neural language models

CS 685, Fall 2020

Advanced Natural Language Processing http://people.cs.umass.edu/~miyyer/cs685/

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many slides from Richard Socher and Matt Peters

Stuff from last time...

- Pass/fail policy? (technically SAT / UNSAT)
 - Deadline to notify us that you want pass/fail: same as final report deadline (12/4)
 - Send an email to the instructors account with your request
 - Send a reminder email at the end of the semester
- HWO due this Friday!
- Form final project groups by Friday or we'll do it for you!

language model review

• Goal: compute the probability of a sentence or sequence of words:

 $P(W) = P(w_1, w_2, w_3, w_4, w_5...w_n)$

- Related task: probability of an upcoming word: P(w₅|w₁,w₂,w₃,w₄)
- A model that computes either of these:

P(W) or P($w_n | w_1, w_2...w_{n-1}$) is called a language model or LM

n-gram models

 $p(w_j | \text{students opened their}) = \frac{\text{count}(\text{students opened their } w_j)}{\text{count}(\text{students opened their})}$

Problems with n-gram Language Models

Sparsity Problem 1

Problem: What if *"students* opened their w_j " never occurred in data? Then w_j has probability 0!

 $p(w_j | \text{students opened their}) = \frac{\text{count}(\text{students opened their } w_j)}{\text{count}(\text{students opened their})}$

Problems with n-gram Language Models

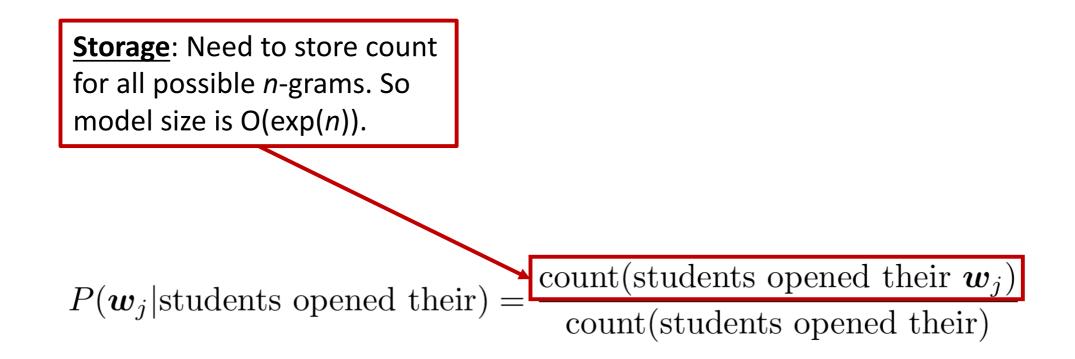
Sparsity Problem 1

Problem: What if *"students* opened their w_j " never occurred in data? Then w_j has probability 0!

(Partial) Solution: Add small δ to count for every $w_j \in V$. This is called *smoothing*.

 $p(w_j | \text{students opened their}) = \frac{\text{count}(\text{students opened their } w_j)}{\text{count}(\text{students opened their})}$

Problems with n-gram Language Models



Increasing *n* makes model size huge!

another issue:

 We treat all words / prefixes independently of each other!

students opened their ____

pupils opened their ____

scholars opened their ____

Shouldn't we share information across these semantically-similar prefixes?

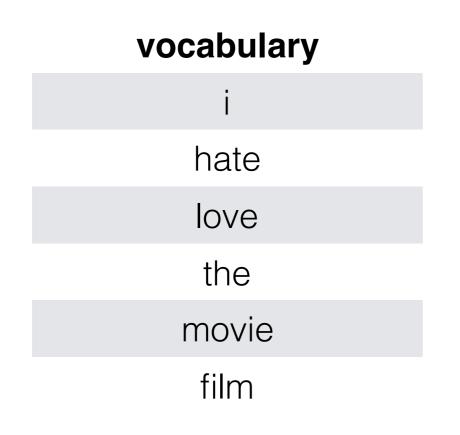
undergraduates opened their ____

students turned the pages of their ____

students attentively perused their ____

one-hot vectors

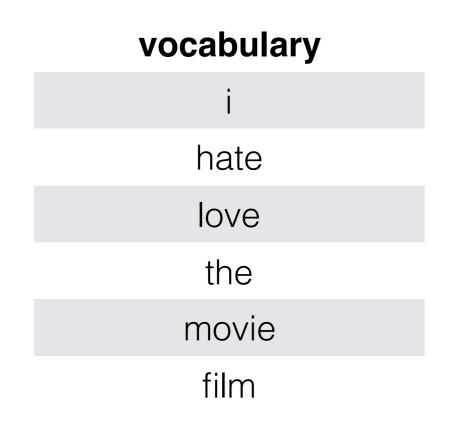
- n-gram models rely on the "bag-of-words" assumption
- represent each word as a vector of zeros with a single 1 identifying the index of the word



