

# ADVERSARIAL TRAINING FOR FREE!

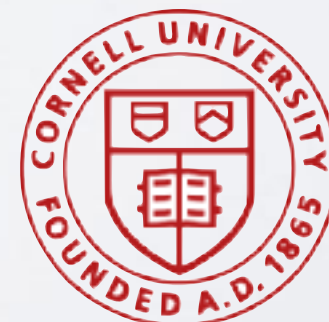


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2019



UNIVERSITY OF  
MARYLAND



# SUPERVISED MACHINE LEARNING

some training data (image, labels)



**Pandas**

**or**



**Pumpkins**



**Training Algorithm**



**Classifier**

# ADVERSARIAL EXAMPLES

“Ox” 85%

“Traffic light” 96%

$$f(x) \rightarrow y$$

$$f(x + \delta) \neq f(x)$$

s.t.

$x + \delta$  looks like  $x$

$$\|\delta\|_p \leq \epsilon$$



$\ell_0$  ↓



$\ell_\infty$  →



only 3% of pixels





# REALISTIC ATTACKS

Sharif et al., 2016




Eykholt et al., 2018




Saadatpanah et al., 2019

Video



0:30


**original**  
Add description


0:30





**adversarial example**  
Add description

Visibility

 **Draft**  
Copyright claim

 **Draft**

The content identified in your video is listed below, along with details and actions.

Content used	Claim type	Impact on the video	Actions
 Tik Tok Keshi		 Video cannot be monetized Ad revenue paid to copyright owner	<a href="#">SELECT ACTION</a> 

CCS'16 Sharif, Bhagavatula, Bauer, Reiter “Accessorize to a Crime: Real and Stealthy Attacks on State-of-the-Art Face Recognition”

CVPR 18 Eykholt, Evtimov, Fernandes, Li, Rahmati, Xiao, Prakash, Kohno, Song “Robust Physical-World Attacks on Deep Learning Visual Classification”

ArXiv 19 Saadatpanah, Shafahi, Goldstein “Adversarial Attacks on Copyright Detection”

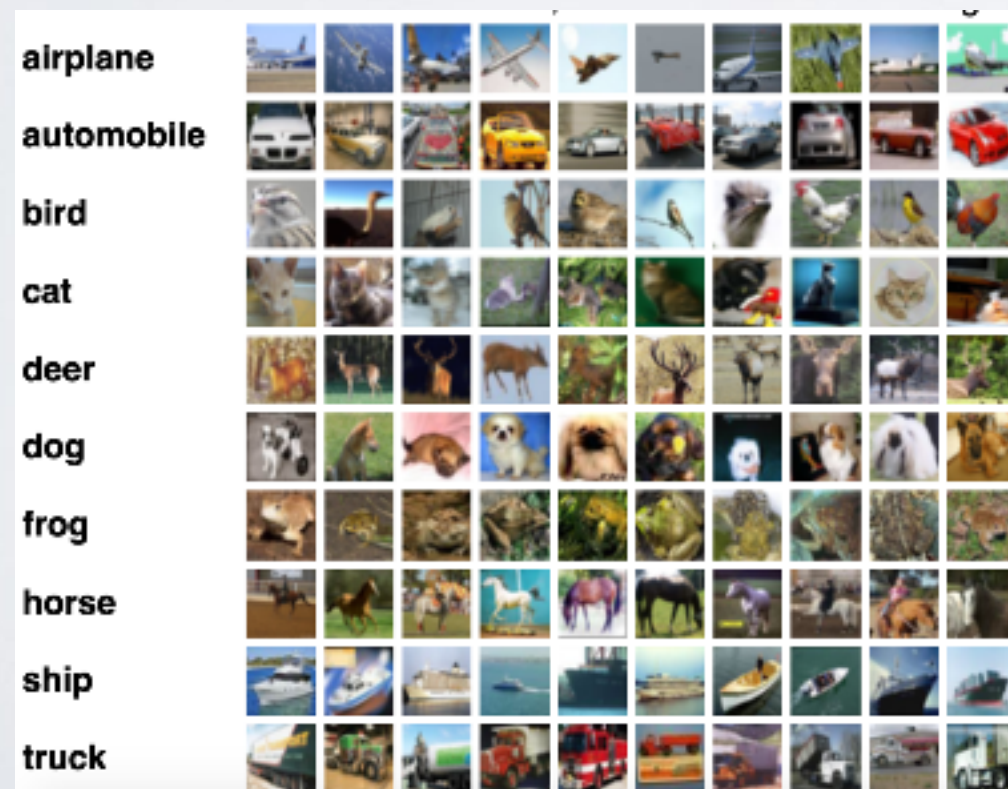
# ROBUSTNESS AGAINST PER-INSTANCE PERTURBATIONS

**Defending against non-targeted per-instance attacks is difficult...**

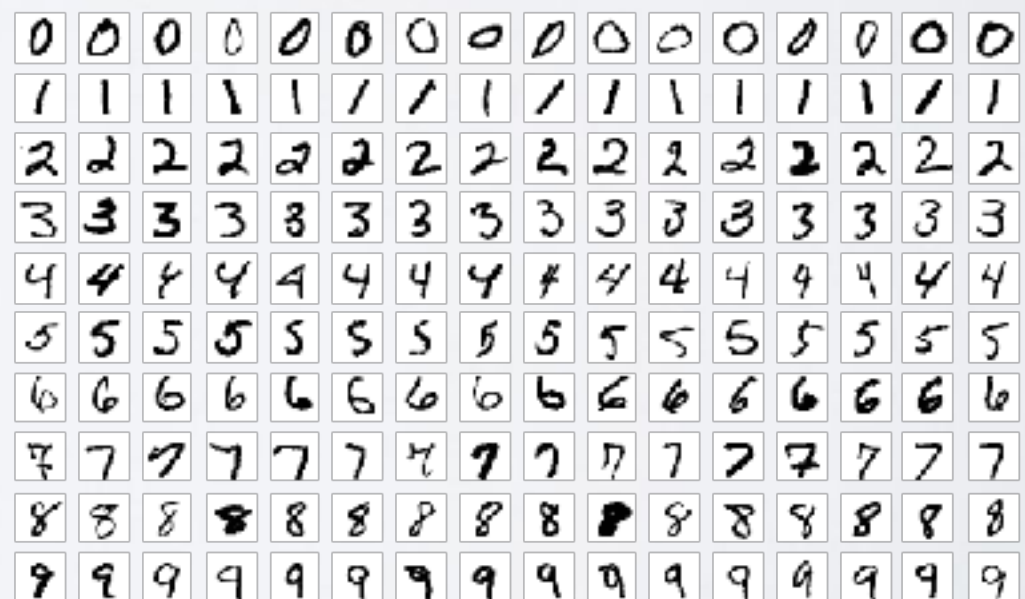
Small  $\epsilon$  is used for p-norm bounded attacks

