

Circular Motion

The basic requirements for an object to complete a cycle while traveling in circular motion are as follows;

1. $\text{Velocity}_{\min} > 0$
2. $\text{Tension}_{\min} \geq 0$ (equals only and if $u^2 \geq 5ga$, where u = initial velocity, g = gravitational acceleration, a = radius of circle)
 - When the rope is considered to be threaded through a ring, the tensions of the rope beside the ring are considered as equal.
 - When an object is attached to the rope, the tensions beside the attached objects are not unequal.
 - When an object leaves from the circular motion, the tension is supposed as zero.

Let us consider an object going through circular motion;

1. Acceleration along the tangent = $a\ddot{\theta}$
2. Acceleration towards the center = $a\dot{\theta}^2$

To find the inclination angle of descend, apply as $T=0$, and to find the velocity while descending, substitute the inclination angle.

The difference of circular motions differing on the initial velocity

1. $0 < u^2 < 2ga$

$$\cos \theta_1 = (2ga - u^2)/2ga$$

$$\cos \theta_2 = (2ga - u^2)/3ga$$

According to the above derivation, the value of $\cos \theta_1$ and $\cos \theta_2$ remains between 0 and 1. Therefore, θ_1 and θ_2 are acute angles.

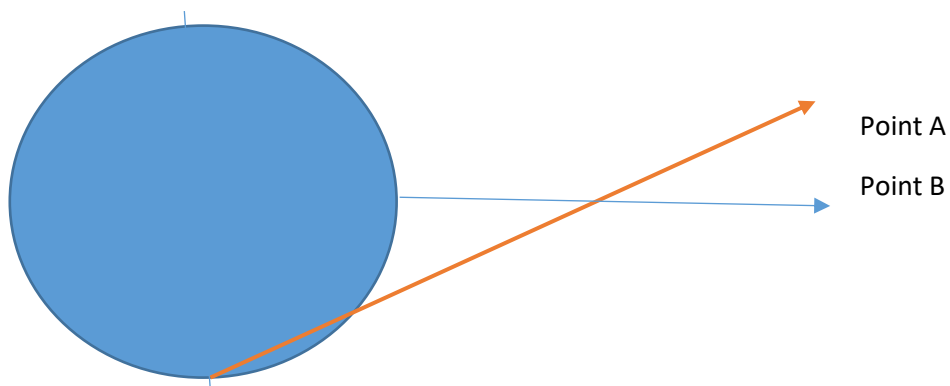
Hence the velocity becomes initially zero and the object begins to swing to and fro in acute angles.

2. $u^2 = 2ga$

$$\cos \theta_1 = 0, \cos \theta_2 = 0.$$

Therefore, θ_1 and θ_2 are right angles.

Hence, the object swings to and fro in right angles(swings beside point A in a semi circle)



3. $2ga < u^2 < 5ga$

The object travels in a wider angle and passes point B. The object leaves the circular motion between point C and Point B

$$\cos \theta_1 = (2ga - u^2)/2ga$$

$$\cos \theta_2 = (2ga - u^2)/3ga$$

$$\cos \theta_1 < \cos \theta_2$$

$$\theta_1 > \theta_2$$

Hence, even though the tension becomes zero, the object will continue to have a velocity, and will leave the circular motion as a projectile.

4. $u^2 = 5ga$

$$\cos \theta_1 = (2ga - u^2)/2ga < 0$$

$$\cos \theta_2 = (2ga - u^2)/3ga < 0,$$

$$\text{Therefore, } \cos \theta_2 = \cos \pi$$

Hence, the tension becomes zero at the highest point of its motion, however the object shall still have a velocity and as a result the object will complete its cycle and journey through circular motion.