movie = <0, 0, 0, 0, 1, 0>film = <0, 0, 0, 0, 0, 1>

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movie = <0, 0, 0, 0, 1, 0>film = <0, 0, 0, 0, 0, 1>

what are the issues of representing a word this way?

all words are equally (dis)similar!

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all words are equally (dis)similar!

movie = <0, 0, 0, 0, 1, 0>
film = <0, 0, 0, 0, 0, 0, 1>
dot product is zero!
these vectors are orthogonal

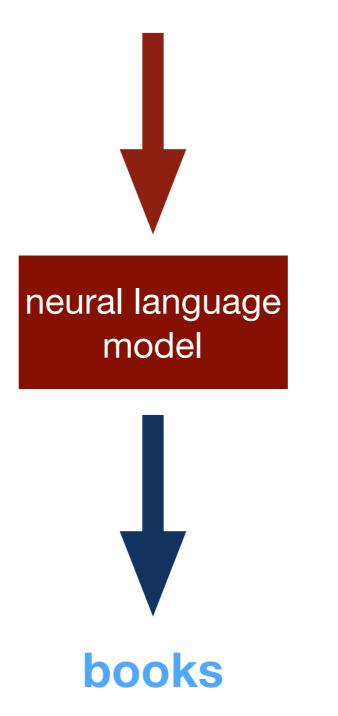
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What we want is a representation space in which words, phrases, sentences etc. that are semantically similar also have similar representations!

Enter neural networks!

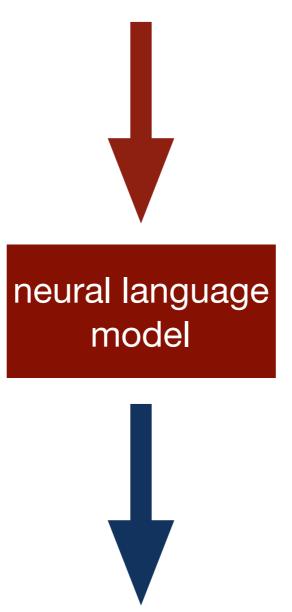
Students opened their



Enter neural networks!

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This lecture: the forward pass, or how we compute a prediction of the next word given an existing neural language model



books

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This lecture: the forward pass, or how we compute a prediction of the next word given an existing neural language model neural language model

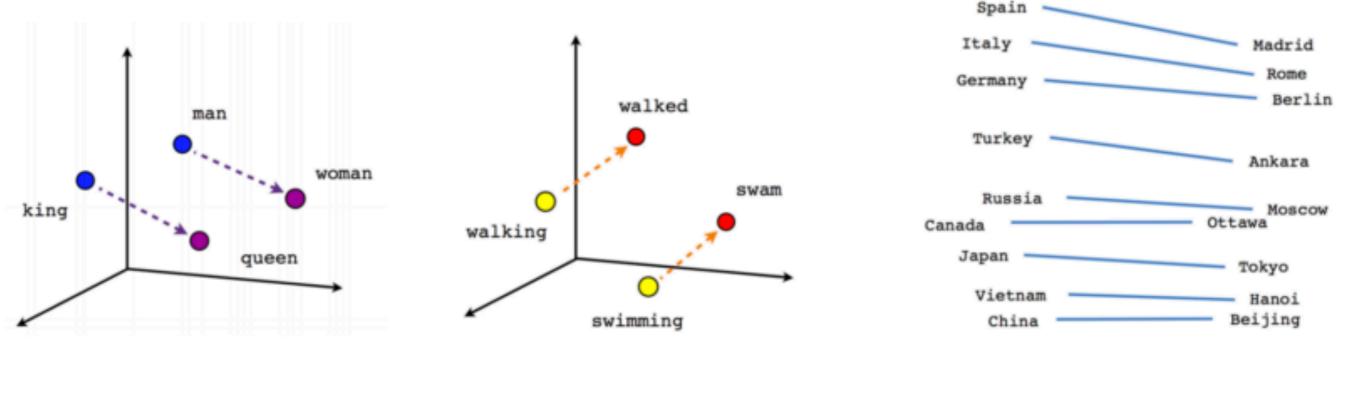
Next lecture: the backward pass, or how we train a neural language model on a training dataset using the backpropagation algorithm

books

words as basic building blocks

• represent words with low-dimensional vectors called embeddings (Mikolov et al., NIPS 2013)

king = [0.23, 1.3, -0.3, 0.43]



