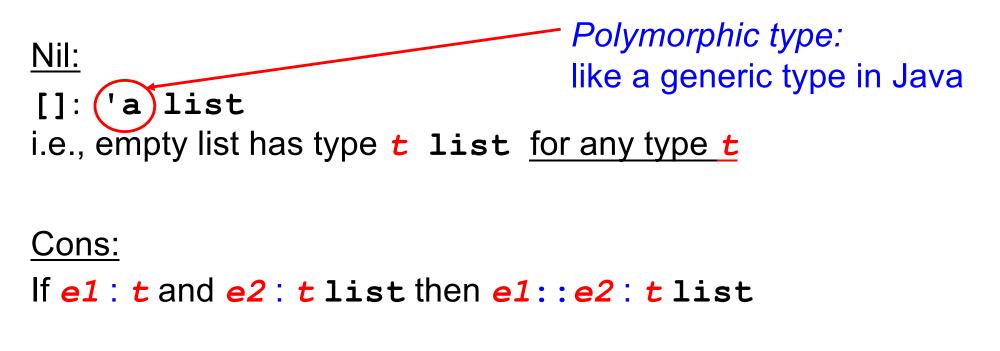
Consequence of the above rules:

 To evaluate [e1;...; en], evaluate e1 to a value v1, ..., evaluate en to a value vn, and return [v1;...; vn]

Examples

```
# let y = [1; 1+1; 1+1+1];
val y : int list = [1; 2; 3]
# let x = 4::y ;;
val x : int list = [4; 1; 2; 3]
# let z = 5::y ;;
val z : int list = [5; 1; 2; 3]
# let m = "hello"::"bob"::[];;
val z : string list = ["hello"; "bob"]
```

Typing List Construction



With parens for clarity: If e1: t and e2: (t list) then (e1::e2): (t list)

Examples

let x = [1; "world"] ;;

```
This expression has type string but an expression
was expected of type int
```

```
# let m = [[1];[2;3]];;
```

```
val y : int list list = [[1]; [2; 3]]
```

```
# let y = 0::[1;2;3];;
```

```
val y : int list = [0; 1; 2; 3]
```

let w = [1;2]::y ;;

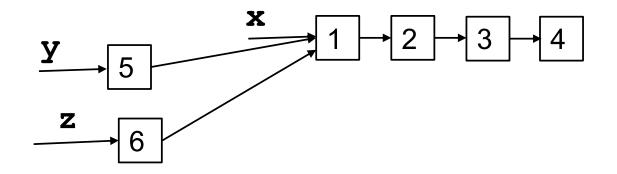
This expression has type int list but is here used with type int list list

- The left argument of :: is an element, the right is a list
- Can you construct a list y such that [1;2]::y makes sense?

Lists are Immutable

- No way to *mutate* (change) an element of a list
- Instead, build up new lists out of old, e.g., using ::

let x = [1;2;3;4]
let y = 5::x
let z = 6::x



What is the type of the following expression?

```
[1.0; 2.0; 3.0; 4.0]
```

- A. array
- B. list
- C. int list
- D. float list

What is the type of the following expression?

```
[1.0; 2.0; 3.0; 4.0]
```

- A. array
- B. list
- C. int list
- D. float list

What is the type of the following expression?

31::[3]

A. int

B. int list

C. int list list

What is the type of the following expression?

31::[3]

A. int

B. int list

C. int list list

What is the type of the following expression?

```
[[[]; []; [1.3;2.4]]]
```

A. int list

- B. float list list
- C. float list list list

What is the type of the following expression?

```
[[[]; []; [1.3;2.4]]]
```

A. int list

- B. float list list
- C. float list list list

What is the type of the following definition?

let f
$$x = x::(0::[])$$

- A. int -> int
- B. int list
- C. int list -> int list

D. int -> int list

What is the type of the following definition?

let f
$$x = x::(0::[])$$

- A. int -> int
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Pattern Matching

- To pull lists apart, use the **match** construct
- Syntax

match e with
| p1 -> e1
| ...
| pn -> en

- p1...pn are patterns made up of [], ::, constants, and pattern variables (which are normal OCaml variables)
- e1...en are branch expressions in which pattern variables in the corresponding pattern are bound

Pattern Matching Semantics

Evaluate e to a value v

•

. . .

