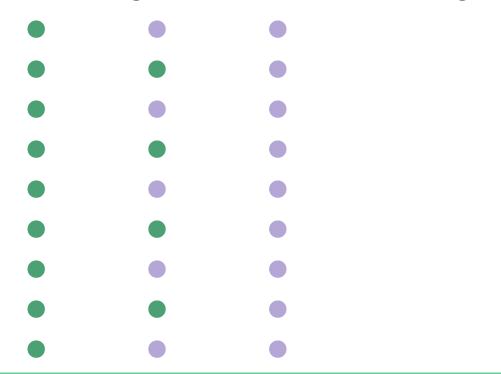
# Grid Coloring

250H

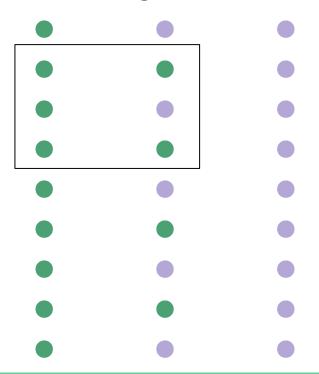
• No matter how you 2-color a 3 x 9 grid there exists a mono rectangle

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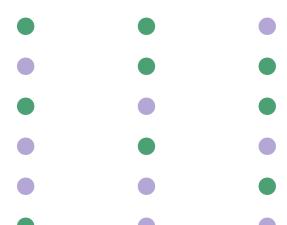
- No matter how you 2-color a 3 x 9 grid there exists a mono rectangle
- What about a
  - o 3 x 8
  - o 3 x 7
  - o 3 x 6
  - o ect?

- No matter how you 2-color a 3 x 9 grid there exists a mono rectangle
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  - o 3 x 8
  - o 3 x 7
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  - o ect?
- I know you are all super excited to talk about this with your classmates in Breakout Rooms

- No matter how you 2-color a 3 x 9 grid there exists a mono rectangle
- What about a

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- $\circ$  3 x 7
- 3 x 6
- o ect?



#### Let's Look Closer

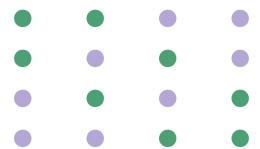
A 2-coloring of a 3x7 grid can be viewed as an 8-coloring of the rows, so if there are 9 rows, two are the same.

# What about?

- 4x4
- 4x5
- 4x6
- 5x5
- 5x6

## What about?

- 4x4
- 4x5
- 4x6
- 5x5
- 5x6



## n x m grid 2-Coloring Theorem

Theorem: n x m is 2-colorable without a monochromatic rectangle if and only if it does not contain a  $3 \times 7$ ,  $7 \times 3$ , or  $5 \times 5$  grid.

#### What if we have 3 colors?

What grids can we color without getting a monochromatic rectangle?

#### What if we have 3 colors?

Theorem: n x m is 3-colorable without a monochromatic rectangle if and only if it does not contain a 19 x 4, 16 x 5, 13 x 7, 11 x 10, 10 x 11, 7 x 13, 5 x 16, 4 x 19 grid.