Motion planning: Beyond Navmeshes

CMSC425.01 Spring 2019

Administrivia

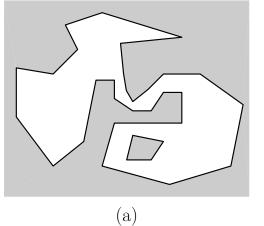
- Exam being graded ...
- Project 2b concepts out, write up soon (add animations to 2a)

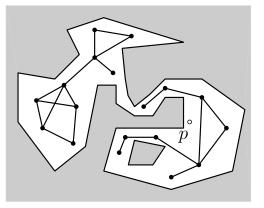
Today's questions

Big question: Making intelligent agents First question: Navigation

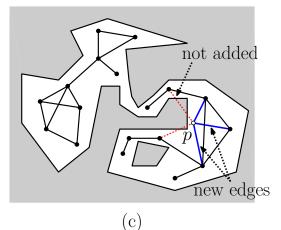
Finding paths in polygonal configuration space

- Version 1: Navmesh
- Others?
- Version 7: Randomized placement (sampling)





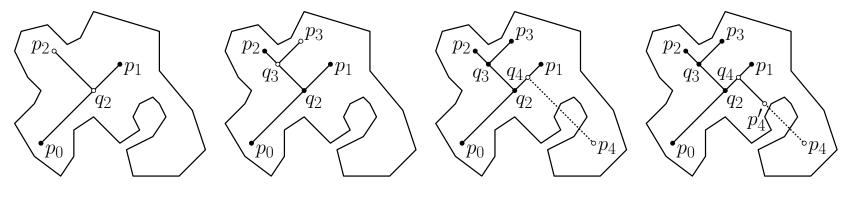
(b)



Finding paths in polygonal configuration space

(a)

- Version 1: Navmesh
- Others?
- Version 8: Rapidly-expanded Random Trees (RRTs)



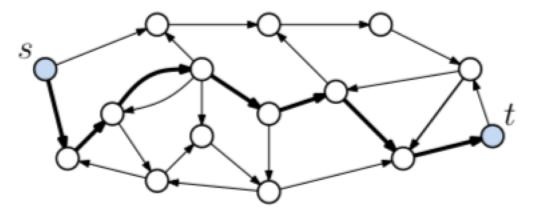
(c)

(d)

(b)

Computing shortest path

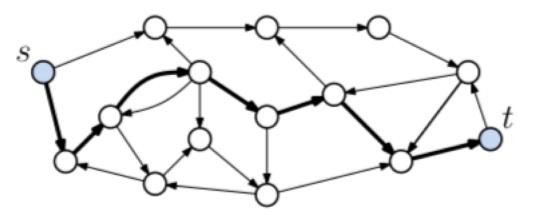
- Reduce navigation to path finding in graphs
 - Directed?
 - Weighted?



- G = (V, E)
 - Vertices $V = \{ u, v, ... \}$
 - Edges $E = \{ (u, v), ... \}$
 - Weight function $w(u, v) \rightarrow reals$

Computing shortest path

- Reduce navigation to path finding in graphs
 - Directed?
 - Weighted?
- G = (V, E)
 - Vertices $V = \{ u, v, ... \}$
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 - Weight function $w(u, v) \rightarrow reals$



- Path sequence of nodes
 - $P = \langle u_{0,} u_{1,} \dots, u_k \rangle$
- Path cost
 - $cost(P) = \sum_{i=0}^{k} w(u_{i,}u_{i+1})$
- Lowest cost path $\partial(s, t)$

First: what's the problem?

• Compute one shortest path?

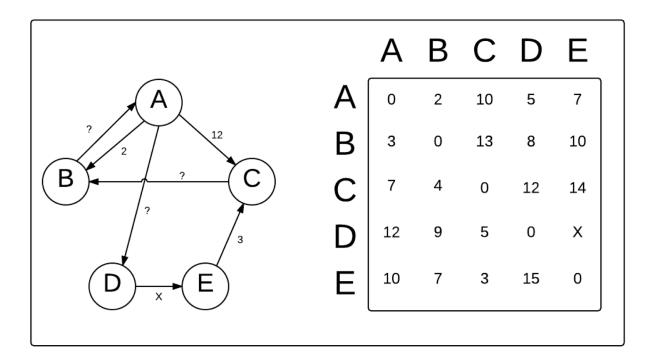
• Compute all shortest paths to store?

First: what's the problem?

• Compute path here to there?

