The following problems refer to the maximum contiguous sum problem. The pseudo-code for each of the three algorithms covered in class is on the class webpage under Class Resources.

- Problem 1. Consider the problem of not only finding the value of the maximum contiguous sum in an array, but also determining the two endpoints.
  - (a) Give a linear time algorithm for solving this problem. If there is more than one sum with the maximum value, find a longest such sum (i.e., a sum with the most elements of the array A). Write the pseudo-code.
  - (b) What is the output if all entries are negative?
- Problem 2. Consider the algorithms from class for finding the maximum contiguous sum. Assume that it takes time x to execute the instruction

$$S \leftarrow S + A[x]$$

- (a) i. Write a sum for exactly how much time the third algorithm (the linear algorithm) takes executing additions involving elements from the array A? Do not justify.
  - ii. Simplify your sum. Do not justify.
- (b) i. Write a sum for exactly how much time the second algorithm (the quadratic algorithm) takes executing additions involving elements from the array A? Do not justify.
  - ii. Simplify your sum. Show your work.
- (c) **Challenge problem, will not be graded.** Exactly how much time does the first algorithm (the cubic algorithm) take executing additions involving elements from the array A? Show your work.