Male-Female

Verb tense

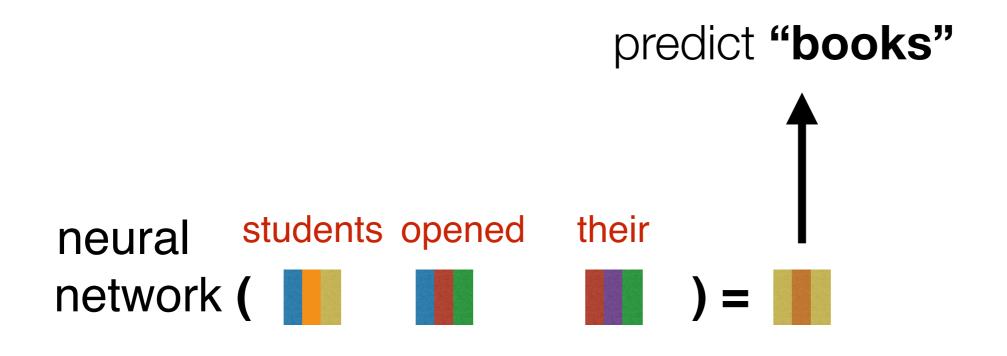
Country-Capital

composing embeddings

 neural networks compose word embeddings into vectors for phrases, sentences, and documents



Predict the next word from composed prefix representation



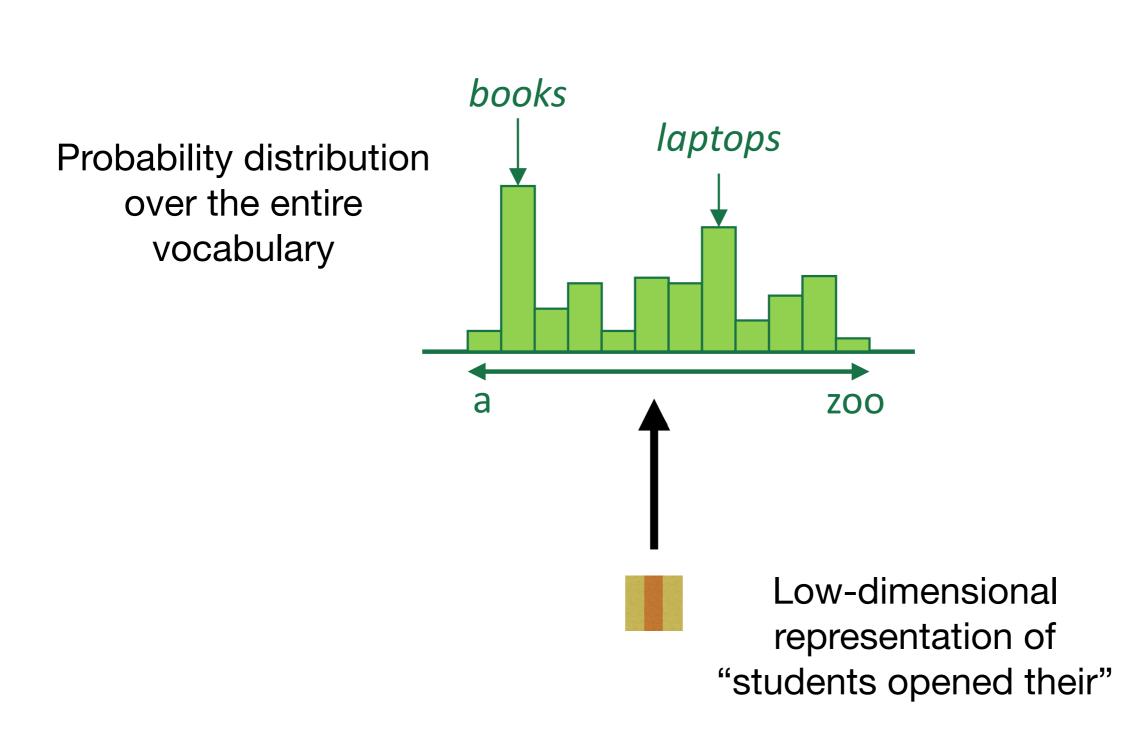
How does this happen? Let's work our way backwards, starting with the prediction of the next word



