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Algorithmic Game Theory Multicast and Network Formation Games

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Motivation

The overarching goal of Network Formation Games is to analyze the way (efficient) networks form under the existence of selfish agents, excluding a central authority.

Examples include:

- The Internet, social networks in general
- Network design(routing etc)
- Operations Research(facility location games)

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A new model Related Games By selfish behavior, we basically mean:

- players want to *minimize the expenses* they incur for building the network
- they also seek to obtain a high quality of service from the network

Informally, the activity of agents reduces to the agents choosing a particular set of edges(generally, paths) according to such selfish behavior.

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A new model Related Games We are interested in the quality(social cost) of the network.

does the game have a Nash equilibrium ?

• if it does, how much worse it is than the optimum ?

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We are interested in the quality(social cost) of the network.

• does the game have a **Nash equilibrium** ?

• if it does, how much worse it is than the optimum ?

Main tool: Potential functions!

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Interesting variations:

- What exactly are the costs inccured by the agents?
 - the cost for using/building an edge
 - congestion?
 - latency?

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Interesting variations:

- What exactly are the costs inccured by the agents?
 - the cost for using/building an edge
 - congestion?
 - latency?
- How are we going to make the agents pay?
 - we can set up certain cost sharing mechanisms that decide the way agents pay for their strategies

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Definition

For any finite game, an **exact potential function** is a function that maps evert strategy vector S to some real value and satisfies the following condition:

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Definition

For any finite game, an **exact potential function** is a function that maps evert strategy vector S to some real value and satisfies the following condition:

if S = (S₁, S₂, ..., S_k), S_i' ≠ S_i is an alternate strategy for some player i, and S' = (S_{-i}, S_i'), then

$$\Phi(S) - \Phi(S') = u_i(S') - u_i(S)$$

A game that possesses an exact potential function is called an **exact potential game**.

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Theorem 19.11

Every potential game has at leat one pure Nash equilibrium, namely the strategy S that minimizes $\Phi(S)$.

Proof

S is stable when no player can increase his/her utility by choosing a different strategy, i.e. when $\Phi(S)$ is at a local minimum.

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Theorem 19.12

In any finite potential game, **best response dynamics** always converge to a Nash equilibrium.

Proof

Best response dynamics is the strategy which produces the most favorable outcome for a player, taking other player's strategies as given. Therefore, it simulates local search on Φ .(improving moves for players decrease Φ)

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Theorem 19.13

Assume that, for any outcome S,

$$\frac{cost(S)}{A} \le \Phi(S) \le B \cdot cost(S)$$

for some constants A, B > 0. Then the price of stability is at most AB.

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A new model Related Games The Model:

- a directed graph G = (V, E)
- nonnegative edge costs c_e for all edges e ∈ E. We will consider these costs to be fixed, though there are games in which that is not the case.
- k players, each with a specified source node s_i and sink node t_i

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A new model Related Games Player *i*'s goal is to build a network in which t_i and s_i are connected, while minimizing construction costs. A strategy for player *i* is therefore a path from t_i to s_i .

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A new model Related Games Apart from these parameters, we also need to set up the cost sharing mechanism, the way in which agents will contribute to building a network and, in particular, the set of edges in their strategy.

A natural choice is the **Shapley cost-sharing mechanism**, also known as the fair mechanism, fair cost allocation, egalitarian cost sharing etc.

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A new model Related Games That just means that all the agents using a particular edge share its cost. Formally, if k_e is the number of players whose path contains e, then e assigns a cost share of c_e/k_e to each of them.

Also, the social objective for this game is simply the cost of the constructed network.(sum of the cost played by all players)

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A new model Related Games First, let's see some examples taken from the textbook.



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In figure a:

- 2 equilibria, one of value 1(also OPT) and the other one of value k
- price of stability is 1
- price of anarchy is k (in fact, the PoA cannot exceed k on any network)

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In figure b:

- 1 equilibrium, of value $H_k = \sum_{j=1}^k \frac{1}{j}$
- OPT is at $1 + \epsilon$
- price of stability is roughly H_k

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In fact...

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In fact...

Theorem 19.10

The price of stability in the global connection game with k players is at most H_k .

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Proof

Define the function $\Phi(S) = \Sigma_e \Phi_e(S)$, where, for each edge, $\Phi_e(S) = c_e \cdot H_{k_e}$.

 Φ is a potential function! Moreover,

 $cost(S) \leq \Phi(S) \leq H_k \cdot cost(S).$

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A new model Related Games The proof extends to the following cases:

- each edge has a **nondecreasing concave cost function** $c_e(x)$, where x is the number of players using edge e.
- c_e is monotone increasing and concave and we add delays d_i
- add capacities

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A new model Related Games A nice observation is that the proof doesn't depend on the topology of the network, which allows us to extend it to a game in which players attempt to share a set of resources. However, there is a big difference between the directed and the undirected case. The same happens when we consider weighted players.

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It's basically similar to the Global Connection Game, except:

- the graph is undirected
- all players are interested in connecting to the same sink

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Price of Anarchy

A new model Related Games While Figure 1 discouraged us from from studying the Price of Anarchy, Chekuri et al. notice that:

- the expensive solution cannot be reached if we initially start with an "empty" configuration and let users join one-by-one
- this leads to an *online* version of the game, introduced by Charikar et al.

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- the expensive solution cannot be reached if we initially start with an "empty" configuration and let users join one-by-one
- this leads to an *online* version of the game, introduced by Charikar et al.