For larger datasets (ImageNet) defenses focused on random targets

Most studies focus on smaller datasets (CIFAR & MNIST)



CIFAR-10



MNIST

# DEFENDING IS TOUGH

Defense	Defense type	Under which attack	Dataset	Distance	$\mathcal{A}_{\text{nat}}(f)$	$\mathcal{A}_{\text{rob}}(f)$
[BRRG18]	gradient mask	[ACW18]	CIFAR10	0.031 ( $\ell_\infty$ )	-	0%
[MLW <sup>+</sup> 18]	gradient mask	[ACW18]	CIFAR10	0.031 ( $\ell_\infty$ )	-	5%
[DAL <sup>+</sup> 18]	gradient mask	[ACW18]	CIFAR10	0.031 ( $\ell_\infty$ )	-	0%
[SKN <sup>+</sup> 18]	gradient mask	[ACW18]	CIFAR10	0.031 ( $\ell_\infty$ )	-	9%
[NKM17]	gradient mask	[ACW18]	CIFAR10	0.015 ( $\ell_\infty$ )	-	15%
[WSMK18]	robust opt.	FGSM <sup>20</sup> (PGD)	CIFAR10	0.031 ( $\ell_\infty$ )	27.07%	23.54%
[MMS <sup>+</sup> 18]	robust opt.	FGSM <sup>20</sup> (PGD)	CIFAR10	0.031 ( $\ell_\infty$ )	87.30%	<b>47.04%</b>
[ZSLG16]	regularization	FGSM <sup>20</sup> (PGD)	CIFAR10	0.031 ( $\ell_\infty$ )	94.64%	0.15%
[KGB17]	regularization	FGSM <sup>20</sup> (PGD)	CIFAR10	0.031 ( $\ell_\infty$ )	85.25%	45.89%
[RDV17]	regularization	FGSM <sup>20</sup> (PGD)	CIFAR10	0.031 ( $\ell_\infty$ )	95.34%	0%

source: Zhang et. al, 2019

Defense	Dataset	Distance	Accuracy
Buckman et al. (2018)	CIFAR	0.031 ( $\ell_\infty$ )	0%*
Ma et al. (2018)	CIFAR	0.031 ( $\ell_\infty$ )	5%
Guo et al. (2018)	ImageNet	0.005 ( $\ell_2$ )	0%*
Dhillon et al. (2018)	CIFAR	0.031 ( $\ell_\infty$ )	0%
Xie et al. (2018)	ImageNet	0.031 ( $\ell_\infty$ )	0%*
Song et al. (2018)	CIFAR	0.031 ( $\ell_\infty$ )	9%*
Samangouei et al. (2018)	MNIST	0.005 ( $\ell_2$ )	55%**
Madry et al. (2018)	CIFAR	0.031 ( $\ell_\infty$ )	47%
Na et al. (2018)	CIFAR	0.015 ( $\ell_\infty$ )	15%

source: Athalye et. al, 2018

**PGD Adversarial training!**

ICML 18 Athalye, Carlini, Wagner “Obfuscated gradients give a false sense of security”

ICML 19 Zhang, Yu, Jiao, Xing, El Ghaoui, Jordan “Theoretically principled trade-off between robustness and accuracy”



# ADVERSARIAL TRAINING

$$\min_w \max_{\delta_i} \frac{1}{N} \sum_{i=1}^N J(w, x_i + \delta_i)$$

s.t.  $\|\delta_i\|_p \leq \epsilon \quad \forall i \in \{1..N\}$

Original

$\ell_2$ -norm=10

$\ell_\infty$ -norm=0.05

$\ell_0$ -norm=5000 (sparse)



egyptian cat (28%)

traffic light (97%)

traffic light (96%)

traffic light (80%)

image source: Shafahi et. al, 2019

# PGD ADVERSARIAL TRAINING

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**Algorithm 1** Standard Adversarial Training (K-PGD)

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**Require:** Training samples  $X$ , perturbation bound  $\epsilon$ , step size  $\epsilon_s$ , maximization iterations per minimization step  $K$ , and minimization learning rate  $\tau$

```
1: Initialize  $\theta$ 
2: for epoch = 1 ...  $N_{ep}$  do
3:   for minibatch  $B \subset X$  do
4:     Build  $x_{adv}$  for  $x \in B$  with PGD:
5:       Assign a random perturbation
6:        $r \leftarrow U(-\epsilon, \epsilon)$ 
7:        $x_{adv} \leftarrow x + r$ 
8:       for  $k = 1 \dots K$  do
9:          $g_{adv} \leftarrow \nabla_x l(x_{adv}, y, \theta)$ 
10:         $x_{adv} \leftarrow x_{adv} + \epsilon_s \cdot \text{sign}(g_{adv})$ 
11:         $x_{adv} \leftarrow \text{clip}(x_{adv}, x - \epsilon, x + \epsilon)$ 
12:      end for
13:     Update  $\theta$  with stochastic gradient descent:
14:        $g_\theta \leftarrow \mathbb{E}_{(x,y) \in B} [\nabla_\theta l(x_{adv}, y, \theta)]$ 
15:        $\theta \leftarrow \theta - \tau g_\theta$ 
16:   end for
17: end for
```

