

# Honors Homework 4: Grid Coloring

CMSC 250H

Due Date: Feb 22, 9:00AM, HARD DEADLINE

1. (50 points) Find a  $n \times m$  grid such that for all 4-colorings of  $n \times m$  there is a mono rectangle. Prove your answer.
2. (50 points) For all  $c$  find  $n$  and  $m$  such that for all  $c$ -colorings of  $n \times m$  there is a mono rectangle. Prove your answer.
3. (0 points) Challenge Problem: There is an  $n$  such that for all 2-colorings of  $n \times n$  there exists a mono SQUARE. Give me something even if you have no idea to show you thought about it.