

**Honors HW03. Morally DUE Mon Feb 28**

In this HW Alice and Bob are doing Diffie Hellman with  $p = 47$  and  $g = 5$ . You can verify that  $g$  IS a generator (you do not have to, but you could).

1. (35 points) Alice uses  $a = 10$  and Bob uses  $b = 11$ . What is the shared secret key? Express as a number in  $\{0, \dots, 46\}$
2. (35 points) Alice uses  $a = 11$  and Bob uses  $b = 10$ . What is the shared secret key? Express as a number in  $\{0, \dots, 46\}$
3. (30 points) If you did the problem correctly the last two answers were the same. Prove the following theorem:

**Thm** Let  $p$  be a prime and  $g$  be a generator. Let  $a, b \in \{0, \dots, p-1\}$ . Let  $s_{a,b}$  be the shared secret key if Alice uses  $a$  and Bob uses  $b$ . Show that  $s_{a,b} = s_{b,a}$ .