BILL, RECORD LECTURE!!!!

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Today:
Admin,
Ramsey Theory and Its
"Applications"

Admin

Necessary Administrative

Everything in these slides is also on the written syllabus on the course website.

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Course Webpage:

https://www.cs.umd.edu/users/gasarch/COURSES/752/S26/index.html

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- 1. Taught by William Gasarch. Tu-Th 3:30-4:45 in IRB 2107.
- 2. TAed by Javier Marinkovic.

Necessary administrative stuff

- Course Website: Will post slides, notes, and HW there.
- ► Elms: will post recording.
- ► Gradescope: you will **submit HW** there.
- ► Gradescope: we will **grade HW** there.
- ▶ Regrade requests due within a week of the HW being graded.
- Piazza is great for asking questions.

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IF you are auditing this class for whatever reason- perhaps you are having a hard time getting permission to take it, or perhaps you like the material but don't want to take it, let me know and I will put you on the class email list and invite you to join the Piazza.

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- ► Appointments (possibly on zoom, possibly at night)

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- ► Ability to write proofs.

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- Ability to write proofs.
- ► There may be some short programming project. (This is not a course like CMSC 412 where the project IS the course.)

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 - 3.4 In Spring of 2025 recording failed 3 times. One was my fault, two were not my fault.
 - 3.5 There will be some in-class problems which count for the final grade.

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- ▶ There will be one in-class midterm, one take home final.

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Bill I am not sure why you are telling me about **time stamps**, but, as the kids say, whatever.

You can use **ChatGPT policy** but

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- 6. This class is rather non-standard.

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- 2. **Recommend** Make sure you understand what you are handing in.
- 3. If not you will crash and burn on the written exams.

Required or Recommended Text None.

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There are actually three textbooks on Ramsey Theory.

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Why?

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Why?

That might be a harder question then improving the bounds on $R_2(k)$.

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For this course there will be notes, slides, and recordings of lecture.

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If **for whatever reason** you are falling behind in the class, or are having trouble with the HW, see us in office hours or **you can** make an appointment to see us! Either in person or on zoom.

Here is a sample of reasons and my comments on them:

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It satisfies a requirement, but also one of the above. FINE, BUT I HOPE THAT YOU ALSO LIKE IT.

To expand my knowledge of Computer Science.

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Ramsey Theory and its "Applications"

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Thm \forall 2-coloring of the edges of K_6 there is a mono triangle. **Def** Let $a, n \in \mathbb{N}$ and $A \subseteq \mathbb{N}$.

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Ramsey's Thm for 2-col Graphs $\forall k \exists n = R(k)$ such that the following happens: For all COL: $\binom{[n]}{2} \rightarrow [2]$ there exists $A \subseteq [n]$, |A| = k, such that COL: $\binom{A}{2}$ is constant.

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Another Example

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Thm For all 2-colorings of [35] there exists a mono 4-AP.

Van der Waerden's Thm for 2-coloring of $\mathbb N$ For all k there exists W=W(k) such that the following happens: For all $\mathrm{COL}\colon [W]\to [2]$ there exists a mono k-AP.

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 to other parts of pure math,
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 to math competitions (I'm on the UMCP HS Math Competition Committee.)

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