- If p1 matches v, then evaluate e1 to v1 and return v1
- Else if *pn* matches *v*, then evaluate *en* to *vn* and return *vn*
- Else, no patterns match: raise Match_failure exception

(When evaluating branch expression *ei*, any pattern variables in *pi* are bound in *ei*, i.e., they are in scope)

match e with

p1 -> e1

-> en

Pattern Matching Example

- let is_empty l =
 match l with
 [] -> true
 | (h::t) -> false
- Example runs
 - is_empty [] (* evaluates to true *)
 - is_empty [1] (* evaluates to false *)
 - is_empty [1;2] (* evaluates to false *)

Pattern Matching Example (cont.)

let hd l =

match 1 with

- $(h::t) \rightarrow h$
- Example runs
 - hd [1;2;3] (* evaluates to 1 *)
 - hd [2;3] (* evaluates to 2 *)
 - hd [3] (* evaluates to 3 *)
 - hd [] (* Exception: Match_failure *)

To what does the following expression evaluate?

A. "zar"
B. "doz"
C. "kitteh"
D. []

To what does the following expression evaluate?

A. "zar"
B. "doz"
C. "kitteh"
D. []

"Deep" pattern matching

- You can nest patterns for more precise matches
 - a::b matches lists with at least one element
 - Matches [1;2;3], binding a to 1 and b to [2;3]
 - a::[] matches lists with exactly one element
 - Matches [1], binding a to 1
 - Could also write pattern a::[] as [a]
 - a::b::[] matches lists with exactly two elements
 - Matches [1;2], binding a to 1 and b to 2
 - Could also write pattern a::b::[] as [a;b]

- a::b::c::d matches lists with at least three elements

- Matches [1;2;3], binding a to 1, b to 2, c to 3, and d to []
- Cannot write pattern as [a;b;c]::d (why?)

Pattern Matching – Wildcards

- An underscore _ is a wildcard pattern
 - Matches anything
 - But doesn't add any bindings
 - Useful to hold a place but discard the value
 - i.e., when the variable does not appear in the branch expression
- In previous examples
 - Many values of h or t ignored
 - Can replace with wildcard ______

Pattern Matching – Wildcards (cont.)

- Code using ______
 - let is_empty l = match l with

[] -> true | (_::_) -> false

- -let hd l = match l with $(h::_)$ -> h
- -let tl l = match l with (_::t) -> t
- Outputs
 - is_empty[1](* evaluates to false *)
 - is_empty[](* evaluates to true *)
 - hd [1;2;3] (* evaluates to 1 *)
 - tl [1;2;3] (* evaluates to [2;3] *)
 - hd [1] (* evaluates to 1 *)
 - -tl [1] (* evaluates to [] *)

