

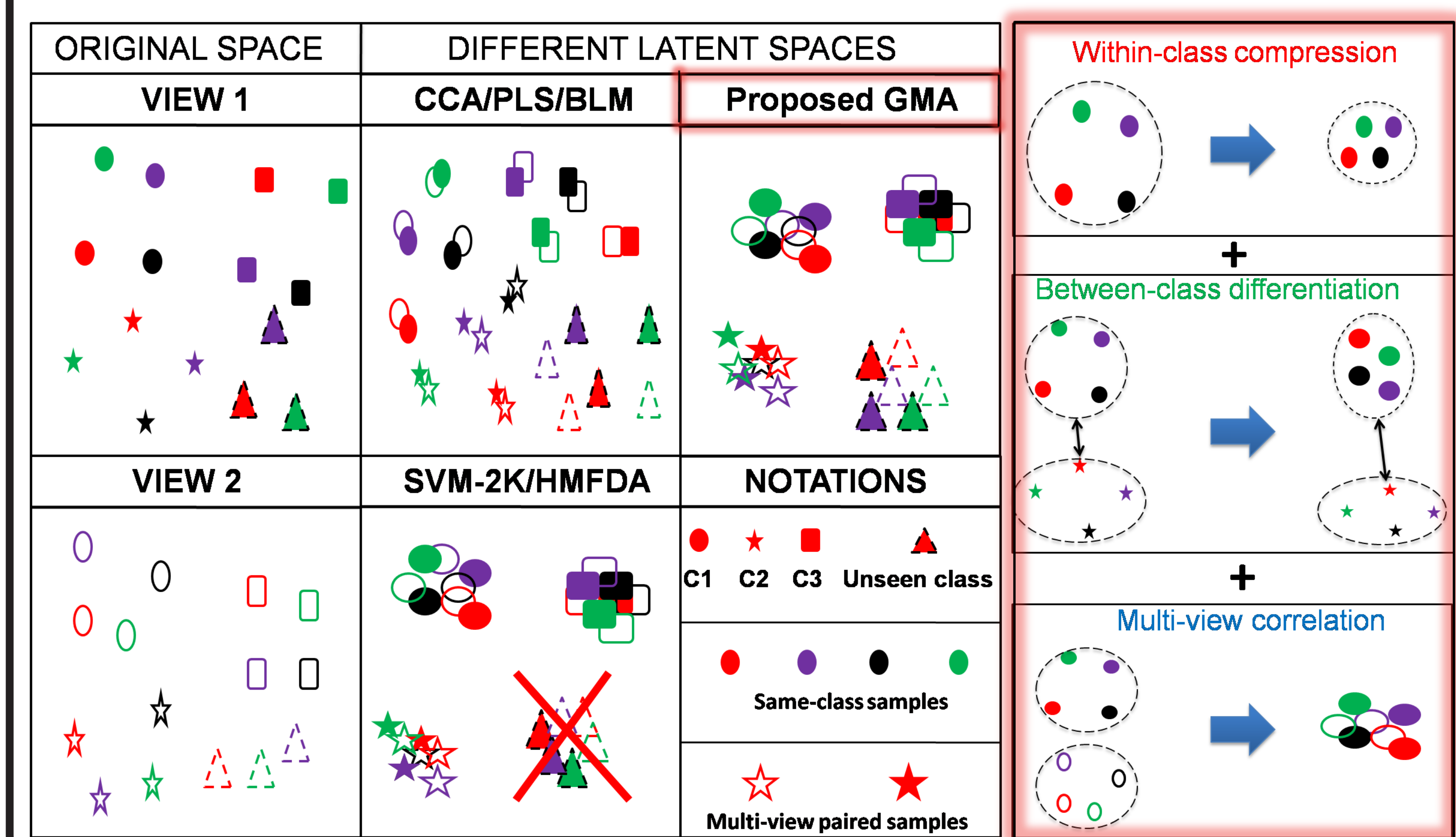
# Generalized Multiview Analysis: A Discriminative Latent Space

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## Contribution

We introduce a multi-view, supervised, domain independent, generalizable to unseen classes and kernelizable mapping to latent space to facilitate multi-view classification and retrieval. Our method has a close-form solution. We show significant improvements over CCA and other domain dependent approaches.

