

TO DO List for Old Ramsey Gang: Ramsey Multiplicity

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1) Seeking many Mono K_3 's in 2-colorings of K_n

1. Write a program that will, given n , form a 2-coloring of $\binom{[n]}{2}$.
2. Write a program that will, given a 2-coloring of $\binom{[n]}{2}$, determine how many mono K_3 's it has.
3. Combine the two programs above to do the following:
The program will be forming a table to be described in the code.
For $n = 6$ to 40 (Might use a lower value if this is too time consuming) Do the following 100 times
 - (a) Randomly color $\binom{[n]}{2}$.
 - (b) Count how many mono K_3 's there are. Record it somewhere.
4. Add to the chart a row with
 n , the min number of mono K_3 's, the max number of mono K_3 's, the average number of mono K_3 's.

2) Seeking many Mono K_4 's in 2-colorings of K_n

Similar to **Seeking Many Mono K_3 's** except that now its K_4 's.

3) Seeking many Mono K_3 's in 3-colorings of K_n

Similar to **Seeking Many Mono K_3 's** except that now its K_4 's.

4) Seeking many Mono K_4 's in 3-colorings of K_n

This may not run fast enough to give answers.)

Similar to **Seeking Many Mono K_3 's** except that now its K_4 's.

5) Seeking many RAINBOW K_3 's in 3-colorings of K_n

Rainbow means all three edges are different colors.

Similar to **Seeking Many Mono K_3 's** except that now its K_4 's.