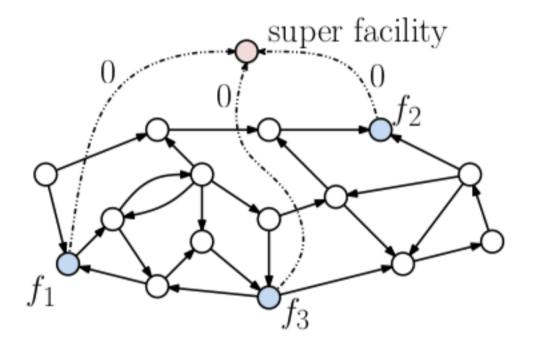
- Compute all shortest paths to store?
 - Floyd-Warshall

- Find fastest way to home base?
 - Reverse edges
 - Find shortest path to all from home
- Find closest facility (health, etc)?
 - Add Supernode connected to all facilities.



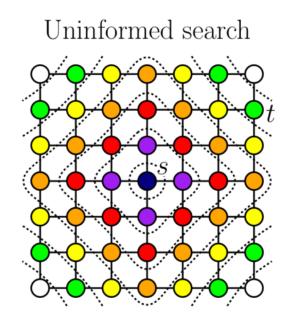
First: what's the problem?

- Find closest facility (health, etc)?
 - Add Supernode connected to all facilities.

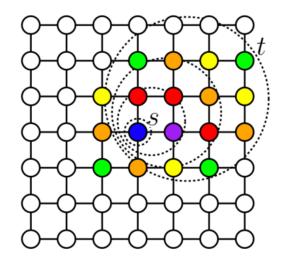


Uninformed vs. informed search

- Uninformed follow weights
 - Pick next node on distance to d[u]
- Informed add bias towards destination
- Heuristic
 - Pick next node on distance to goal h(u)

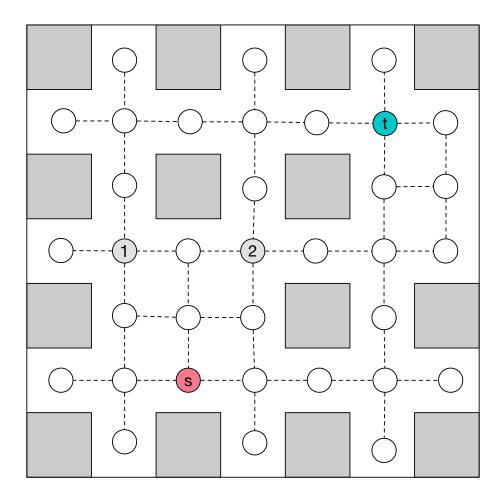


Informed search



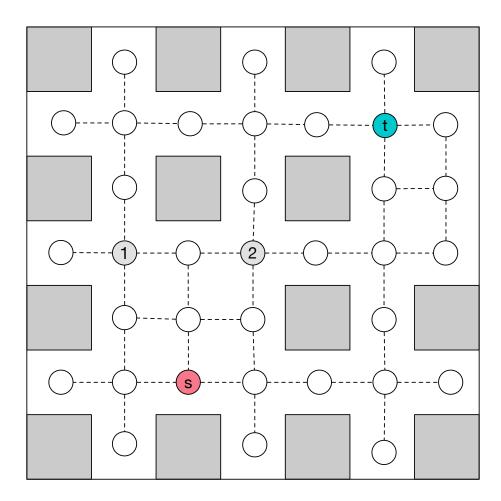
Informed search

- Distance functions
 - w(u,v) distance node u to v
 - d[u] distance traversed from start to node u
 - dist(u,t) distance from u to t
- w(s,1) = ____ dist(1,t) = ____
- w(s,2) = ____ dist(1,t) = ____



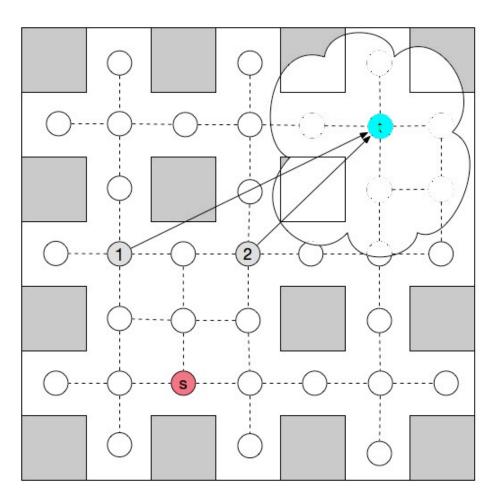
Informed search

- Distance functions
 - w(u,v) distance node u to v
 - d[u] distance traversed from start to node u
 - dist(u,t) distance from u to t
- w(s,1) = 3 dist(1,t) = 6
- w(s,2) = 3 dist(1,t) = 4
- dist(u,t) is a *heuristic*