**Adversarial  
example  
generation**



Madry et. al, 2018

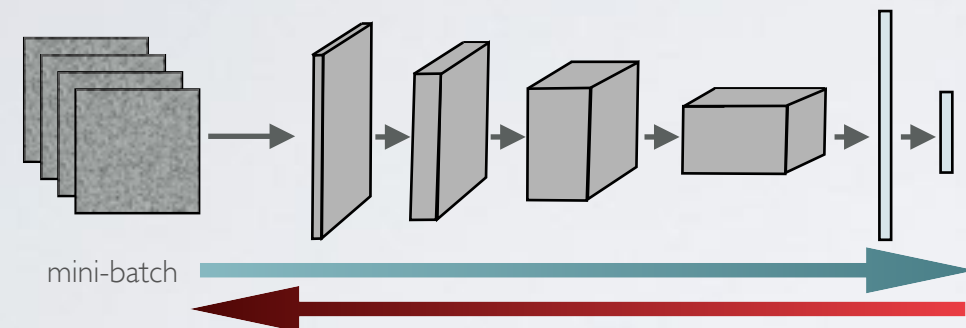
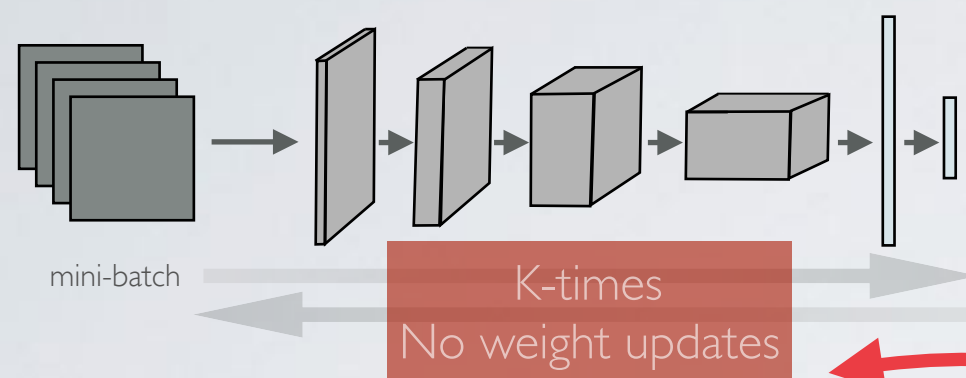


# PGD ADV. TRAINING

K-PGD adversarial training

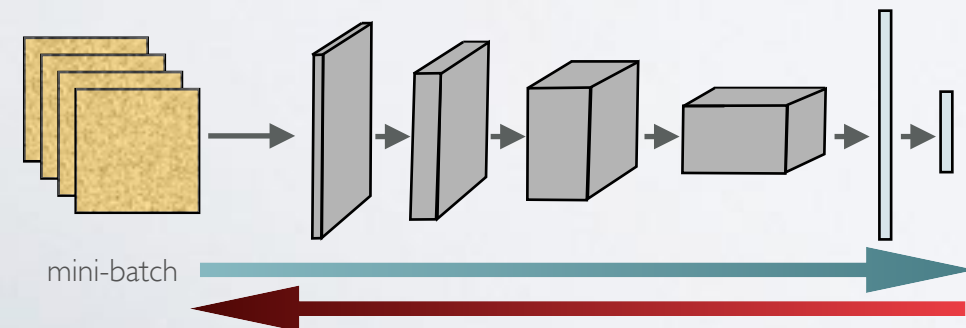
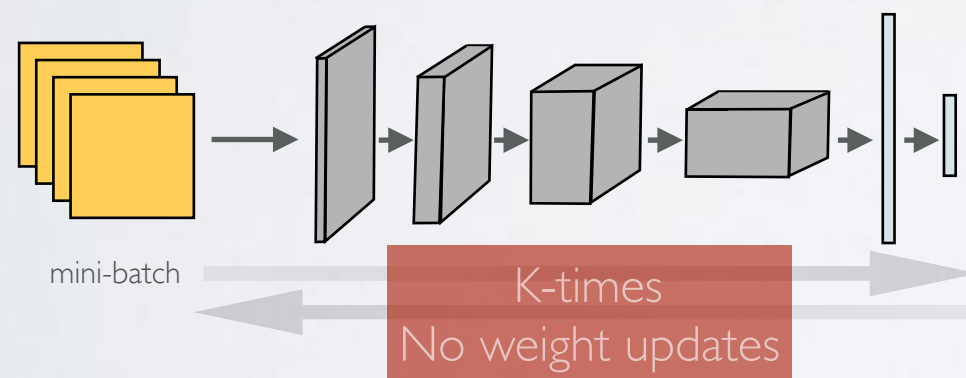
$$\min_w \max_{\delta_i} \frac{1}{N} \sum_{i=1}^N J(w, x_i + \delta_i)$$

First weight update



**Adds a K-factor Overhead:**  
**We perform an additional K**  
**Forward and Backward passes without**  
**updating the network parameters**

Second weight update



# ADVERSARIAL TRAINING WITH PGD REQUIRES MANY FWD/BWD PASSES

Impractical for ImageNet?

Not if you have a lot of compute...

