

## Properties of Criteria

- Program-based
- To recognize a good adequacy criteria
- And to discard poor choices
- Objective, well-defined properties

## 1. Applicability Property

- For every program, there exists an adequate test set
- Every program must be adequately testable

## Criteria

- Statement coverage
- Branch coverage
- Path coverage
- Def-use coverage
- One cannot algorithmically determine whether more testing must be performed

## Exhaustive test set

- If all representable points of the specification's domain have been tested
  - Set of all inputs for which the program *should* produce the desired output
- Exhaustive test set is **surely** adequate
  - No matter what criterion is used
- There *can* be no additional testing possible
- Practical if domain is small
- A criterion that *always* requires an exhaustive test set is unacceptable

## 2. Non-exhaustive Applicability

- There is a program P and (not exhaustive) test set T such that P is adequately tested by T

## 3. Monotonicity

- Once a program has been adequately tested, running some additional test cases cannot cause the program to be deemed inadequately tested
- If T is adequate for P, and  $T \subseteq T'$  then T' is adequate for P
- "Stop when we find less than 50 errors per 1000 hours of testing"
- Note
  - An exhaustive test set is always adequate

#### 4. Inadequate empty set

- If no testing has been performed, then the program cannot be considered adequately tested
- The empty set is not an adequate test set for any program

#### Program Equivalence

- $P \equiv Q$ 
  - P is equivalent to Q
- For  $x$  (input vector) in the specification's domain
- $P(x) = Q(x)$ 
  - Results of P and Q on every  $x$  are same

#### 5. Antiextensionality

- There are programs P and Q, such that  $P \equiv Q$ , and a test set T is adequate for P but T is not adequate for Q
- Remember
  - Program-based
- Semantic equivalence of two programs does not necessarily imply that they be tested the same way
- Program-based testing should consider the implementation, not the functions computed

#### Syntactic Closeness

- Two programs have the same shape
  - If one can be transformed into another by applying the following transformations, any number of times
    - Replace relational operator  $r_1$  in a predicate with relational operator  $r_2$
    - Replace constant  $c_1$  in a predicate or assignment statement with constant  $c_2$
    - Replace arithmetic operator  $a_1$  in an assignment statement with arithmetic operator  $a_2$

#### 6. General Multiple Change

- There are programs P and Q, which are the same shape, and a test set T is adequate for P but T is not adequate for Q
- Syntactic closeness of programs does not imply that they should be tested the same way

#### Program Decomposition

- A component Q of a program P is any contiguous sequence of statements of P

## 7. Antidecomposition

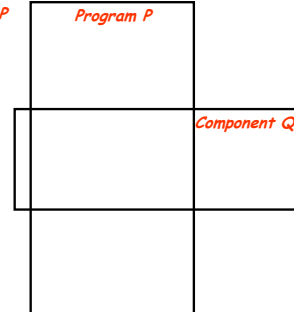
- There exists a program P, and
- component Q,
- such that test set T is adequate for P,
- T' is the set of vectors of values that variables can assume on entrance to Q for some t in T, and
- T' is not adequate for Q

## Explanation

T is adequate for P

$t \in T$

T' is not adequate for Q



## Explanation

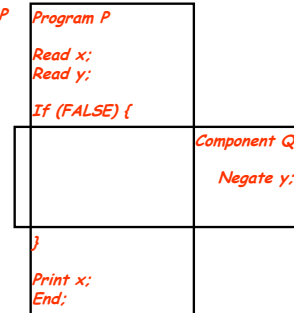
- Although a program has been adequately tested, it does not necessarily imply that each of its component pieces has been properly tested
- A routine that has been adequately tested in some environment or context has not necessarily been tested for other environments
- Even though P appears to be more complicated than Q, (P syntactically contains Q), semantically, Q may be more complex than P

## Explanation

T is adequate for P

$t \in T$

T' is not adequate for Q

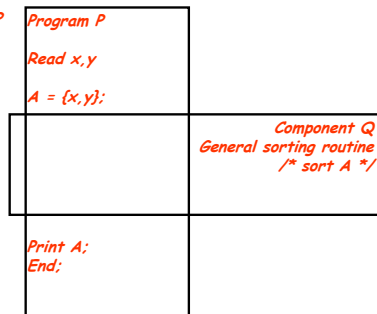


## Explanation

T is adequate for P

$t \in T$

T' is not adequate for Q



## Criteria

- Statement coverage
- Branch coverage
- Antidecomposition property rules out criteria that do not recognize that the context of a piece of code is important

## Program Composition

- Assume a structured programming language
  - Programs are single-entry/single-exit
  - All input statements appear at the start of the program
  - All output statements appear at the end of the program
- Programs P and Q
  - Using the same set of identifiers
  - Remove all output statements of P
  - Remove all input statements of Q
- P;Q is the composed program

## 8. Anticomposition

- There exist programs P and Q, and
- test set T,
- such that T is adequate for P, and
- the set of vectors of values that variables can assume on entrance to Q for inputs in T is adequate for Q, but
- T is not adequate for P;Q

## Criteria

- Statement coverage
- Branch coverage
- Anticomposition property eliminates criteria that do not have provision for testing the interaction of program pieces

## Gödel Numbering

- Definition
  - A unique numerical value for each program, such that the program can be algorithmically retrieved from this value
- For a program P with Gödel number p
  - A test set T is Gödel adequate for P if  $p \in T$
- Any test set T that contains a program P's Gödel number is adequate for P

## Examining Gödel Adequacy

- Gödel adequacy has nothing to do with a program's semantics, syntax or specifications
- Every program will always have an adequate test set of size one
- Does this criterion satisfy all the properties that we have discussed?
- Do you think that this criterion is useful?

## Program Renaming

- P is a *renaming* of Q if
  - P is identical to Q, except
  - All instances of an identifier  $x_i$  of Q have been replaced by an identifier  $x_j$  where  $x_j$  does not appear in Q, or
  - If there exists a sequence  $Q = P_1, P_2, P_3, \dots, P_n = P$ , where
    - $P_{i+1}$  is a renaming of  $P_i$  for  $i = 1, \dots, n-1$

## 9. Renaming Property

- Let  $P$  be a renaming of  $Q$
- Test set  $T$  is adequate for  $P$  iff  $T$  is adequate for  $Q$
- Intuitively, an “inessential” change in a program, such as changing variable names, should not change the test data required to adequately test the program
- Gödel adequacy does not satisfy this property!!

## Canonical Representation

- Given a Program  $P$  with  $k$  variables
  - Obtain its canonical representation by
  - Renaming variables using the set  $\{x_1, x_2, \dots, x_k\}$  where  $x_1$  replaces the first variable used in the program and  $x_k$  replaces the  $k^{\text{th}}$  variable used;  $x_i$  replaces the  $i^{\text{th}}$  variable used

## Gödel-class Numbering

- Definition
  - A unique numerical value for each program's canonical form, such that the it can be algorithmically retrieved from this value
- For a program  $P$  with Gödel-class number  $p$ 
  - A test set  $T$  is Gödel-class adequate for  $P$  if  $p \in T$
- Any test set  $T$  that contains a program  $P$ 's Gödel-class number is adequate for  $P$
- Does it satisfy Renaming Property?
- And all other 8 properties?

## 10. Statement Coverage

- If  $T$  is adequate for  $P$ , then  $T$  causes every executable statement of  $P$  to be executed