## CMSC132 Summer 2017 Midterm 2

First Name (PRINT): $\qquad$
Last Name (PRINT): $\qquad$

I pledge on my honor that I have not given or received any unauthorized assistance on this examination.

Your signature: $\qquad$
Instructions

- This exam is a closed-book and closed-notes exam.
- Total point value is 100 points.
- The exam is a 80 minutes exam.
- Please use a pencil to complete the exam.
- WRITE NEATLY. If we cannot understand your answer, we will not grade it (i.e., 0 credit).

| 1. Multiple Choice | $/ 25$ |
| :--- | :---: |
| 2. Short Answer | $/ 45$ |
| 3. Programming | $/ 30$ |
| Total | $/ 100$ |

## 1. [25 pts] Multiple Choice

Identify the choice that best completes the statement or answers the question. Circle your answer.

1) [2] The cost of inserting or removing an element to/from a heap is $\log (N)$, where $N$ is the total number of elements in the heap. The reason for that is:
a) Heaps keep their entries sorted
b) Heaps are balanced BST.
c) Heaps are balanced binary trees.
d) Heaps are a version of Red-Black trees
2) [2] What is the output of fun (2)?
```
int fun(int n) {
    if (n == 4)
        return n;
    else
        return 2*fun(n+1);
    }
```

a) 4
b) 8
c) 16
d) Runtime Error
3) [2] 2-3-4 Tree guarantees searching in $\qquad$ time.
a) $O(\log n)$
b) $\mathrm{O}(\mathrm{n})$
c) $\mathrm{O}(1)$
d) $\mathrm{O}(\mathrm{n} \log \mathrm{n})$
4) [2] What is the advantage of an iterative method over a recursive one?
a. It makes fewer calls
b. It has less overhead
c. It is easier to write, since you can use the method within itself.
d. It uses a stack
5) [2] A priority queue can be efficiently implemented using which of the following data structures?
a) Array
b) Linked List
c) Binary Heaps
d) None of the above
6) [2] A Priority-Queue is implemented as a Max-Heap. Initially, it has 5 elements. The levelorder traversal of the heap is given below: $10,8,5,3,2$. What is the level order traversal of the heap after inserting 1 and 7.
a) $10,8,7,5,3,2,1$
b) $10,8,7,2,3,1,5$
c) $10,8,7,1,2,3,5$
d) $10,8,7,3,2,1,5$
7) [2] What is the worst-case time complexity for insert and remove operations in a Binary Heap?
a) $\mathrm{O}(\mathrm{n})$ for all
b) $O(\log n)$ for all
c) $O(\log n)$ insert, and $O(n)$ for remove
d) $O(\log n)$ for remove, and $O(n)$ for insert
8) [2] In an array based implementation (root index is 1) of a Binary Heap, the children of a node at position k are at positions:
a) 2 k and $2 \mathrm{k}-1$
b) $2 \mathrm{k}+1$ and $2 \mathrm{k}+2$
c) $2 k$ and $2 k+1$
d) $2(\mathrm{k}+1)$ and $2(\mathrm{k}+1)+1$
9) [3] The following numbers are inserted into an empty binary search tree in the given order: $10,12,3,5,14,2,11,18$. What is the height of the binary search tree (the height is the maximum distance (number of edges) of a leaf node from the root, height of a tree with one node is 0 .)?
a) 5
b) 3
c) 4
d) 2
10) [3] Here is an INCORRECT pseudo code for the algorithm which is supposed to determine whether a sequence of parentheses is balanced:

```
declare a character stack
while ( more input is available) {
    read a character
    if (the character is a '(' )
        push it on the stack
        else if( the character is a ')' and the stack is not empty )
            pop a character off the stack
        else
            print "unbalanced" and exit
}
print "balanced"
```

