

Efficient Three-Party Computation from Cut-and-Choose

Seung Geol Choi¹ and Jonathan Katz² and **Alex J. Malozemoff**²
and Vassilis Zikas³

¹United States Naval Academy

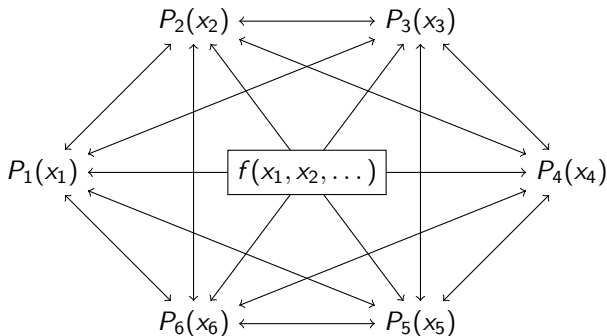
²University of Maryland

³ETH Zurich

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Background

Secure Computation: Parties P_1, P_2, \dots, P_n compute some (common) function $f(x_1, x_2, \dots, x_n)$ while keeping x_1, x_2, \dots, x_n private, *even if $n - 1$ parties are corrupt!*



Note: Interested in **malicious** security, where adversaries can deviate *arbitrarily*

Secure Computation: 2PC vs. MPC

Considered separately in the literature:

2PC

- Two parties, 1 corruption
- Many efficient constructions
- Most based on *garbled circuits*
 - Boolean circuits
 - $\mathcal{O}(1)$ rounds
 - Preprocessing time: **none**
 - Online time: **fast**

MPC

- n parties, $\leq n - 1$ corrupt
- Fewer efficient constructions
- Most efficient scheme: SPDZ
 - Arithmetic circuits
 - $\mathcal{O}(\text{depth})$ rounds
 - Preprocessing time: **slow**
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Question: Say we want to do secure computation with (fixed) $n > 2$.
Do we need all the MPC machinery?

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Question: Say we want to do secure computation with $n = 3$.
Do we need all the MPC machinery?

Three-Party Computation: Challenges

1. Not 2PC, so not clear that two-party protocols/ideas apply
 - e.g., cut-and-choose, oblivious transfer, authenticated bits
2. Do not want to resort to complexity/cost of full MPC
 - Only need efficiency for *three* parties, not arbitrary n

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- Requires almost entirely two-party communication
 - Only *three* broadcasts needed
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 - Roughly $8\times$ more expensive than underlying 2PC scheme
- Requires almost entirely two-party communication
 - Only *three* broadcasts needed
 - Existing schemes require broadcast in every round
- Faster *start-to-finish* running time versus SPDZ
 - SPDZ has faster *on-line* running time

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Garble(C) →



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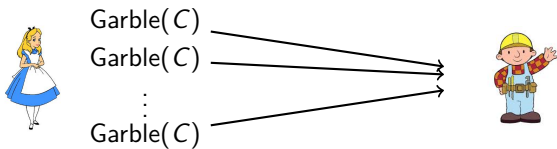
Garble(C')



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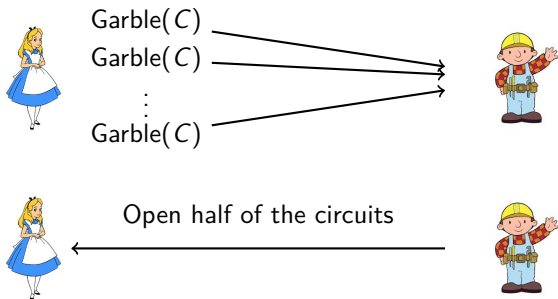
Cut-and-Choose (High-Level Idea) [LP07]:



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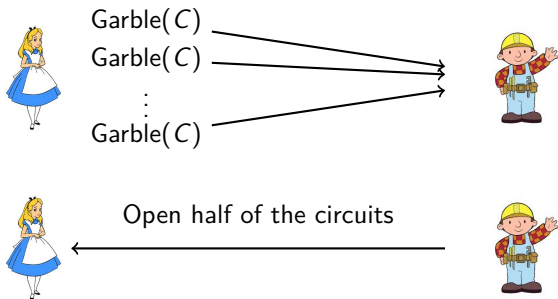
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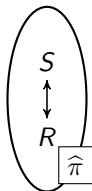
If “checked” circuits constructed correctly, w.h.p. majority of unopened garbled circuits constructed correctly

3PC: High-level Idea

How to lift cut-and-choose 2PC protocol to three-party setting:

$\widehat{\pi}(S, R)$: cut-and-choose 2PC protocol between sender S and receiver R

- S generates many garbled circuits using a *circuit garbling scheme*
- R does cut-and-choose on circuits

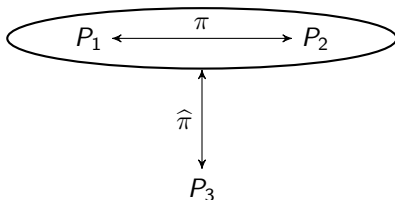


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How to lift cut-and-choose 2PC protocol to three-party setting:

We *emulate* $\hat{\pi}$ using three parties:

- P_1 and P_2 run two-party protocol π emulating S
 - In particular, the *circuit garbling scheme* of S
- P_3 plays role of R

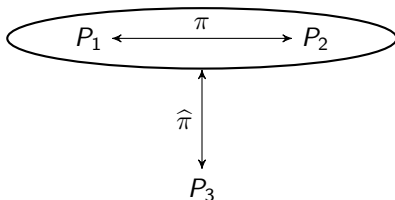


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Note: using generic 2PC schemes for $\hat{\pi}$ and π not efficient!

3PC: Main Steps

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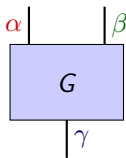
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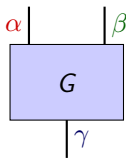
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Recall: (Single-Party) Circuit Garbling Scheme



Wire	Keys		Mask Bit
α	$K_{\alpha,0}$	$K_{\alpha,1}$	λ_{α}
β	$K_{\beta,0}$	$K_{\beta,1}$	λ_{β}
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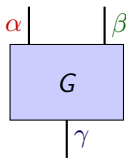
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Garbled Gate:

0	0	$\text{Enc}_{K_{\alpha,0}, K_{\beta,0}} \left(K_{\gamma, G(\lambda_{\alpha}, \lambda_{\beta}) \oplus \lambda_{\gamma}} \parallel G(\lambda_{\alpha}, \lambda_{\beta}) \oplus \lambda_{\gamma} \right)$
0	1	$\text{Enc}_{K_{\alpha,0}, K_{\beta,1}} \left(K_{\gamma, G(\lambda_{\alpha}, \lambda_{\beta} \oplus 1) \oplus \lambda_{\gamma}} \parallel G(\lambda_{\alpha}, \lambda_{\beta} \oplus 1) \oplus \lambda_{\gamma} \right)$
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Note: This is standard Yao using point-and-permute

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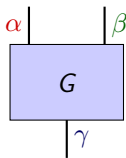
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Keys

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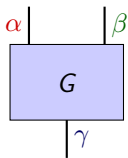
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↑
Tags

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Note: Garbling party knows keys/tags being encrypted

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Solution: Combine distributed encryption [DI05] with authenticated bit shares [NNOB12]

Building Blocks (1): Distributed Encryption Scheme [DI05]

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Note: Cost per party (in PRF calls) to encrypt message of length ℓ is 2ℓ

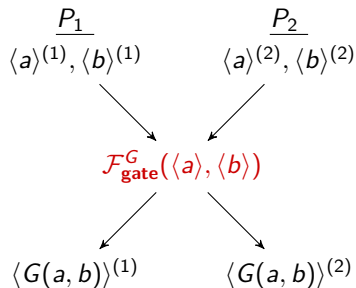
Building Blocks (2): Functionalities Needed

$\langle \cdot \rangle$ denotes (form of authenticated and linear) bit secret sharing

