

Problem 1. Let  $G = (V, E)$  be a directed graph.

- (a) Assuming that  $G$  is represented by an adjacency matrix  $A[1..n, 1..n]$ , give a  $\Theta(n^2)$ -time algorithm to compute the adjacency list representation of  $G$ . (Represent the addition of an element  $v$  to a list  $l$  using pseudocode by  $l \leftarrow l \cup \{v\}$ .)
- (b) Assuming that  $G$  is represented by an adjacency list  $\text{Adj}[1..n]$ , give a  $\Theta(n^2)$ -time algorithm to compute the adjacency matrix of  $G$ .

Problem 2. An undirected graph is 2-colorable if each vertex can be assigned either Red or Blue so that no two vertices that share an edge have the same color.

- (a) Use breadth-first-search to determine if an undirected graph  $G = (V, E)$  is 2-colorable, and if so 2-color it.
- (b) Use depth-first-search to determine if an undirected graph  $G = (V, E)$  is 2-colorable, and if so 2-color it.

Problem 3. Let  $G = (V, E, p)$  be a directed graph representing a network of roads between cities. The weight  $p(e)$  is the probability that road  $e$  will be open, so that  $0 \leq p(e) \leq 1$ . The probabilities are assumed to be independent. You want to take a trip from city  $a$  to city  $b$ .

- (a) Give an algorithm to find the route that has the most chance of being open.
- (b) How fast is your algorithm?