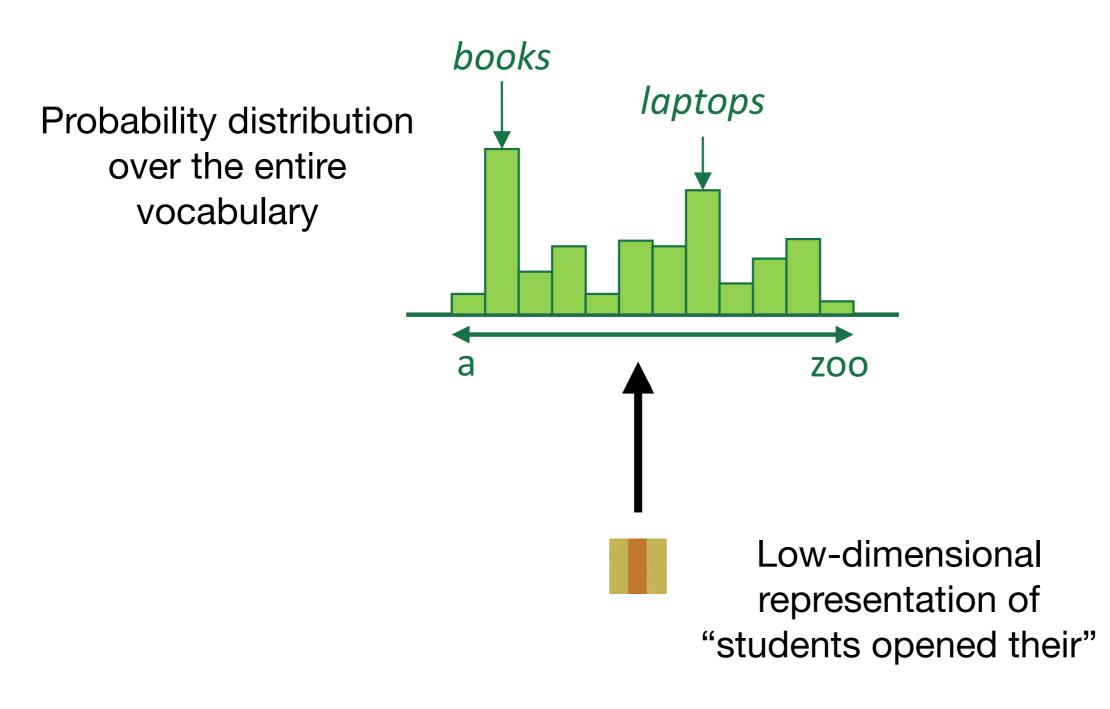
How does this happen? Let's work our way backwards, starting with the prediction of the next word



Softmax layer: convert a vector representation into a probability distribution over the entire vocabulary



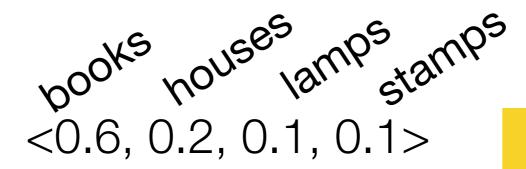
$P(w_i | \text{vector for "students opened their"})$



Let's say our output vocabulary consists of just four words: "books", "houses", "lamps", and "stamps".



Low-dimensional representation of "students opened their" Let's say our output vocabulary consists of just four words: "books", "houses", "lamps", and "stamps".



We want to get a probability distribution over these four words



Low-dimensional representation of "students opened their"

$$\mathbf{W} = \left\{ \begin{array}{l} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{array} \right\}$$

Here's an example 3-d prefix vector

product

x = <-2.3, 0.9, 5.4>

Here's an example 3-d prefix vector

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intuition: each row of **W** contains *feature weights* for a corresponding word in the vocabulary