Kannan et al., 2018	<b>53 P100s</b>
Xie et al., 2019	<b>128 V100s</b>
Qin et al., 2019	<b>128 TPUv3</b>



ArXiv 18 Kannan, Kurakin, Goodfellow “Adversarial Logit Pairing”

CVPR 19 Xie, Wu, Maaten, Yuille, He “Feature denoising for improving adversarial robustness”

NeurIPS 19 Qin, Martens, Goyal, Krishnan, Fawzi, De, Stanforth, Kohli “Adversarial Robustness Through Local Linearization”

# ADV. TRAINING FOR FREE!

Free-m adversarial training

First weight update

Second weight update

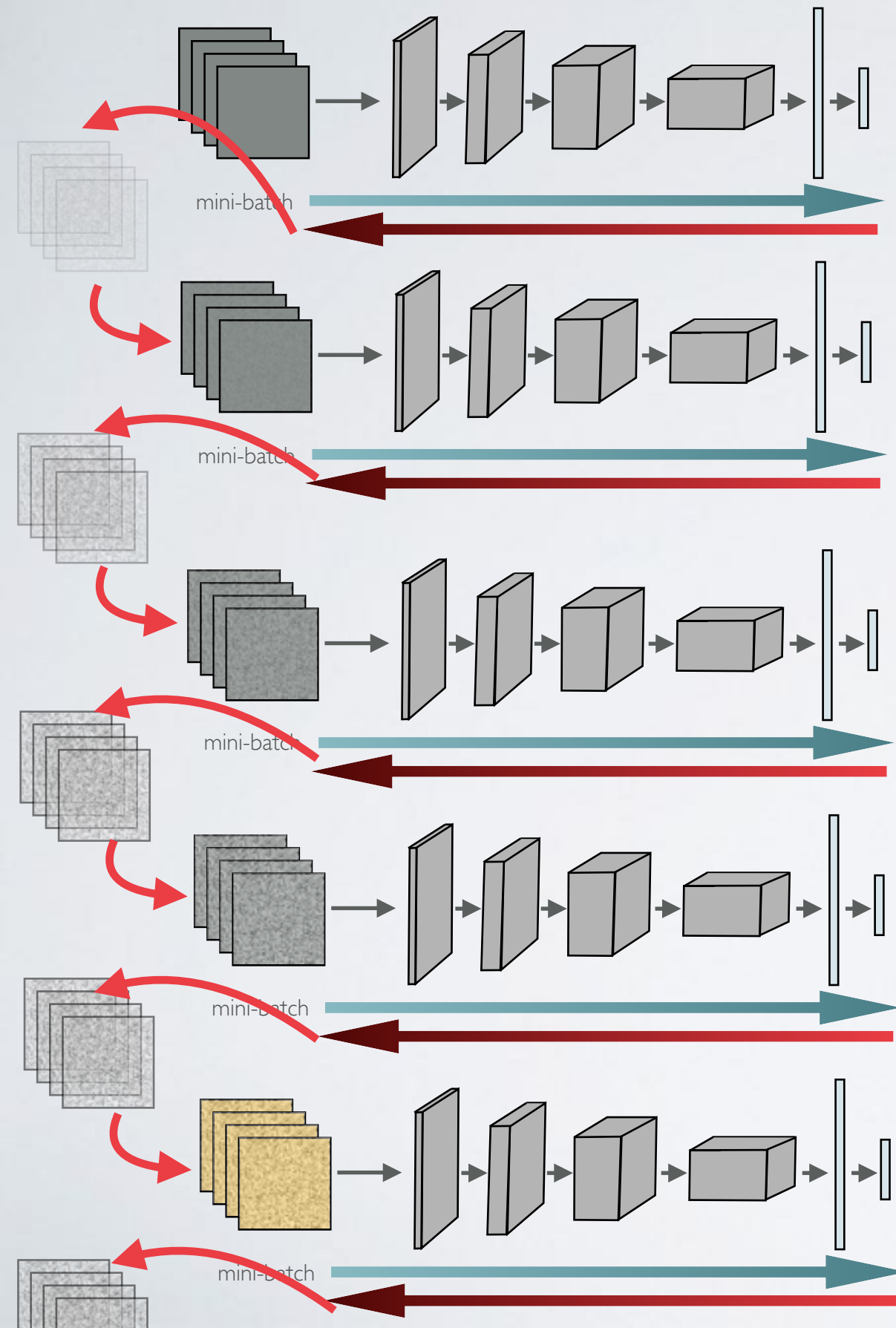
**m[=4] replays  
of the same mini-batch**

Third weight update

Fourth weight update

**Unlike K-PGD training,  
we update the network parameters  
every time we do a back-ward pass**

Fifth weight update





# ADVERSARIAL TRAINING FOR FREE!

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**Algorithm 2** “Free” Adversarial Training (Free- $m$ )

---

**Require:** Training samples  $X$ , perturbation bound  $\epsilon$ , learning rate  $\tau$ , hop steps  $m$

```
1: Initialize  $\theta$ 
2:  $\delta \leftarrow 0$ 
3: for epoch = 1 ...  $N_{ep}/m$  do
4:   for minibatch  $B \subset X$  do
5:     for  $i = 1 \dots m$  do
6:       Update  $\theta$  with stochastic gradient descent
7:        $g_\theta \leftarrow \mathbb{E}_{(x,y) \in B} [\nabla_\theta l(x + \delta, y, \theta)]$ 
8:        $g_{adv} \leftarrow \nabla_x l(x + \delta, y, \theta)$ 
9:        $\theta \leftarrow \theta - \tau g_\theta$ 
10:      Use gradients calculated for the minimization step to update  $\delta$ 
11:       $\delta \leftarrow \delta + \epsilon \cdot \text{sign}(g_{adv})$ 
12:       $\delta \leftarrow \text{clip}(\delta, -\epsilon, \epsilon)$ 
13:    end for
14:  end for
15: end for
```

---

- Update both perturbation and network parameters in one pass
- Replay every mini-batch  $m$  times to simulate PGD training

# ADVERSARIAL TRAINING FOR FREE!

Table 1: Validation accuracy and robustness of CIFAR-10 models trained with various methods.

