

Homework 9, Morally Due Tue May 5, 2020, 3:30PM
COURSE WEBSITE: <http://www.cs.umd.edu/~gasarch/858/S18.html>
THIS HW IS ONE PAGE LONG!!!!!!!!!!!!!!

1. (0 points) What is your name? Write it clearly.
2. (50 points) In this problem you may assume that, for all c , there exists $N = N(c)$ such that for all c -colorings of $[N] \times [N]$ there exists a monochromatic square.

Show that there exists M such that, for all 2-colorings of $[M] \times [M]$, there exists five points that are the same color of the following form:

(x, y)

$(x + d, y)$

$(x, y + d)$

$(x + d, y + d)$

$(x + 2d, y + d)$

(This is called a *Little Dipper*.)

You can (and should) prove this by making drawings and pointing to stuff.

3. (50 points) Assume that you know that, for all c , $W(100, c)$ exists. Prove that $W(101, 2)$ exists. You can draw diagrams; however, your proof should be completely rigorous.