Furthermore, under this assumption, the following results are obtained:

- upper bound of $O(\sqrt{n\log^2 n})$
- lower bound of $\Omega(\frac{\log n}{\log \log n})$

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A new model Related Games The upper bound is obtained by considering a two round game:

- first, all players join one-by-one
 - forms a greedy online Steiner tree which is only O(logn) away from the cost of an optimal Steiner tree
 - that, in turn, is $O(\sqrt{n})$ away from OPT
- players take turns in choosing their strategy by best-response
 - in this round, we lose at most another factor of O(logn) with respect to the cost of the solution obtained from the first round

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A new mode Related Games However...

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However...

Hardness of approximation

It is NP-hard to find a Nash equilibrium that minimizes the potential function.

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But there is hope!

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But there is hope!

The Fractional Multicast Game

- each user is allowed to split its connection to the source into several paths
- a potential function exists, even for the weighted case

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Moreover,

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Moreover,

The Fractional Multicast Game

For the Fractional Multicast Game, a Nash equilibrium that minimizes the potential function can be computed in polynomial time using linear programming.

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Proof

- split every edge into n copies of it, copy e_i having price c_e/i
- write an LP minimizing the potential function
- characterize an optimal solution(canonical flow)
- rearrange the output flow of the LP into a canonical flow that is not larger than the potential of the original flow f

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Moreso,

Price of Anarchy

The price of anarchy is O(logn).

and

The Weighted Fractional Case

A Nash equilibrium exists in the Weighted Fractional Multicast Game.

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A new model Related Games Charikar et al. improve the bound on the PoA for the integral case by showing that, in Phase 1, the greedy algorithm has competitive ratio $O(log^2n)$. We therefore get that:

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A new model Related Games Charikar et al. improve the bound on the PoA for the integral case by showing that, in Phase 1, the greedy algorithm has competitive ratio $O(log^2n)$. We therefore get that:

PoA for Multicast Cost Sharing

The Nash equilibrium reached by the two-phase Multicast Cost Sharing game with best response dynamics has cost $O(log^3n)OPT$.

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A new model Related Games As a sidenote, there is an interesting new game that has just been introduced by Anshelevich et al.

Network Cutting Game

- players want to cut themselves from nodes in the network
- if the player does not meet the cut requirement, it pays a penalty cost
- does not, in general, have pure Nash equilibria
- for some special case, there exist approximate equilibria

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Network Multicut Game

- each player i wants to disconnect from some specific node t_i
- there always exists a 2-approximate Nash equilibrium as cheap as OPT
- proof is done by an algorithm that actually assigns edges of OPT to the players
- it can be shown that no player can reduce the cost by more than half by deviating from the state

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Related Games

First, let's look at the inspiration:

Network Creation Games

- each player can build a set of edges around him
- the objective is to be connected to all the other nodes in the graph

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First, let's look at the inspiration:

Network Creation Games

- each player can build a set of edges around him
- the objective is to be connected to all the other nodes in the graph
- the game comes in two flavors: unilateral and bilateral, depending on the cost-sharing scheme
- unilateral : at most one node pays for the edge
- bilateral: both of the nodes contribute to the cost of the edge

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First, let's look at the inspiration:

Network Creation Games

- each player can build a set of edges around him
- the objective is to be connected to all the other nodes in the graph
- the game comes in two flavors: unilateral and bilateral, depending on the cost-sharing scheme
- unilateral : at most one node pays for the edge
- bilateral: both of the nodes contribute to the cost of the edge
- constant bounds on the price of anarchy have been establihed for a variety of ranges of the cost of an edge

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AGT-Network Formation Games **Related Games**

This motivates our next game:

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A new model Related Games This motivates our next game:

The Contribution Game

- introduced by Anshelevich et al.
- every player contributes to an edge(relationship) with a certain effort, within the limit of a particular budget
 - there is a reward function for each edge
 - the player's wellfare is the total sum of rewards he obtains for the relationships he establishes
 - mixed results, depending on the nature of the reward function(ex: price of anarchy is at most 2 when the functions are concave)
- authors consider pairwise equilibrium, instead of Nash

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A new model Related Games This finally brings us to a new game:

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A new model Related Games This finally brings us to a new game:

The PeerWise Game

- players have a set of destinations they are trying to reacg
- each edge has a latency associated with it
- triangle inequality might not apply so it is often the case that a detour is faster
- connections(edges) are constructed based on "'mutual advantage"'
- the wellfare of the player is equal to the total sum of fastest(min latency) distances to its destinations

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A new model Related Games

- Mutual advantage is defined according to a reward function depending on the node with which the current player wants to establish a connection
- reward function = difference between the player's wellfare when it makes the connection with the node - the player's wellfare when it doesn't connect to the node

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A new model Related Games

- Mutual advantage is defined according to a reward function depending on the node with which the current player wants to establish a connection
- reward function = difference between the player's wellfare when it makes the connection with the node - the player's wellfare when it doesn't connect to the node
- the model is inspired by the PeerWise latency-reducing overlay network introduced by Lumezanu et al
- in PeerWise, "'mutual advantage"' is a principle according to which to users establish a connection only if they can provide resources to each other

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A new model Related Games

- can we use some of the methods in the games presented so far?
- how can we characterize a Nash equilibrium? Is there a potential function?
- it might be wiser to consider pairwise and approximate equilibrium

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- can we extend the analysis to the case of multi-source case(i.e. Global Connection Game for an undirected graph)
- what about the case in which we allow for random replays and arrivals? (Chekuri et al. show that in the case of a semi-random setting, the solution is within O(polylog(n)√n · OPT)
- in case of the fractional multicast game, can we use an SDP instead of an LP?

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A new model Related Games Thank you!

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