Training	Evaluated Against					Training Time (minutes)
	Natural Images	PGD-20	PGD-100	CW-100	10 restart PGD-20	
Natural	<b>95.01%</b>	0.00%	0.00%	0.00%	0.00%	<b>780</b>
Free $m = 2$	91.45%	33.92%	33.20%	34.57%	33.41%	816
Free $m = 4$	87.83%	41.15%	40.35%	41.96%	40.73%	800
Free $m = 8$	85.96%	<b>46.82%</b>	<b>46.19%</b>	<b>46.60%</b>	<b>46.33%</b>	785
Free $m = 10$	83.94%	46.31%	45.79%	45.86%	45.94%	785
Madry <i>et al.</i> (7-PGD trained)	87.25%	45.84%	45.29%	46.52%	45.53%	5418

Architecture: WRN 32-10  
No. of iterations = 80k  
batchsize=128  
epsilon=8

  
**Robust against many attacks**

  
**Fast**

# ADV. TRAINING FOR FREE!

Free-m also maintains important valuable properties of PGD adversarially trained models

natural



PGD-7



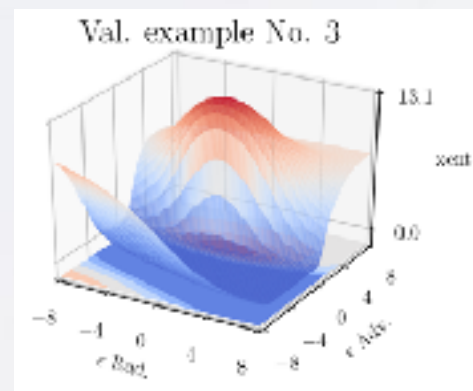
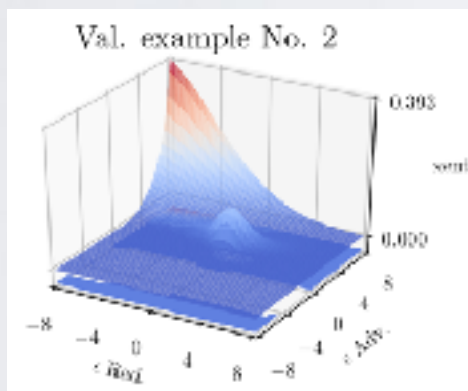
Free-8



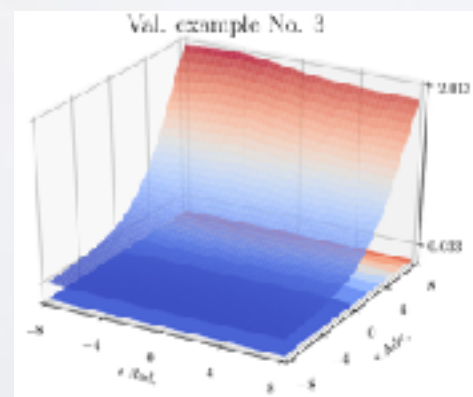
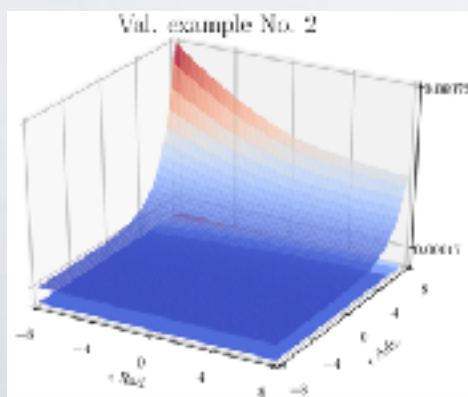
Interpretable gradients



