

Interactive Sound Rendering

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Themes

- Exploiting analytical solutions using Modal Analysis to accelerate numerical simulation and reducing runtime computation
- Capture only perceptually important auditory cues to perform real-time sound synthesis and acoustic propagation on complex 3D scenes

2

Overview

- Interactive Sound Synthesis
- Efficient Numerical Acoustic Simulation
- Interactive Sound Propagation
- Conclusion and Future Work

3

Overview

- Interactive Sound Synthesis
 - Modal Analysis
 - Perceptually-based acceleration techniques
 - Hundreds of sounding objects
 - Sound from image textures
- Efficient Numerical Acoustic Simulation
- Interactive Sound Propagation
- Conclusion and Future Work

4

Physically-based Sound Synthesis

- Aim: Take object geometry and material as input and produce sound
- Current trend: Recorded sounds
- Problems with recorded sounds:
 - Difficult, expensive or dangerous to record (eg. Explosions)
 - Repetitiveness
 - Complex interactions (impact/rolling)



A typical foley studio*

* Image taken from: <http://www.marblehead.net/foley/index.html>

5

Physical Simulation

- Elastic deformable model
- Typical simulation time-steps must be $\sim 10^{-5}$ s
- Direct simulation infeasible
- Efficient method: Modal Analysis

6

Modal Analysis

1st Mode
Frequency = f_0

2nd Mode
Frequency = $f_1 = 2 * f_0$

...Higher modes
Frequency = $f_k = k * f_0$

- Each mode represents a resonant mode of vibration
- Frequency of a mode is fixed
- Applying impulse excites modes of vibration
- Position of impact determines relative amplitude of modes

7

Overview of Technique

Pre-processing

Input Mesh → Transform → Spring-Mass System → Decouple (Diagonalize) → Modal Bank (Frequencies $\omega_1, \omega_2, \dots, \omega_n$)

Runtime

Impulses (f_i) → Transform ($f_i \rightarrow g_i$) → Excitation → Vibration → Add → Sinusoids → Output

9

Approach

- Simpler model: Spring-mass system
- Fast: Supports hundreds of sounding objects
- Runs in real-time, low CPU utilization (~10%), graceful degradation in quality with limited computation
- Exploit human auditory perception
 - Mode Compression
 - Mode Truncation
 - Quality Scaling

10

Modal Analysis

- Deformation modeling
 - Vibration of surface generates sound
 - Sound sampling rate: 44100 Hz
 - Impossible to calculate the displacement of the surface at sampling rate
 - Represent the vibration pattern by a bank of damped oscillators (modes)
- Standard technique for real-time sound synthesis

Modal Analysis

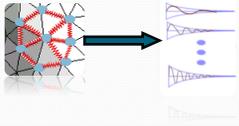
- Discretization
 - An input triangle mesh → a spring-mass system
 - A spring-mass system → a set of decoupled modes

Modal Analysis

- The spring-mass system set-up
 - Each vertex is considered as a mass particle
 - Each edge is considered as a damped spring

Modal Analysis

- Coupled spring-mass system to a set of decoupled modes

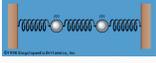


Modal Analysis

- A discretized physics system
 - We use spring-mass system

$$\boxed{K}d + \boxed{C}(\dot{d}, \dot{d}) + \boxed{M}\ddot{d} = f$$

Stiffness Damping Mass



- Small displacement, so consider it linear

$$\boxed{K}d + \boxed{C}\dot{d} + \boxed{M}\ddot{d} = f$$

Stiffness Damping Mass

Modal Analysis

- Solve the Ordinary Differential Equation (ODE)

$$Kd + C\dot{d} + M\ddot{d} = f$$
- Rayleigh damping

$$Kd + (\gamma M + \eta K)\dot{d} + M\ddot{d} = f$$

And diagonalizing $K = GDG^{-1}$
- Now, solve this ODE instead

$$DG^{-1}d + (\gamma G^{-1}M + \eta DG^{-1})\dot{d} + G^{-1}M\ddot{d} = G^{-1}f$$