Pattern Matching – An Abbreviation

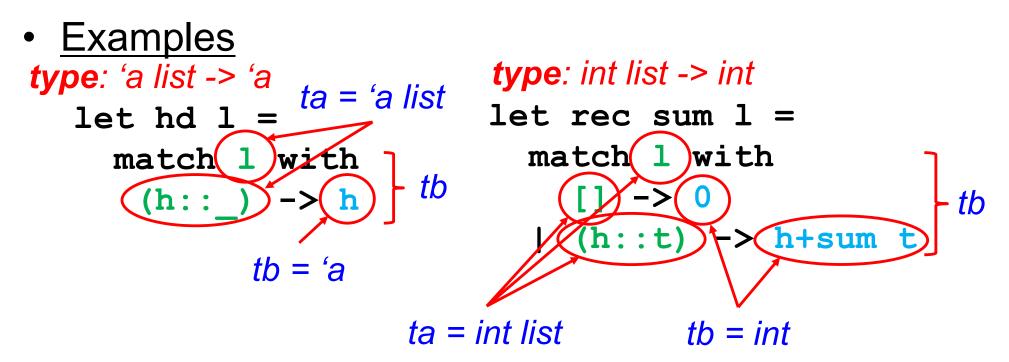
• let f p = e, where p is a pattern

- is shorthand for let f x = match x with $p \rightarrow e$

- Examples
 - -let hd $(h::_) = h$
 - let tl (_::t) = t
 - -let f $(x::y::_) = x + y$
 - -let g [x; y] = x + y
- Useful if there's only one acceptable input

Pattern Matching Typing

- match e with
 | p1 -> e1
 | ...
 | pn -> en
- If e and p1, ..., pn each have type ta
- and e1, ..., en each have type tb
- Then entire match expression has type tb



Polymorphic Types

- The sum function works only for int lists
- But the hd function works for any type of list
 - hd [1; 2; 3] (* returns 1 *)
 - hd ["a"; "b"; "c"] (* returns "a" *)
- OCaml gives such functions polymorphic types
 - hd : 'a list -> 'a
 - this says the function takes a list of *any* element type
 'a, and returns something of that same type
- These are basically generic types in Java
 - 'a list is like List<T>

Examples Of Polymorphic Types

```
• let fst x y = x
    # fst 1 "hello";;
    - : int = 1
    # fst [1; 2] 1;;
    - : int list = [1; 2]
    (* fst : 'a -> 'b -> 'a *)
```

Examples Of Polymorphic Types

```
• let hds (x::_) (y::_) = x::y::[]
# hds [1; 2] [3; 4];;
- : int list = [1; 3]
# hds ["kitty"] ["cat"];;
- : string list = ["kitty"; "cat"]
# hds ["kitty"] [3; 4] -- type error
(* hds: 'a list -> 'a list -> 'a list *)
```

```
• let eq x y = x = y (* let eq x y = (x = y) *)
# eq 1 2;;
- : bool = false
# eq "hello" "there";;
- : bool = false
# eq "hello" 1 -- type error
(* eq : 'a -> 'a -> bool *)
```

What is the type of the following function?

A. 'a -> 'b -> int

B. 'a -> 'a -> int

C. 'a -> 'a -> bool

D. int

What is the type of the following function?

C. 'a \rightarrow 'a \rightarrow bool

D. int

Pattern matching is **AWESOME**

- 1. You can't forget a case
 - Compiler issues inexhaustive pattern-match warning
- 2. You can't duplicate a case
 - Compiler issues unused match case warning
- 3. You can't get an exception
 - Can't do something like List.hd []
- 4. Pattern matching leads to elegant, concise, beautiful code

Lists and Recursion

- Lists have a recursive structure
 - And so most functions over lists will be recursive

```
let rec length l = match l with
    [] -> 0
    | (_::t) -> 1 + (length t)
```

- This is just like an inductive definition
 - The length of the empty list is zero
 - The length of a nonempty list is 1 plus the length of the tail
- Type of length?
 - `a list -> int

More Examples

- sum l (* sum of elts in l *)
 let rec sum l = match l with
 [] -> 0
 | (x::xs) -> x + (sum xs)

```
    last 1 (* last element of 1 *)
        let rec last 1 = match 1 with
            [x] -> x
            (x::xs) -> last xs
```

More Examples (cont.)

- (* return a list containing all the elements in the list l followed by all the elements in list m *)
- append 1 m

let rec append 1 m = match 1 with
 [] -> m
 | (x::xs) -> x::(append xs m)

- rev l (* reverse list; hint: use append *)
 let rec rev l = match l with
 [] -> []
 | (x::xs) -> append (rev xs) [x]
- rev takes O(n²) time. Can you do better?