natural



Free-8



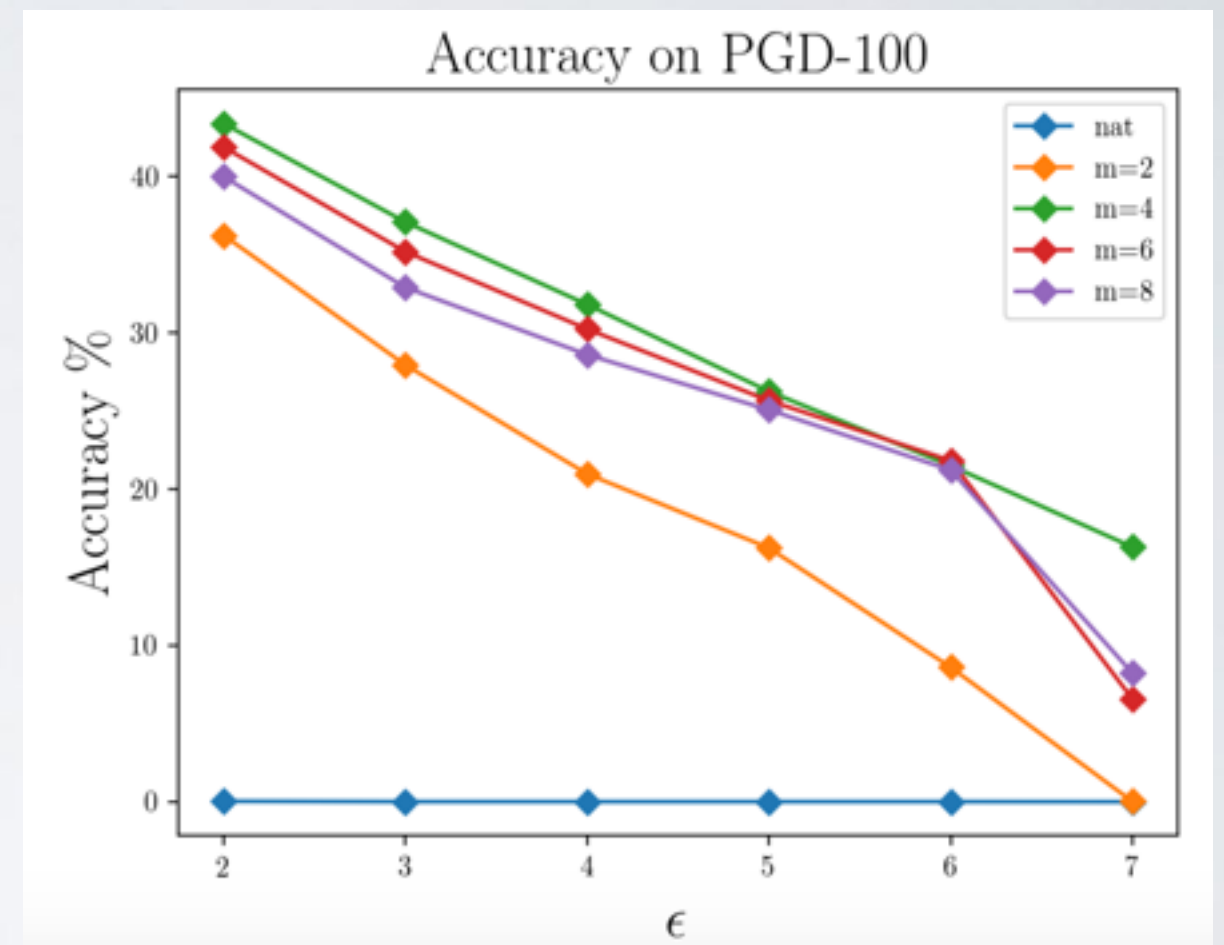
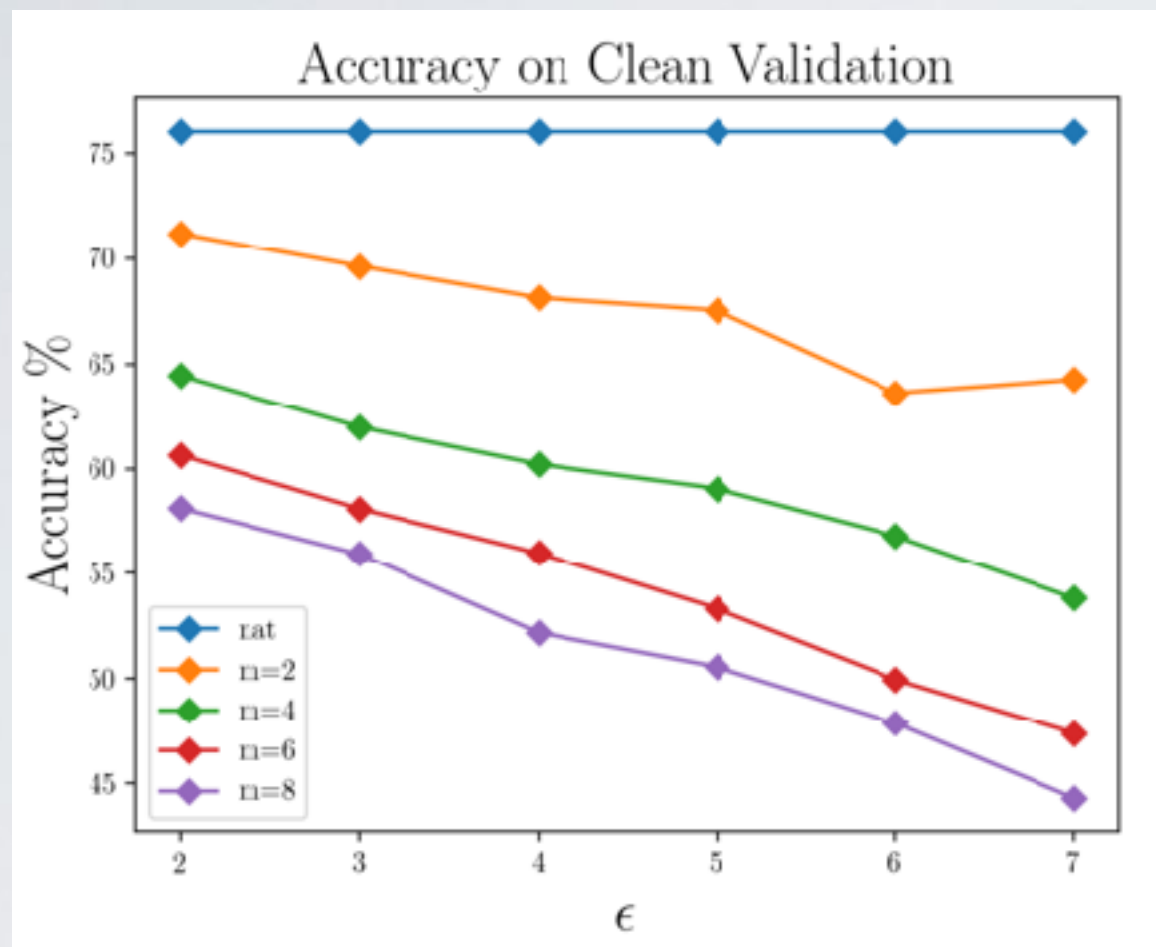
Smooth and flattened loss surface  
compared to naturally trained models





# ADV.TRAINING FOR FREE!

ImageNet (ResNet-50)