Modal Analysis

- Solve the ODE

$$DG^{-1}d + (\gamma G^{-1}M + \eta DG^{-1})\dot{d} + G^{-1}M\ddot{d} = G^{-1}f$$
- Substitute $z = G^{-1}d$ (the modes)
Now, solve this ODE instead

$$Dz + (\gamma M + \eta D)\dot{z} + M\ddot{z} = G^{-1}f$$

Modal Analysis

- General solution

$$z_i = c_i e^{\omega_i^+ t} + \bar{c}_i e^{\omega_i^- t}$$

$$\omega_i^\pm = \frac{-(\gamma\lambda_i + \eta) \pm \sqrt{(\gamma\lambda_i + \eta)^2 - 4\lambda_i}}{2}$$
- External excitation defines the initial conditions

Modal Analysis

- Assumptions
 - In most graphics applications, only surface representations of geometries are given
 - A surface representation is used in modal Analysis
 - Synthesized sound appears to be "hallow"

Modal Analysis Summary

- An input triangle mesh →
- A spring-mass system →
- A set of decoupled modes

State Detection

State Detection

- Distinguishing between lasting and transient contacts
 - In contacts?

$$\begin{cases} v_p \cdot n_p < 0 & \text{in contact} \\ v_p \cdot n_p > 0 & \text{not in contact} \end{cases}$$
 - In lasting contacts?

$$\begin{cases} v_t \neq 0 & \text{lasting contact} \\ v_t = 0 & \text{not in lasting contact} \end{cases}$$

Interaction Handling

- Lasting contacts → a sequence of impulses
- Transient contacts → a single impulse

Impulse Response

- Dirac Delta function as impulse excitation
 - General solution

$$z_i = c_i e^{\omega_i^+ t} + \bar{c}_i e^{\omega_i^- t}$$

with initial condition given by the impulse, we have:

$$c_i' = c_i e^{\omega_i^+ t_0} + \frac{g_i}{m_i(\omega_i^+ - \omega_i^-)}$$

$$\bar{c}_i' = \bar{c}_i e^{\omega_i^- t_0} - \frac{g_i}{m_i(\omega_i^+ - \omega_i^-)}$$

Impulse Response

$$z_i = c_i e^{\omega_i^+ t} + \bar{c}_i e^{\omega_i^- t}$$

Handling Lasting Contacts

- The interaction simulation has to be stepped at the audio sampling rate: 44100 Hz
- The update rate of a typical real-time physics simulator: on the order of 100's Hz
- Not enough simulation is provided by the physics engine
- An customized interaction model for sound synthesis

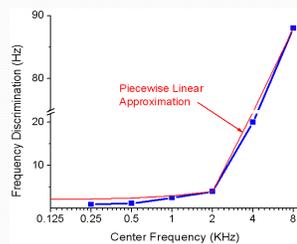
Mode Compression: Principle

- Humans can't distinguish two frequencies arbitrarily close to each other [Sek et. al., 1995*]
- Accuracy in discriminating frequencies depends on the frequency in question
- Different frequencies were played in succession to find if the subject could distinguish between them

*Sek, A., and Moore, B. C. 1995. Frequency discrimination as a function of frequency, measured in several ways. J. Acoust. Soc. Am. 97, 4 (April), 2479–2486.

27

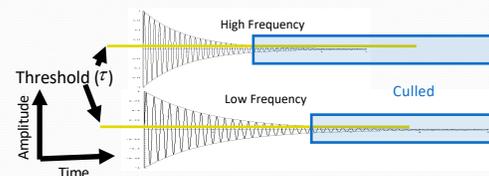
Mode Compression: Auditory Perception



Frequency Discrimination at 2 KHz is about 4 Hz -- We can't tell apart frequencies within the range 1998 - 2002 Hz

28

Mode Truncation



- Impact Sounds: Attack + Decay
- Key Point: Critical to capture attack properly
- Stop mixing mode when its contribution falls below a prescribed threshold, τ (typically -60 to -80 dB of initial level)

29

Quality Scaling

- A typical audio scene consists of foreground and background sounds
- Higher intensity sounds are considered to be foreground
- Idea: Give more importance to foreground sounds
- Provides a graceful way to adapt to variable time constraints

30

Implementation Details

- System: 3.4 GHz Pentium 4 Laptop, 1 GB RAM
- Graphics: GeForce 6800 Go, 256 MB
- Sound: Creative Sound Blaster Audigy 2 ZS
- Physics: Pusk (written by former student: Nico Galoppo), Rendering: G3D
- Also integrated with NVIDIA PhysX Engine recently