Note: $[\cdot]$ denotes (standard) secret sharing

$\langle \cdot \rangle^{(i)}$, $[\cdot]^{(i)}$ denotes P_i 's share

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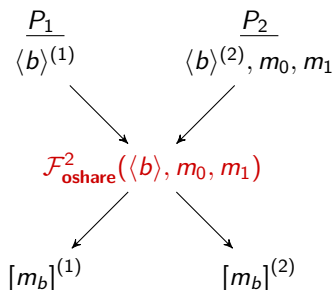


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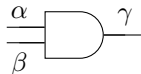
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Building Blocks (2): Functionalities Needed

Note: efficient maliciously secure constructions exist

- Uses ideas from [NNOB12]
- See paper for details

Example: Garbling an AND Gate



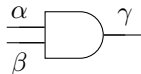
$$\lambda_\alpha = 1, \lambda_\beta = 0, \lambda_\gamma = 1$$

Standard (single-party) garbling:

Step 1: S computes tags:

i	j	$AND(\lambda_\alpha \oplus i, \lambda_\beta \oplus j) \oplus \lambda_\gamma$
0	0	$AND(1 \oplus 0, 0 \oplus 0) \oplus 1 = 1$
0	1	$AND(1 \oplus 0, 0 \oplus 1) \oplus 1 = 0$
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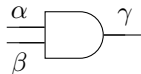
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Distributed garbling:

Step 1: P_1 and P_2 compute *oblivious sharings* of tags:

i	j	$\langle \text{AND}(\lambda_\alpha \oplus i, \lambda_\beta \oplus j) \oplus \lambda_\gamma \rangle$
0	0	$\mathcal{F}_{\text{gate}}^{\text{AND}}(\langle 1 \rangle \oplus \langle 0 \rangle, \langle 0 \rangle \oplus \langle 0 \rangle) \oplus \langle 1 \rangle = \langle 1 \rangle$
0	1	$\mathcal{F}_{\text{gate}}^{\text{AND}}(\langle 1 \rangle \oplus \langle 0 \rangle, \langle 1 \rangle \oplus \langle 1 \rangle) \oplus \langle 1 \rangle = \langle 0 \rangle$
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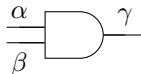
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Standard (single-party) garbling:

Step 2: S encrypts key + tag:

i	j	
0	0	$\text{Enc}_{K_{\alpha,0}, K_{\beta,0}}(K_{\gamma,1} \ 1)$
0	1	$\text{Enc}_{K_{\alpha,0}, K_{\beta,1}}(K_{\gamma,0} \ 0)$
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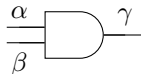
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Distributed garbling:

Step 2a: P_1 and P_2 compute *oblivious sharings* of each party's sub-keys:

i	j		
0	0	$\mathcal{F}_{\text{oshare}}^1(\langle 1 \rangle, s_{\gamma,0}^1, s_{\gamma,1}^1) = \begin{bmatrix} s_{\gamma,1}^1 \end{bmatrix}$	$\mathcal{F}_{\text{oshare}}^2(\langle 1 \rangle, s_{\gamma,0}^2, s_{\gamma,1}^2) = \begin{bmatrix} s_{\gamma,1}^2 \end{bmatrix}$
0	1	$\mathcal{F}_{\text{oshare}}^1(\langle 0 \rangle, s_{\gamma,0}^1, s_{\gamma,1}^1) = \begin{bmatrix} s_{\gamma,0}^1 \end{bmatrix}$	$\mathcal{F}_{\text{oshare}}^2(\langle 0 \rangle, s_{\gamma,0}^2, s_{\gamma,1}^2) = \begin{bmatrix} s_{\gamma,0}^2 \end{bmatrix}$
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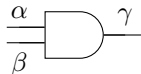
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Distributed garbling:

Step 2b: P_1 and P_2 use *distributed encryption* to encrypt:

i	j	
0	0	$\text{Enc}_{K_{\alpha,0}, K_{\beta,0}} \left(\left[s_{\gamma,1}^1 \right] \parallel \left[s_{\gamma,1}^2 \right] \parallel \langle 1 \rangle \right)$
0	1	$\text{Enc}_{K_{\alpha,0}, K_{\beta,1}} \left(\left[s_{\gamma,0}^1 \right] \parallel \left[s_{\gamma,0}^2 \right] \parallel \langle 0 \rangle \right)$
1	0	$\text{Enc}_{K_{\alpha,1}, K_{\beta,0}} \left(\left[s_{\gamma,1}^1 \right] \parallel \left[s_{\gamma,1}^2 \right] \parallel \langle 1 \rangle \right)$
1	1	$\text{Enc}_{K_{\alpha,1}, K_{\beta,1}} \left(\left[s_{\gamma,1}^1 \right] \parallel \left[s_{\gamma,1}^2 \right] \parallel \langle 1 \rangle \right)$

Example: Garbling an AND Gate



$$\langle \lambda_\alpha \rangle = 1, \langle \lambda_\beta \rangle = 0, \langle \lambda_\gamma \rangle = 1$$

Distributed garbling:

Step 2b: P_1 and P_2 use *distributed encryption* to encrypt:

i	j	
0	0	$\text{Enc}_{K_{\alpha,0}, K_{\beta,0}} \left(\begin{bmatrix} s_{\gamma,1}^1 \end{bmatrix} \parallel \begin{bmatrix} s_{\gamma,1}^2 \end{bmatrix} \parallel \langle 1 \rangle \right)$
0	1	$\text{Enc}_{K_{\alpha,0}, K_{\beta,1}} \left(\begin{bmatrix} s_{\gamma,0}^1 \end{bmatrix} \parallel \begin{bmatrix} s_{\gamma,0}^2 \end{bmatrix} \parallel \langle 0 \rangle \right)$
1	0	$\text{Enc}_{K_{\alpha,1}, K_{\beta,0}} \left(\begin{bmatrix} s_{\gamma,1}^1 \end{bmatrix} \parallel \begin{bmatrix} s_{\gamma,1}^2 \end{bmatrix} \parallel \langle 1 \rangle \right)$
1	1	$\text{Enc}_{K_{\alpha,1}, K_{\beta,1}} \left(\begin{bmatrix} s_{\gamma,1}^1 \end{bmatrix} \parallel \begin{bmatrix} s_{\gamma,1}^2 \end{bmatrix} \parallel \langle 1 \rangle \right)$

Note: Cost of encryption $8\times$ cost in 2PC setting

3PC: Main Steps

Two main steps:

1. Distribute S 's circuit garbling scheme between two parties
2. Modify existing 2PC protocol to use distributed circuit garbling scheme

Lifting 2PC Protocols to Three Party Setting

Goal: Construct 3PC scheme using distributed garbling protocol

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High-Level Idea

- Take existing cut-and-choose protocol (e.g., [LP07, LP11, Lin13])
- Replace sender's circuit generation by distributed circuit generation

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Note: Not exactly this straightforward; see paper for details

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Security Intuition

- **Exactly one of P_1 or P_2 malicious:** garbled circuits either correct or abort independent of input
- **Both P_1 and P_2 malicious:** cut-and-choose by P_3 detects cheating
- **P_3 malicious:** covered by security of garbling protocol

Summary

Can “lift” cut-and-choose 2PC protocols to 3PC setting

- Provides efficient **constant round** 3PC protocol
- Only $\approx 8\times$ slower than underlying 2PC protocol
- Approach works for combination of [LP07, LP11] and [Lin13]
- Only *three* broadcast calls needed
 - Important in WAN settings where broadcast is expensive
- Faster *start-to-finish* time than existing 3PC solutions

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Future Work:

- Support free-XOR
- Optimize distributed encryption scheme (à la JustGarble [BHKR13])

Any questions?

E-mail: `amaloz@cs.umd.edu`

URL: `https://www.cs.umd.edu/~amaloz`

ePrint: `https://eprint.iacr.org/2014/128`