Which of these unbalanced sequences does the above code think is balanced?
a) $((())$
b) $(()()))$
c) ()$)(()$
d) $(()))()$
11) [2] What is the complexity of 2-3-4 Tree insert/delete/search operations?
a) $O(\log n)$
b) $(\mathrm{n})$
c) (1)
d) $(\mathrm{n} \log \mathrm{n})$
12) What is the number of swaps that occur after inserting 20 into the following heap:

a) 0
b) 1
c) 2
d) 3

## 2. [45 pts ] Short Answer

1) [6] Write the preorder, inorder, and postorder traversal of the following binary tree:


| preOrder |  |
| :--- | :--- |
| inOrder |  |
| postOrder |  |

2) [3] What does this function do?
```
int foo(Node n) {
    if (n == null) return 0;
    if (n.left == null && n.right == null) return 1;
    return foo(n.left) + foo(n.right);
}
```

Answer:
3) [3] Suppose that you do binary search for the key 39 in the following sorted array of size 15:

$$
101125313639535556646875788287
$$

Give the sequence of keys in the array that are compared with 39 Answer:
4) [3] If the given preOrder traversal for a binary search tree is $\{10,3,1,7,15,20,25\}$, construct the binary search tree.
5) [4] Given the following contents of an array implementation of a stack, where 50 is at the top of the stack.
$\begin{array}{llllll}0 & 1 & 2 & 3 & 4 & 5\end{array}$

| 20 | 30 | 40 | 50 |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |

Show the contents of the stack and the location of top after doing the following

```
stack.pop();
stack.push(60);
stack.push(70);
stack.push(80);
stack.pop();
stack.push(90)
\begin{tabular}{|l|l|ll|l|l|l|}
\hline 0 & 1 & 2 & 3 & 4 & 5 \\
\hline & & & & & \\
\hline
\end{tabular}
```

6) [4] Given the following contents of a circular array implementation of a queue

| 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 30 | 40 |  |  |  |
| first |  |  |  |  |  |

Show the contents of the queue and locations of first and last after doing the following:

```
Queue. dequeue();
Queue. dequeue();
Queue.enqueue (50);
Queue.enqueue (60);
Queue.enqueue (70);
Queue. dequeue();
Queue.enqueue (80) ;
    \(0 \quad 1\)
```

    2
    3
    4 5

|  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |

7) [4] Draw the binary heap shown in the form of an array.

| 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| -- | 16 | 14 | 10 | 8 | 7 | 9 | 3 | 2 | 4 | 1 |

8) [4] Show the contents of the heap after the value 15 is inserted.

0 \begin{tabular}{llllllllll|l|l|l|l|}
0 \& 1 \& 2 \& 3 \& 4 \& 5 \& 6 \& 7 \& 8 \& 9 \& 10 \& 11 <br>

| -- |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | <br>

\hline
\end{tabular}

9) [3] Draw the Binary Search Tree after you delete key 8.

10) [5]Construct a left-leaning red-black tree when the following elements are inserted in this order: 20, 10, 15, 18, 30. Show your steps for each number. Use dashed line for red edge.
11) Given a 2-3-4 tree as follows

a) [3] Draw the 2-3-4 after inserting 44, 84,86 into this tree
b) [3] Draw the tree after deleting 94 from the original 2-3-4 tree

## 3. [30 pts] Programming questions

Use the following Node definition for questions 1)—4)
class Node\{
int key;
Node left, right;
\}

1) [6] Write a method "int sum (Node $r$ )", which returns the sum of all keys in a given binary tree. Calling sum on the following tree will return 51 . Sum of an empty tree is 0 .

2) [8] Write a method "boolean find(Node r, int key)", which receives a Binary Search Tree $r$ and a key as arguments, and returns if the key exists in the tree
3) [8] Write a method "int getMin (Node r)", which returns the minimum key in the given Non-Empty Binary Tree. Calling getMin on the following tree returns 1.

4) [8] write the method "Node mirror (Node r)", which returns the mirror of the given binary tree. For example, calling mirror on the original tree, will return the mirror tree shown below.

Original Tree

Mirror Tree