## Compression + Discrimination + Correlation = GMA



## Mathematical Formulation

**CCA:**  $\operatorname{argmax}_{v_1, v_2} v_1^T X_1 X_2^T v_2$  s.t.  $v_1^T X_1 X_1^T v_1 = v_2^T X_2 X_2^T v_2 = 1$   
**CCA+Compression:**  $\operatorname{argmax}_{v_1, v_2} v_1^T X_1 X_2^T v_2$  s.t.  $v_1^T B_1 v_1 = v_2^T B_2 v_2 = 1$   
 $B_i$  is Within-class variance: LDA, MFA, LPP and so on  
**Convex relaxation:**  $\operatorname{argmax}_{v_1, v_2} v_1^T X_1 X_2^T v_2$  s.t.  $v_1^T B_1 v_1 + \alpha v_2^T B_2 v_2 = 1$   
**GMA:**  $\operatorname{argmax}_{v_1, v_2} v_1^T A_1 v_1 + \mu v_2^T A_2 v_2 + \beta v_1^T Z_1 Z_2^T v_2$  s.t.  $v_1^T B_1 v_1 + \alpha v_2^T B_2 v_2 = 1$   
 $Z_i$  are exemplars in view  $i$  and  $A_i$  is Between-class variance: LDA, MFA and so on  
 Make the Lagrangian > differentiate and equate to 0 > solve eigen-value problem :)

**Closed form solution:**

$$\begin{bmatrix} A_1 & \beta Z_1 Z_2^T \\ \beta Z_2 Z_1^T & \mu A_2 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = \begin{bmatrix} B_1 & 0 \\ 0 & \alpha B_2 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix}$$

### Unified view and supervised extensions under GMA

**GMPCA:**  $A_i = X_i X_i^T / N_i, B_i = I, Z_i = X_i$ ; **BLM:**  $A_i = X_i X_i^T / N_i, B_i = I, Z_i = X_i$   
**CCA:**  $A_i = 0, B_i = X_i X_i^T, Z_i = X_i$ ; **PLS:**  $A_i = 0, B_i = I, Z_i = X_i$   
**GMLDA:**  $A_i = S_i^B, B_i = S_i^W, Z_i = M_i$  or  $X_i$ , where  $S^W / S^B$  are Within/Between-class scatter matrices and  $M_i$  is the class mean matrix for view  $i$

## Mathematical Formulation continued..

**GMMFA:**  $A_i = S_{(B)}^i, B_i = S_{(W)}^i, Z_i = X_i$ , where  $S_{(B/W)}^{kk} = \sum_{kl, k \neq l} W_{(b/w)i}^{kl}$ . The *within class compression* or *intrinsic graph-*  
 $W_{wi}^{kl} = \begin{cases} 1 & : k \in R_i^{k1}(l) \text{ or } l \in R_i^{k1}(k) \\ 0 & : \text{otherwise} \end{cases}$ , where  $R_i^{k1}(l)$  indicates the index set of the  $k1$  nearest neighbors of the sample  $x_i^l$  in the same class. The *between class separation* or *penalty graph-*  $W_{bi}^{kl} = \begin{cases} 1 & : (k, l) \in P_i^{k2}(c_l) \text{ or } (k, l) \in P_i^{k2}(c_k) \\ 0 & : \text{otherwise} \end{cases}$ , where  $P_i^{k2}(l)$  is a set of data pairs that are the  $k2$  nearest pairs among the set  $\{(k, l) : k \text{ and } l \text{ are not in the same class}\}$ .

## Algorithmic view of the overall framework

- Step 1: Input multi-view paired data  $X_i$  with label/similarity information.
- Step 2: Learn projection directions  $v_i$  using GMA.
- Step 3: Project  $X_i$  to latent space using  $v_i$ .
- Step 4: Use k-NN matching or learn a classifier in the latent space.

## Experimental Results

### MultiPIE pose and lighting invariant face recognition

Manually annotated fiducial points for cropping are publicly available<sup>1</sup>, simple intensity used as feature.  
**Mode 1- Training:** 129 subjects, 5 lighting; **Testing:** Same 129 subjects, 18 lightings, frontal pose gallery in illum 7.  
**Mode 2- Training:** 129 subjects, 5 lighting; **Testing:** Different 120 subjects, 18 lightings, frontal pose gallery in illum 7.

