1. (40 points) Throughout this problem Bill has a 2 -sided dice with numbers 1,2 and a 3 -sided die with numbers $1,2,3$.
(a) (15 points) Assume both dice are fair. Bill throws both of them. For $2 \leq i \leq 5$ give the prob that the sum is $i$.
(b) (20 points) Let $0 \leq p \leq \frac{1}{2}$. Assume the 2 -sided dice is fair but the 3 -sided dice has
Prob of $1=p$
Prob of $2=1-2 p$
Prob of $3=p$
Bill throws both of them. For $2 \leq i \leq 5$ give the prob that the sum is $i$.
(c) (5 points) Let $p$ be as in the last part. Is there a value of $p$ such that all of the sums $2,3,4,5$ come up with the same probability.
(d) (0 points but thing about it) Can you load two 6-sided dice to get fair sums?

## GO TO NEXT PAGE

2. (60 points) On the planet Vorlon they play a game that is similar to what we call Poker but with a different deck of cards.

Every card has a rank from $\{1,2, \ldots, 7\}$.
Every card has a suite from $\{R, B\}$.
Every player gets 3 cards.
In most of the questions we will ask for the prob of a certain type of hand. Give the answer to 4 places since the last question is to rank them.
(a) What is prob of a straight that is NOT a flush (e.g., $3 R, 4 R, 5 B$ ) We DO allow wrap-around, so 7-1-2 counts.
(b) What is prob of a flush that is NOT a straight (e.g., 2R, 4R, 9R)
(c) What is prob of a straight flush (e.g., $3 R, 4 R, 6 R$ ) We DO allow wrap-around, so 7-1-2 counts.
(d) What is prob of a pair (e.g., $3 R, 3 B, 7 R$ ). Note that a pair cannot be a straight of a flush.
(e) What is prob of getting NOTHING- a hand that is neither a straight, nor a flush, nor does it contain 2 of a kind. (e.g., $3 R$, $5 R, 6 B$ )
(f) Rank the types of hands from most likely to least likely.

