

CMSC/MATH 858R Homework 3
Morally Due TUESDAY Feb 25 at 3:30PM.

1. (0 points) What is your name? When is the midterm? By what day must you tell Dr. Gasarch you can't make the midterm? (While this problem is 0 points, if you miss the midterm and do not tell Dr. Gasarch, you will get -100 on every single homework problem 1). When is the final?

2. (45 points) Let (X, \preceq) be a well quasi order. Let $2^{\text{fin}X}$ be the set of FINITE subsets of X . We DEFINE an order \preceq_{BILL} on $2^{\text{fin}X}$:

$A \preceq_{\text{BILL}} B$ if there is an injection f from A to B such that $x \preceq f(x)$ for all x .

($\emptyset \preceq_{\text{BILL}} B$ is always true: use the empty function and the condition holds vacuously.)

Show that $(2^{\text{fin}X}, \preceq_{\text{BILL}})$ is a well quasi order.

(NOTE- You may use the fact, proven in class, that well-quasi orders are closed under cross product)

3. (45 points) Let $TREE$ be the set of trees. We define $T \preceq_{\text{CLYDE}} T'$ if T is a minor of T' (recall that T is a minor of T' if you can get T by removing vertices, removing edges, and contracting edges from T')

Show that $TREE$ under \preceq_{CLYDE} is a wqo.

HINT: You will need to use the theorem you proved in problem 2 of this homework. As an additional hint, your proof should begin like this:

Assume, BWOC that the set of trees under minor is NOT a wqo.

Let T_1, T_2, \dots be a MINIMAL BAD SEQUENCE defined in some fashion (you figure it out).

None of the trees is the empty tree, so they all have a root.

Assume the root of T_i has degree d_i . For each T_i remove the root to obtain d_i trees $T_{i,1}, \dots, T_{i,d_i}$

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4. (10 points) Listen to the following songs all set to the tune of Coolio's *Gangsta Paradise*

- *Gangsta Paradise* (not math): <https://www.youtube.com/watch?v=fP076Jlnz6c>
- *Mathematics paradise* by Klein Four: https://www.youtube.com/watch?v=ncUm362M_gc
LYRICS: <https://genius.com/The-klein-four-mathematics-paradise-lyrics>
- *Mathematics Paradise* diff song entirely, not by Klein four: <https://www.youtube.com/watch?v=nskSfmeCFic>
- *Amish Paradise* (not math): <https://www.youtube.com/watch?v=10fZLb33uCg>

Which math version is your favorite? Is it better than the other math songs we have heard so far?