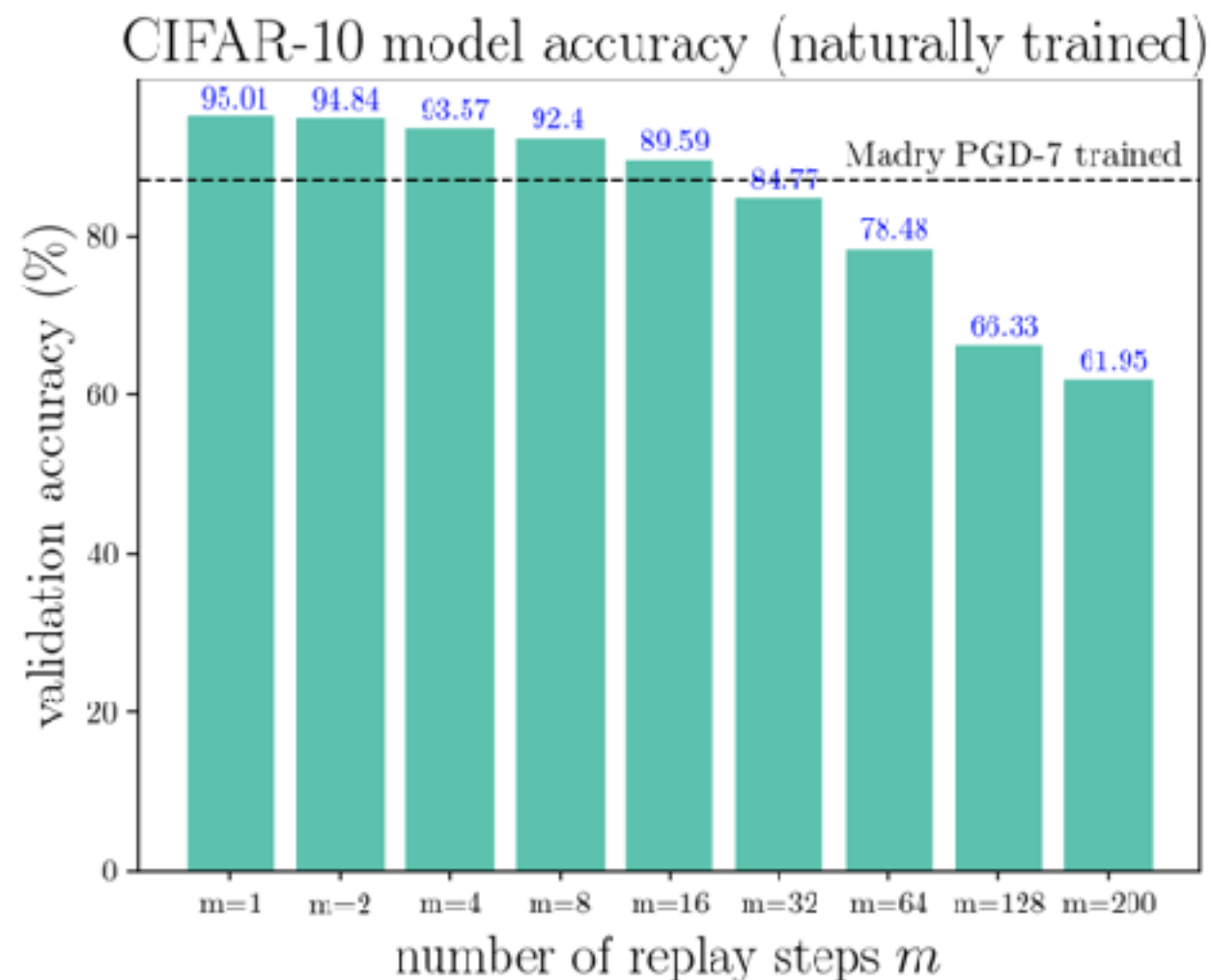


Free-4  
(epsilon=4)  
batchsize=256

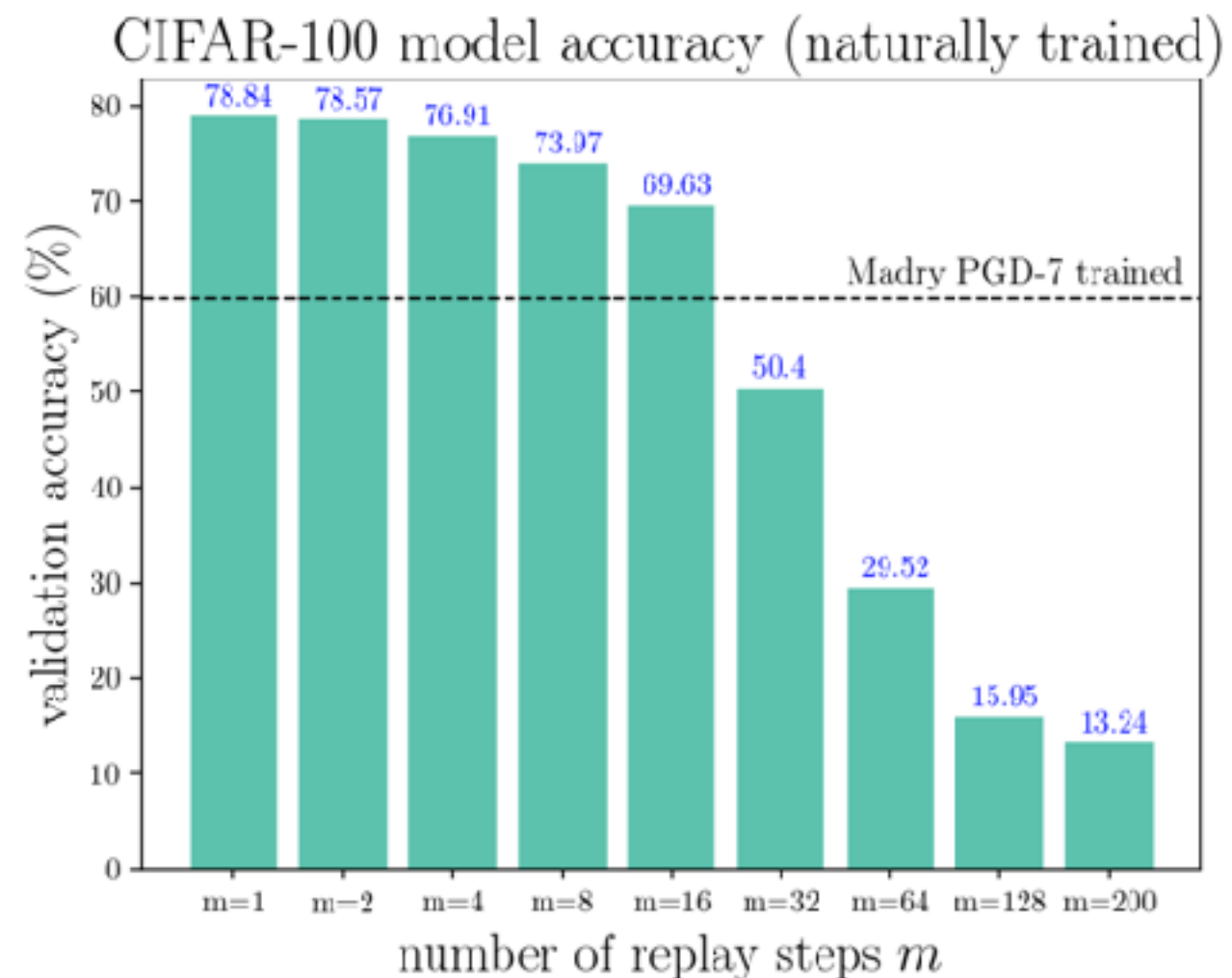
Architecture	Evaluated Against			
	Natural Images	PGD-10	PGD-50	PGD-100
ResNet-50	60.206%	32.768%	31.878%	31.816%
ResNet-101	63.340%	35.388%	34.402%	34.328%
ResNet-152	64.446%	36.992%	36.044%	35.994%