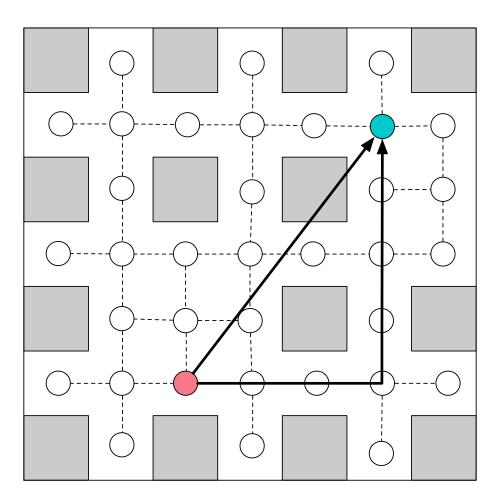
Less perfect information?

- Can't see rest of graph until you expand it
- Need guess on what's to come
- dist(u,t) as Euclidean distance
- Approximates actual cost



Footnote

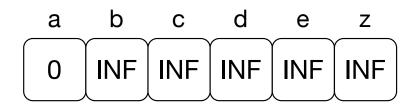
- Euclidean distance
 - distE(p1,p2) = sqrt((x1-x2)^2 + (y1-y2)^2)
- Manhattan distance
 - distM(p1,p2) = abs(x1-x2) + abs(y1-y2)

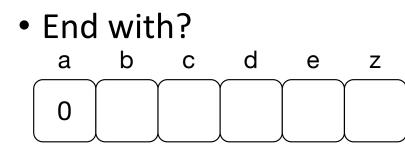


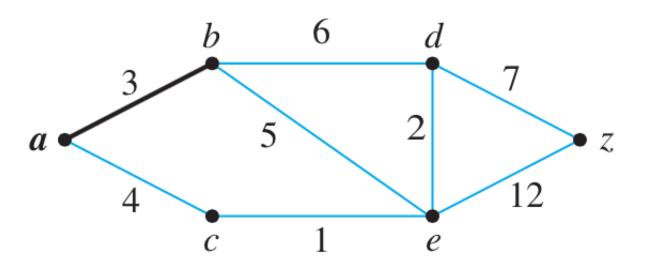
```
Dijkstra(G, s, t) {
foreach (node u) {
                                      // initialize
  d[u] = +infinity; mark u undiscovered
}
d[s] = 0; mark s discovered // distance to source is 0
repeat forever {
                                      // go until finding t
  let u be the discovered node that minimizes d[u]
  if (u == t) return d[t]
                         // arrived at the destination
  else {
    for (each unfinished node v adjacent to u) {
      d[v] = min(d[v], d[u] + w(u,v)) // update d[v]
      mark v discovered
    }
    mark u finished
                                      // we're done with u
```

Example

- w(u,v) as given
- Start with d array as

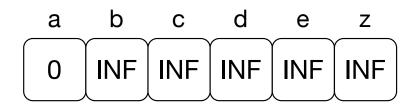






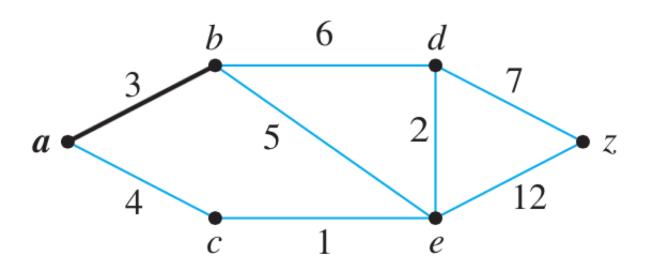
Example

- w(u,v) as given
- Start with d array as



• End with?