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x = <-2.3, 0.9, 5.4>

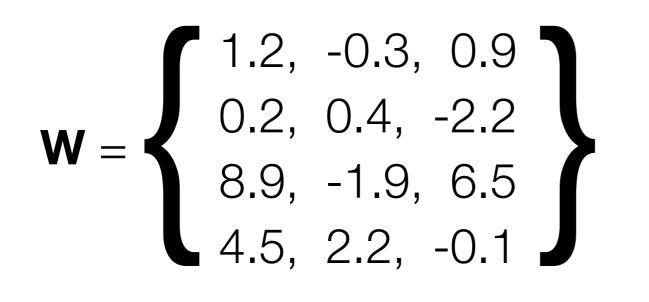
intuition: each row of **W** contains *feature weights* for a corresponding word in the vocabulary CAUTION: we can't easily *interpret* these features! For example, the second dimension of **x** likely does not correspond to any linguistic property

 $\mathbf{W} = \left\{ \begin{array}{ll} 1.2, \ -0.3, \ 0.9 \\ 0.2, \ 0.4, \ -2.2 \\ 8.9, \ -1.9, \ 6.5 \\ 4.5, \ 2.2, \ -0.1 \end{array} \right\} \begin{array}{l} books \\ houses \\ houses \\ tamps \\ stamps \\ stamps \end{array} \right.$

x = <-2.3, 0.9, 5.4>

Wx = <1.8, -11.9, 12.9, -8.9>

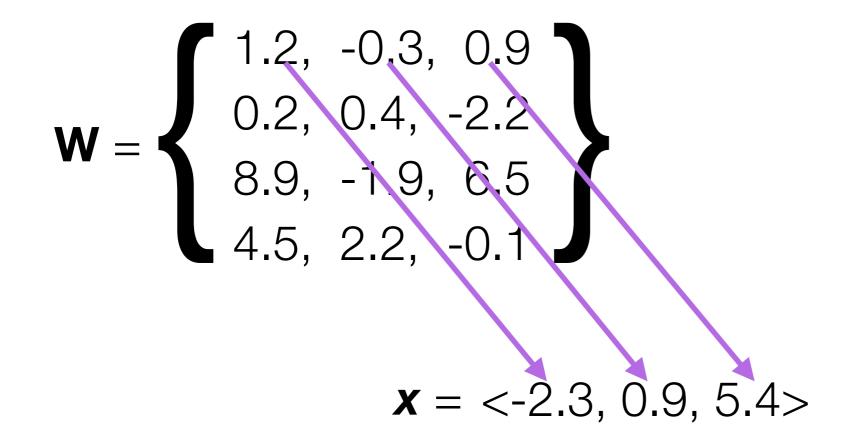
How did we compute this? It's just the dot product of each row of **W** with **x**!

