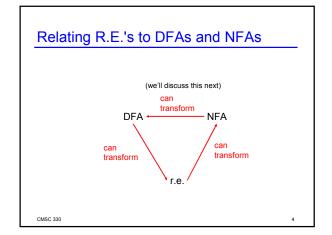
# CMSC 330: Organization of Programming Languages

Theory of Regular Expressions NFAs  $\rightarrow$  DFAs



## Reminders

- Homework 1 due Sep. 20
- Project 1 due Sep. 24
- Exam 1 on Sep. 25
  - Study this weekend!
- Project 2 given out on Sep. 24.
  - Start soon!

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## **Reduction Complexity**

- · Regular expression to NFA reduction:
  - -O(n)
- · NFA to DFA reduction
  - Intuition: Build DFA where each DFA state represents a set of NFA states
  - How many states could there be in the DFA?
  - Given NFA with n states, DFA may have 2<sup>n</sup> states
  - Not so good, since DFAs are what we can implement easily

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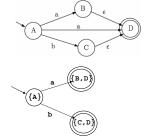
#### Review

- How are DFAs and NFAs different?
- When does an NFA accept a string?
- How do we convert from a regular expression to an NFA?
- What is the  $\epsilon$ -closure of a state?

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NFA → DFA reduction

Example:

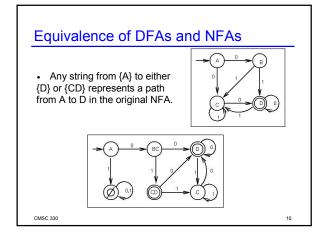


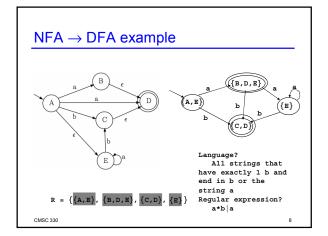
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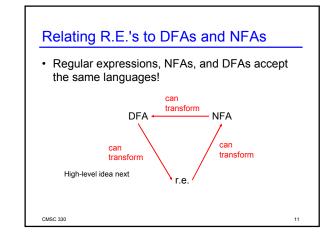
## NFA → DFA reduction Algorithm

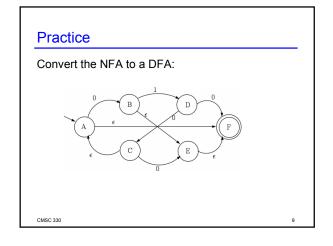
- Let  $r_0$  be the  $\epsilon$ -closure of  $q_0$ , add it to R
- While there is an unmarked state ri in R
  - Mark r<sub>i</sub>
  - For each a  $\in \Sigma$ 
    - Let S = {s | q  $\in$  r, and for {q, a, B}  $\in \delta,$  s  $\in B$ }
    - Let E = ε-closure(S)
    - If E∉R
    - R = E ∪ R
    - $\delta = \delta \cup \{ri, a, E\}$
- Let  $r_f = \{r_i \mid \exists \ s \in r_i \text{ with } s \in q_f\}$

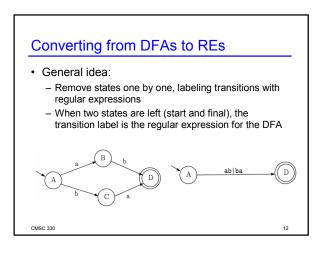
Notes: Let Q be the set of states for the NFA and R be the set of states for the DFA. All states are unmarked at creation.  $^{\text{CMSC}\,330}$ 











## Relating R.E's to DFAs and NFAs

- · Why do we want to convert between these?
  - Can make it easier to express ideas
  - Can be easier to implement

## Run Time of Algorithm

- Given a string s, how long does algorithm take to decide whether s is accepted?
  - Assume we can compute  $\delta(q0, c)$  in constant time
  - Then the time per string s to determine acceptance is O(|s|)
  - Can't get much faster!
- · But recall that constructing the DFA from the regular expression A may take O(2|A|) time
  - But this is usually not the case in practice
- So there's the initial overhead, but then accepting strings is fast

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#### Implementing DFAs

It's easy to build a program which mimics a DFA



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```
switch (cur state) {
case 0: switch (symbol) {
case '0': cur_state = 0; break;
case '1': cur_state = 1; break;
case '\n': printf("rejected)n"); return 0;
default: printf("rejected\n"); return 0;
 default: printf("unknown state; I'm confused\n");
break;
```

#### Regular Expressions in Practice

- Regular expressions are typically "compiled" into tables for the generic algorithm
  - Can think of this as a simple byte code interpreter
  - But really just a representation of  $(\Sigma, Q_A, q_A, \{f_A\}, \delta_A)$ , the components of the DFA produced from the r.e.
- Regular expression implementations often have extra constructs that are non-regular
  - I.e., can accept more than the regular languages
  - Can be useful in certain cases
  - Disadvantages: nonstandard, plus can have higher complexity

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## Implementing DFAs (Alternative)

Alternatively, use generic table-driven DFA

given components ( $\Sigma$ , Q, q<sub>0</sub>, F,  $\delta$ ) of a DFA: let q = q while (there exists another symbol s of the input string)  $a := \delta(a, s)$ : if q∈F then accept else reject

- q is just an integer
- Represent o using arrays or hash tables
- Represent F as a set

# Considering Ruby Again

- Interpreted
- Implicit declarations
- Dynamically typed
  - These three make it quick to write small programs
- Built-in regular expressions and easy string manipulation
  - · This and the three above are the hallmark of scripting languages
- Object-oriented
  - · Everything (!) is an object
- Code blocks
  - · Easy higher-order programming!
  - · Get ready for a lot more of this...

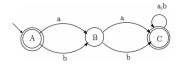
## Other Scripting Languages

- Perl and Python are also popular scripting languages
  - Also are interpreted, use implicit declarations and dynamic typing, have easy string manipulation
  - Both include optional "compilation" for speed of loading/execution
- · Will look fairly familiar to you after Ruby
  - Lots of the same core ideas
  - All three have their proponents and detractors
  - Use whichever one you like best

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**Complement Steps** 

- · Add implicit transitions to a dead state
- Change every accepting state to a nonaccepting state and every non-accepting state to an accepting state
- · Note: this only works with DFAs Why?



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#### **Practice**

Convert to a DFA:





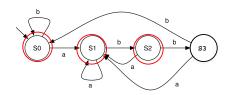
Convert to an NFA and then to a DFA:

- (0|1)\*11|0\*
- · strings of alternating 0 and 1
- aba\*|(ba|b)

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**Practice** 

Make the DFA which accepts the complement of the language accepted by the DFA below.

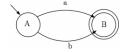


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## Complement of DFA

Given a DFA accepting language L, how can we create a DFA accepting its complement? (the alphabet = {a,b})



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#### **Practice**

- Make the DFA which accepts all strings with a substring of 330
- · Take the complement of this DFA

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