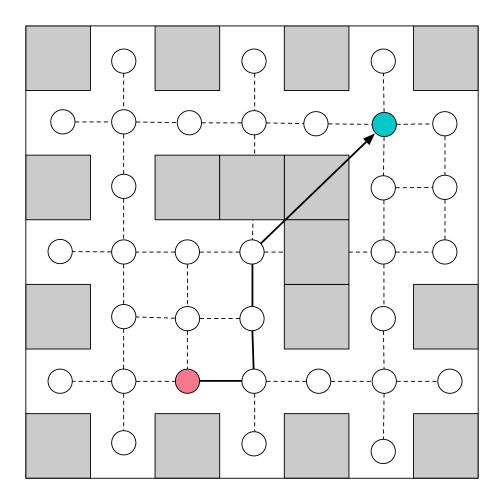
а	b	С	d	е	Z
0	3	4	7	5	14



```
BestFirst(G, s, t) {
 foreach (node u) {
                                      // initialize
  d[u] = +infinity; mark u undiscovered
 }
d[s] = 0; mark s discovered // distance to source is 0
 repeat forever {
                                      // go until finding t
  let u be the discovered node that minimizes dist(u,t)
   if (u == t) return d[t]
                          // arrived at the destination
  else {
    for (each unfinished node v adjacent to u) {
      d[v] = min(d[v], d[u] + w(u,v)) // update d[v]
      mark v discovered
    }
    mark u finished
                                      // we're done with u
```

Best first bad case ...

• Trapped in local minimum



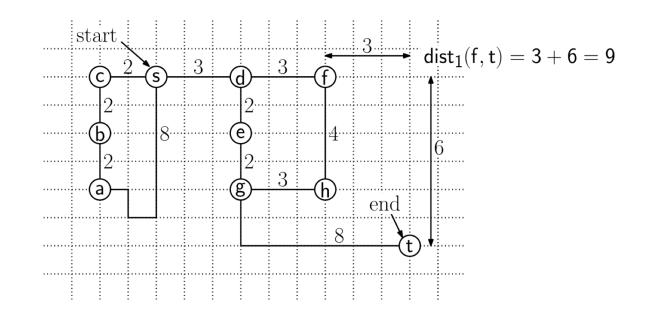
 Pick next node to expand based on sum of distance so far and heuristic

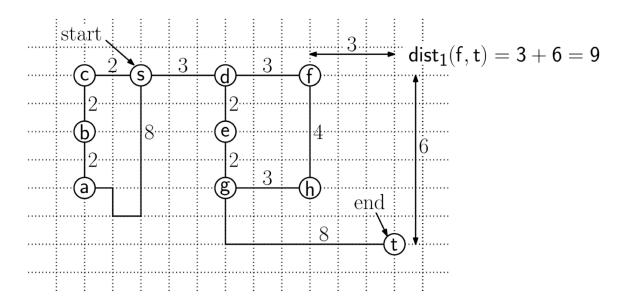
$$f(u) = d[u] + h(u) = d[u] + \operatorname{dist}(u, t)$$

```
A-Star(G, s, t) {
 foreach (node u) {
                                       // initialize
  d[u] = +infinity; mark u undiscovered
 }
 d[s] = 0; mark s discovered // distance to source is 0
 repeat forever {
                                       // go until finding t
   let u be the discovered node that minimizes d[u] + dist(u,t)
                               // arrived at the destination
   if (u == t) return d[t]
   else {
    for (each unfinished node v adjacent to u) {
      d[v] = min(d[v], d[u] + w(u,v)) // update d[v]
      mark v discovered
     }
    mark u finished
                                       // we're done with u
```

A* Example

• Manhattan distance





A [*] Search – Each entry is $d[u] : f(u)$											
Stage	d[s]	d[a]	d[b]	d[c]	d[d]	d[e]	d[f]	d[g]	d[h]	d[t]	
h(u)	15	13	15	17	12	10	9	8	5	0	
Init	0:15	∞ :13	∞ :15	∞ :17	∞ :12	∞ :10	$\infty:9$	∞ :8	∞ :5	$\infty:0$	
1: s	0	8:13	_	2:17	<u>3:12</u>	_	_	_	_	_	
2: d	\downarrow	8:13	_	2:17	3	<u>5:10</u>	6:9	_	_	_	
3: e		8:13	_	2:17	\downarrow	5	<u>6:9</u>	7:8	_	_	
4: f		8:13	_	2:17		\downarrow	6	7:8	_	<u>15:0</u>	
5: t		8:13	_	2:17			\downarrow	7:8	_	15	
Final	0	8	∞	2	3	5	6	7	∞	15	

Good heuristics

- For A* to compute correctly the heuristic h(u) must be:
- Admissible: h(u) never overestimates the graph distance from node u to goal t
- Consistent: h(u') <= delta(u',u'') + h(u'')