31

System Demonstration

VIDEO

32

Sound from Image Textures

VIDEO

33

Limitations

- Implementation: Model only the surface (not an inherent limitation of the approach)
- More approximate than an FEM-based formulation
 - Some tuning is required
- All sound synthesis techniques relying on Modal Analysis: Can only use linear damping models

34

Sounding Liquids [Moss et al. 2009]

- Work in physics and engineering literature since 1917
 - Sound generated by resonating bubbles
- *Physically-based Models for Liquid Sounds* (van den Doel, 2005)
 - Spherical bubble model
 - No fluid simulator coupling
 - Hand tune bubble profile

Background (Fluid)

- Grid-based methods
 - Accurate to grid resolution
 - Bubbles can be smaller
 - Slow
 - Can be two-phase



Background (Fluid)

- Shallow Water Equations
 - Simulate water surface
 - No breaking waves
 - Real time
 - One phase
 - Explicit bubbles



Overview

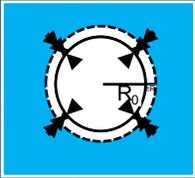
- Generate sound from existing fluid simulation
 - Model sound generated by bubbles
- Apply model to two types of fluid simulators
 - **Particle-Grid-based**
 - Extract bubbles
 - Process spherical and non-spherical bubbles
 - Generate sound
 - **Shallow Water Equations**
 - Processes surface
 - Curvature and velocity
 - Select bubble from distribution
 - Generate sound

Mathematical Formulations

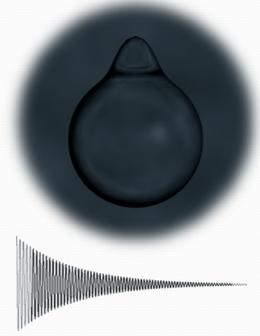
- **Spherical Bubbles**

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{3\gamma p_0}{\rho R_0^3}}$$

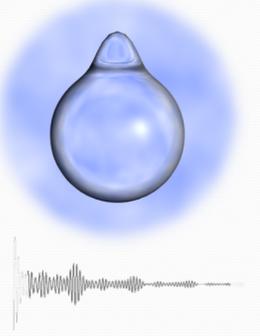
$$\tau(t) = A \sin(2\pi f(t)t) e^{-dt}$$
- **Non-spherical bubbles**
 - Decompose into a spherical harmonics
$$f_n^2 \approx \frac{1}{4\pi^2} (n-1)(n+1)(n+2) \frac{\sigma}{\rho R_0^3}$$

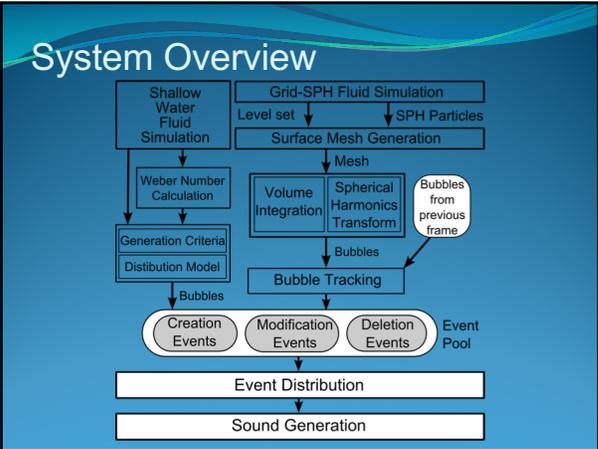


Without
Spherical Harmonics



With
Spherical Harmonics





Summary

- Simple, automatic sound synthesis
- Applied to two fluid simulators
 - Interactive, shallow water
 - High-quality, grid based



Video Demonstration

VIDEO

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44

Overview

- Interactive Sound Synthesis
- Efficient Numerical Acoustic Simulation
 - Novel technique based on 3D Adaptive Rectangular Decomposition
 - Hundred times faster than Finite Difference Time Domain
- Interactive Sound Propagation
- Conclusion and Future Work

45

Acoustics: Governing Equation

- Solve the Linear Wave Equation:

$$\frac{\partial^2 p}{\partial t^2} - c^2 \nabla^2 p = F(\mathbf{x}, t)$$

∇^2 is the Laplacian operator in 3D

c is the speed of sound in air

p is the pressure field to solve

- The RHS is the forcing term, corresponding to volume sound sources in the scene