# ADVERSARIAL TRAINING FOR FREE!

How much replaying a mini-batch hurts...



(a) CIFAR-10 sensitivity to  $m$



(b) CIFAR-100 sensitivity to  $m$

Architecture: WRN 32-10

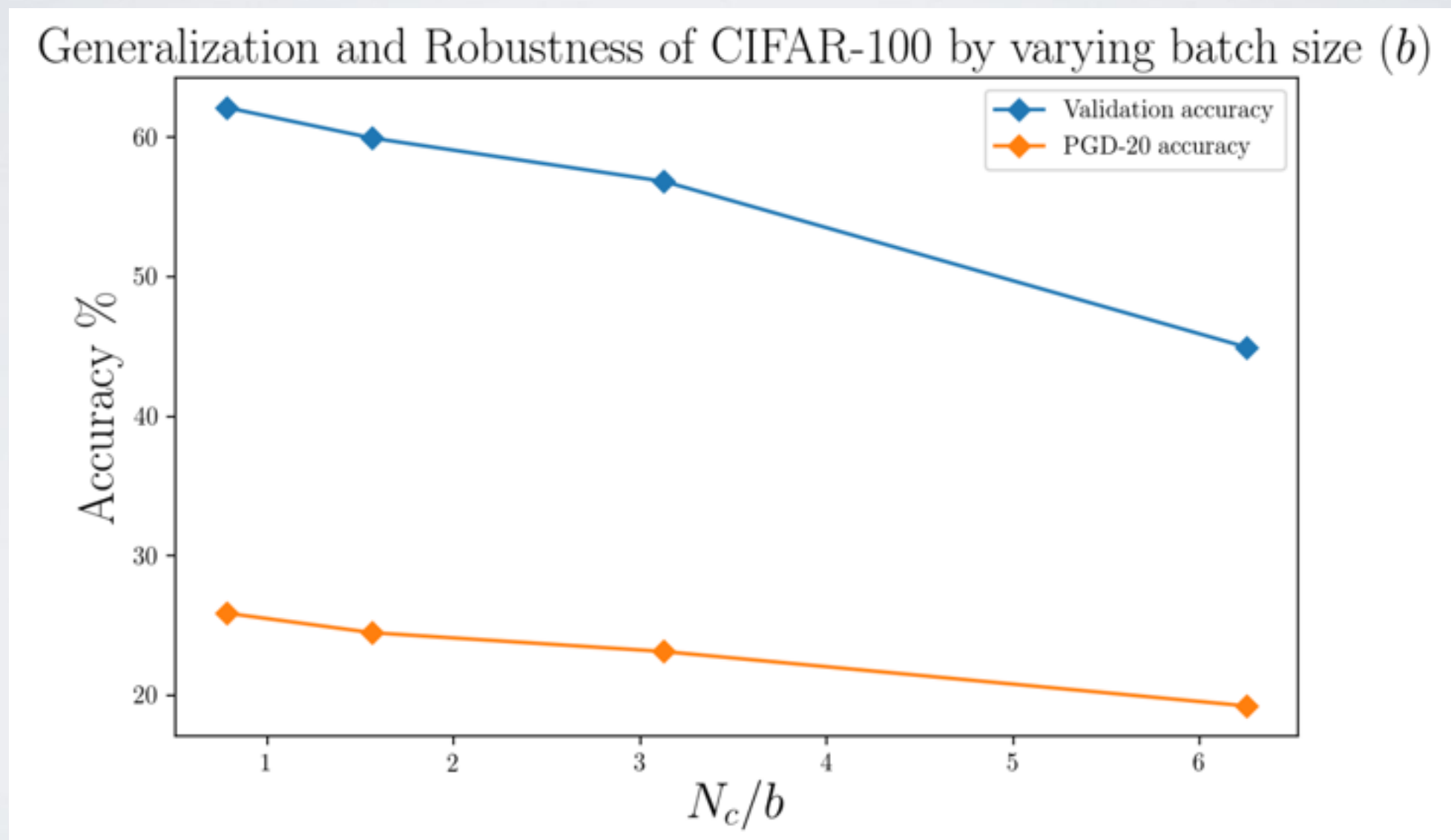
No. of iterations = 80k

batchsize=128

NeurIPS 19 Shafahi, Najibi, Ghiasi, Xu, Dickerson, Studer, Davis, Taylor, Goldstein “Adversarial Training for Free!”

# ADVERSARIAL TRAINING FOR FREE!

Could compensate some of the negative effects of replay by increasing batch-size



Our ImageNet result were with a batch-size of 256 ...  $N_c/b = \frac{1000}{256} = 3.91$



# FREE CODE!



**Pytorch**



**ImageNet**

**Tensorflow**



**CIFAR**

THANK YOU!