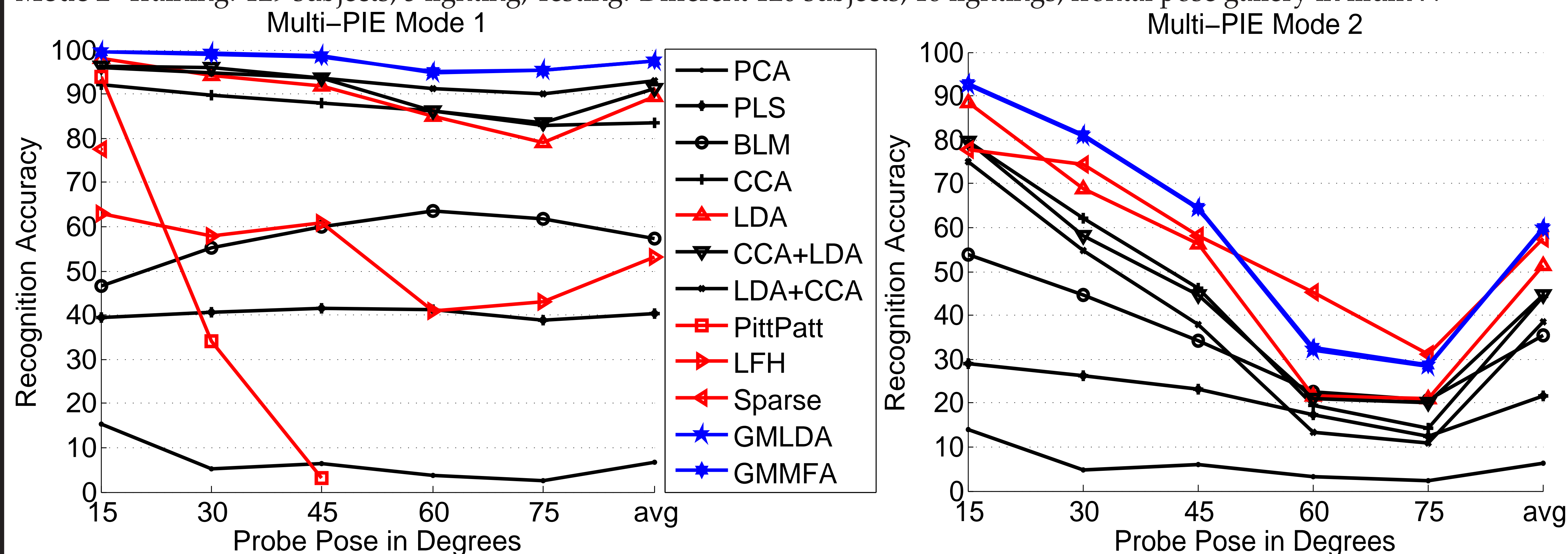


Fig 1 Recognition accuracy for MultiPIE. Red curves indicate domain dependent methods under multi-view setting.

### Text-Image retrieval

**Wikipedia text-image data:** 10 classes, 2173/693 training/testing, publicly available features<sup>2</sup>  
**Pascal image-tag data:** 20 classes, 2808/2841 training/testing, publicly available features<sup>3</sup>

Query	Wikipedia Dataset						Pascal Dataset					
	Others					Proposed	Others					Proposed
	PLS	BLM	CCA	SM	SCM	GMMFA	GMLDA	KPLS	KCCA	KGMLDA	KGMMFA	
Image	0.207	0.237	0.182	0.225	<b>0.277</b>	0.264	0.272	0.279	0.298	0.421	<b>0.427</b>	
Text	0.192	0.144	0.209	0.223	0.226	0.231	<b>0.232</b>	0.232	0.269	0.328	0.339	
Average	0.199	0.191	0.196	0.224	<b>0.252</b>	0.248	<b>0.253</b>	0.256	0.283	0.375	<b>0.383</b>	

<sup>1</sup> [http://www.umiacs.umd.edu/~bhokaal/data/FERET\\_MultiPIE\\_fiducials.tar](http://www.umiacs.umd.edu/~bhokaal/data/FERET_MultiPIE_fiducials.tar)

<sup>2</sup> <http://www.svcl.ucsd.edu/projects/crossmodal/> <sup>3</sup> <http://www.cs.utexas.edu/~grauman/research/datasets.html>