46

State of the art: Room Acoustics

- Geometric Techniques (e.g. Ray/Beam/Frustum Tracing) combined with explicit diffraction modeling
- Auralization software (e.g. ODEON, CATT): Hybrid image-source and ray-tracing along with (upcoming) explicit diffraction modeling
- Numerical acoustic simulation for complex 3D scenes has been explored only recently (2006)

47

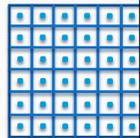
Acoustics for Interactive Applications

- Geometric Approaches
 - Beam Tracing (Funkhouser et. al.)
 - Phonon Tracing (Bertram and Deines et. al.)
 - Frustum Tracing (Chandak et. al.)
- Advantages: Efficient, easy to understand
- Difficulties: Diffraction / Scattering, high-order reflections

48

Numerical Acoustics

- Discretize and solve Wave Equation on a grid
- Explored for complex 3D scenes (eg. auditoria) only recently (2004 – 2006) by Sakamoto et. al.
- Disadvantage: Slow and memory-intensive
 - Simulations are band-limited
- Advantages: Diffraction / Scattering, high-order reflections



49

Acoustics in Games

EAX Advanced HD v4 scenario

Source 1 Environment Source 2 Environment Source 3 Environment

Creative EAX: Pre-baked reverb filters assigned manually to different parts of a map

Property of Dmitry Gait (c) 2003 50

Adaptive Rectangular Decomposition

26 m 35 m

Source (r) Listener

Interface Handling

- Numerical Simulation of the Wave Equation
- Rectangular Decomposition of a 3D scene
- Exploit analytical solutions on rectangular spaces
- 6th order Finite Difference for interface transmission

51

Solution on a Rectangular Domain

- Rectangular space in 3D with size (l_x, l_y, l_z) , and perfectly reflective boundary
- Modal Analysis can be done **analytically** –

$$p(x, y, z, t) = \sum_{i=(i_x, i_y, i_z)} m_i(t) \Phi_i(x, y, z)$$

$$\Phi_i(x, y, z) = \cos\left(\frac{\pi i_x}{l_x} x\right) \cos\left(\frac{\pi i_y}{l_y} y\right) \cos\left(\frac{\pi i_z}{l_z} z\right)$$

52

Leveraging GPU for Acoustics

- Solution of Wave Equation within each rectangle can be done using a 3D Discrete Cosine Transform (DCT)
- DCTs can be computed using FFT
- Use efficient FFT implementation on GPU
 - Govindaraju, N. K., Lloyd, B., Dotsenko, Y., Smith, B., and Manferdelli, J. High-Performance Discrete Fourier Transforms on Graphics Processors. In the *Proc. of 2008 ACM/IEEE Supercomputing*

53

Computational Efficiency

- For a scene of size L in 3D and simulation duration T –

Memory: $\left(\frac{L s v_{\max}}{c}\right)^3$

Time: $T \left(\frac{L}{c}\right)^3 (s v_{\max})^4$

$s = 4$

λ_{\min}

- Nyquist Limit: $s \geq 2$
- FDTD: $s = 10$. My approach: $s = 2.6$
- Speedup with my technique: $(10/2.6)^4 > 100$

54

Demo

[Video](#)

55

Performance Comparison

Scene Name	Volume (m ³)	Time: FDTD (CPU)	Time: My Technique (GPU)	Speedup
Corridor	375	365 min	4 min	~ 90x
House*	1,275	3.5 days	24 min	~ 200x
Cathedral	13,650	1 week (estimated)	29 min	~ 300 x

• Quad-core 2.8GHz Intel Xeon CPU with 8GB RAM, NVIDIA GeForce GTX 280
 * This simulation was band-limited to 2 kHz, instead of 1 kHz

56

Summary

- Adaptive Rectangular Decomposition yields 100x improvement in performance over FDTD and consumes 10x less memory
- Source of Speedup: Modal Analysis of rectangular spaces as well as GPU-DCT
- Can feasibly simulate acoustics for large, complex scenes, such as a Cathedral

57

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59

Overview

- Interactive Sound Synthesis
- Efficient Numerical Acoustic Simulation
- Interactive Sound Propagation
 - Perceptual aspects of acoustics
 - Novel perceptually-motivated techniques
 - Interactive auralization system: moving sources and listener
- Conclusion and Future Work

60

Impulse Response (IR)

The diagram illustrates sound propagation from a source (head) to a listener (ear) via a direct path and a reflected path off a wall. Below, two graphs show the relationship between time and frequency. The 'Impulse Response' graph plots amplitude (1+a) against time, showing a direct impulse at time Δt and a reflected impulse at a later time. The 'Frequency Response' graph plots amplitude (1+a) against frequency (Hz), showing a sinusoidal wave with a period of $1/\Delta t$.

61

Challenges

- Direct approach is costly
- Days of simulation (even with fast simulator)
- Terabytes of storage

A grid diagram representing a simulation space. Red circles indicate source locations, and blue circles indicate listener locations. The grid is composed of small squares, with sources and listeners placed at various intersections.

62

Contributions

- Approach –
 - Sample data at lower resolution in space (~1 m)
 - Novel perceptually-based scheme: Store each Impulse Response compactly
 - Spatially-interpolate Impulse Responses
- Audio engine that uses fast frequency-domain convolutions

63

Auditory perception of acoustic spaces

- Direct Sound: Sense of direction
- ER: Loudness, Timbre, "Envelopment". Perceivable spatial variation.
- LR: Only statistical properties perceivable – Decay Time (RT60), Periodicities (Flutter echoes)

Reference: "Room Acoustics" by Heinrich Kuttruff ⁶⁴

IR Factoring (1)

65

IR Factoring (2)

Peak Detection

- Finds peak delays and amplitudes

66

IR Factoring (3)

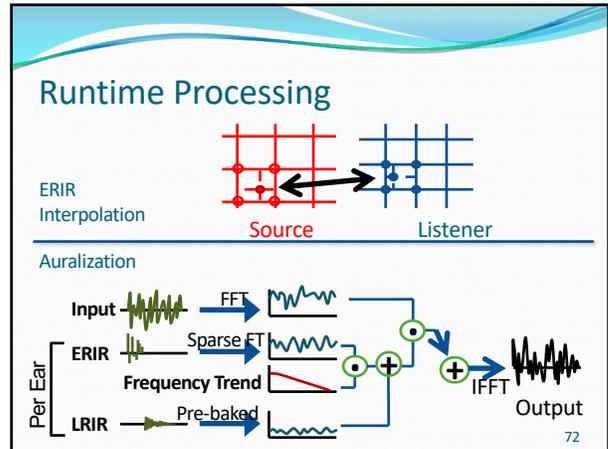
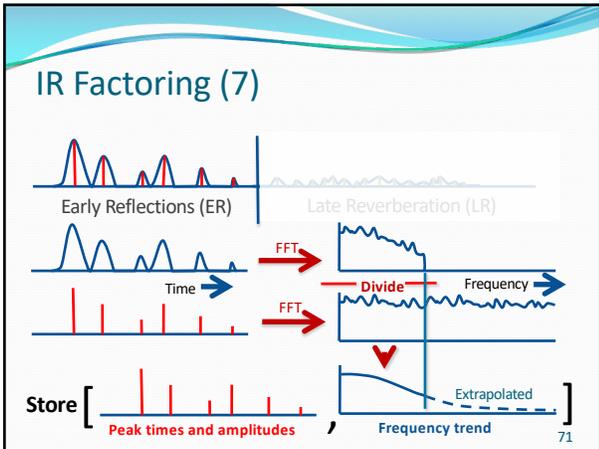
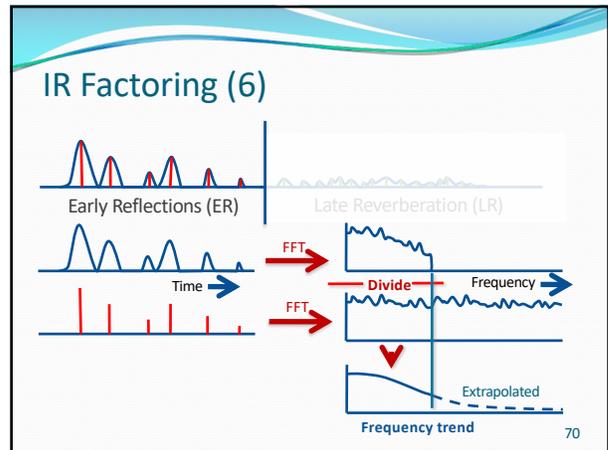
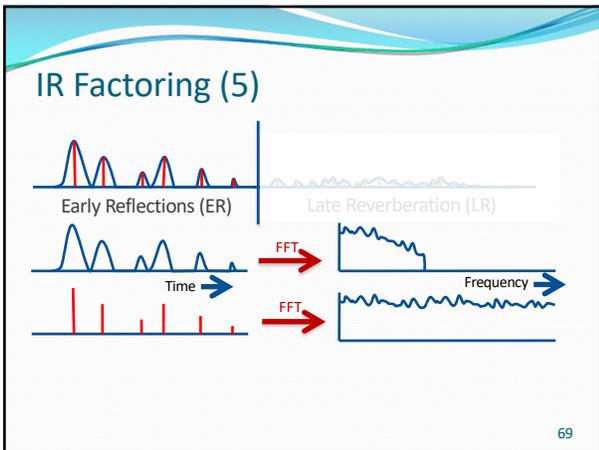
ER - LR Decomposition

- Compute and store only one Late Reverberation filter per room
- Reduces pre-computation time and runtime memory usage by 10 times

67

IR Factoring (4)

68



Performance

- Pre-processing times typically a few hours
- Can handle about 10 sound sources in real-time on a Quad-core Xeon system with 4 GB RAM
- Bottleneck: 1D FFT
 - Auralization system maps well to parallel processors

83

Walkthrough: Game Scene

- "Citadel" Scene from the game Half-Life 2
- Large Size: 3,500 m³
- Complex geometry (fin-like structures)

84

System Demonstration

Video

<http://www.youtube.com/watch?v=MQt1jtDBNK4>

75

Summary

- The first interactive sound propagation system that leverages numerical simulation
- Can render important acoustic effects like Late Reverberation and Diffraction low-pass filtering in real-time
- Can handle multiple moving sound sources and listener
- Works for large, complex 3D scenes

76

Overview

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78

Summary

- Interactive Sound Synthesis
 - Perceptually-motivated optimizations enabling hundreds of sounding objects in real-time
- Efficient Numerical Acoustics
 - A simulator 100 times faster than Finite Difference Time Domain for constant wave speed simulations
- Interactive Sound Propagation
 - Leverage fast numerical acoustics
 - Exploit auditory perception
 - Render wave-based acoustics for multiple moving sources and listener in real-time

79

Conclusion

- Physically-based Sound: Complex underlying physical processes require a lot of computational power
- Combination of efficient algorithms, perceptually-motivated optimizations and fast hardware

80

Future Work: Sound Synthesis

- Ultimate goal: Virtual Worlds with physically-based sounds for collisions, rolling, sliding, creaking, cloth, gunshots, water, automobiles, and so on
- [Infer audio materials](#) from video
- [Virtual Musical Instruments](#) using next generation user interfaces

81

Future Work: Sound Propagation

- Acoustics for Games and Virtual Worlds
- Accurate numerical predictions in auditorium design
- Efficient numerical solvers for high-performance computing applications
- Combine Sound Synthesis and Acoustics for a completely physically-based auralization system

82

References

- Nikunj Raghuvanshi and Ming C. Lin. **Interactive Sound Synthesis for Large Scale Environments**. In SI3D '06: Proceedings of the 2006 symposium on Interactive 3D graphics and games, 2006.
- Nikunj Raghuvanshi, Nico Galoppo, and Ming C. Lin. **Accelerated Wave-based Acoustics Simulation**. In SPM '08: Proceedings of the 2008 ACM symposium on Solid and physical modeling, 2008.
- Nikunj Raghuvanshi, Rahul Narain, and Ming C. Lin. **Efficient and Accurate Sound Propagation using Adaptive Rectangular Decomposition**. IEEE Transactions on Visualization and Computer Graphics, December 2009.
- Nikunj Raghuvanshi, Brandon Lloyd, and Ming C. Lin. **Efficient Numerical Acoustic Simulation on Graphics Processors Using Adaptive Rectangular Decomposition**. Proc. EAA Symposium on Auralization, 2009.

83

84