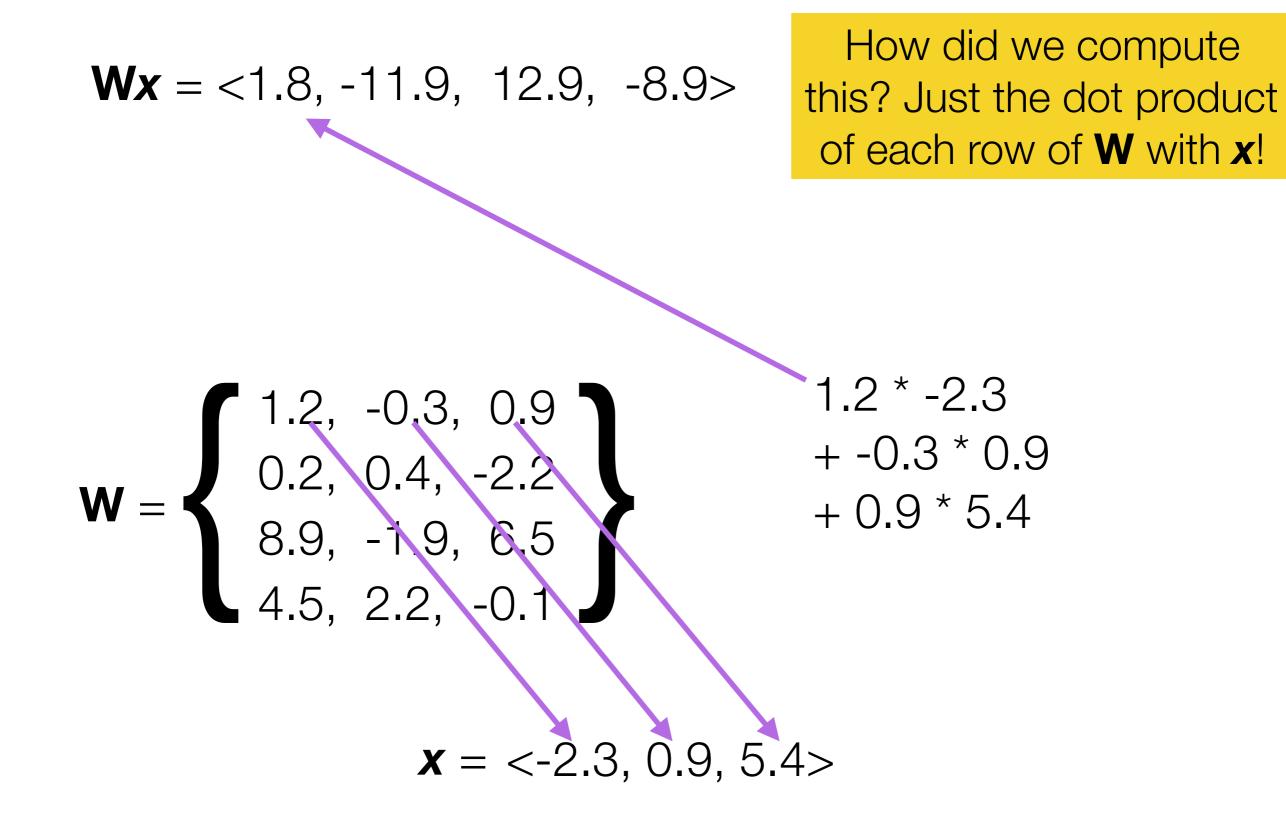


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How did we compute this? It's just the dot product of each row of **W** with **x**!





Okay, so how do we go from this 4-d vector to a probability distribution?

We'll use the **softmax** function!

softmax(x) =
$$\frac{e^x}{\sum_j e^{x_j}}$$

- x is a vector
- x_j is dimension j of x
- each dimension *j* of the softmaxed output represents the probability of class *j*

Wx = <1.8, -1.9, 2.9, -0.9> **softmax(Wx)** = <0.24, 0.006, 0.73, 0.02>

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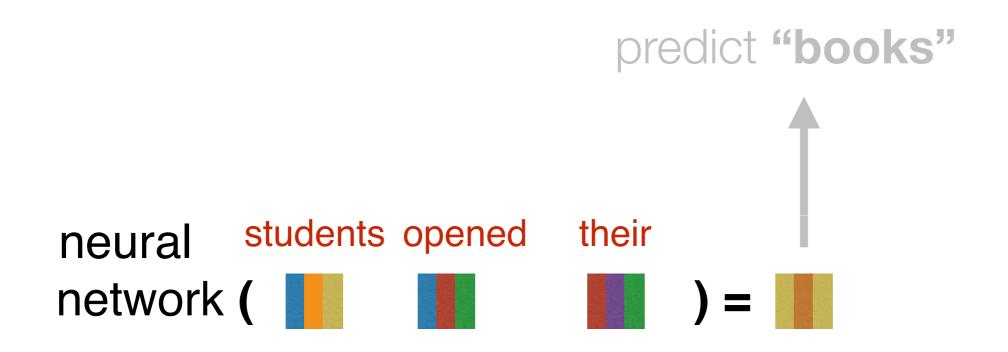
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We'll see the softmax function over and over again this semester, so be sure to understand it!

so to sum up...

- Given a *d*-dimensional vector representation *x* of a prefix, we do the following to predict the next word:
 - 1. Project it to a *V*-dimensional vector using a matrix-vector product (a.k.a. a "linear layer", or a "feedforward layer"), where *V* is the size of the vocabulary
 - 2. Apply the softmax function to transform the resulting vector into a probability distribution

Now that we know how to predict **"books"**, let's focus on how to compute the prefix representation **x** in the first place!



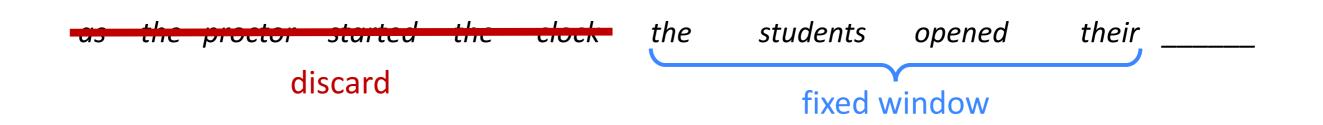
Composition functions

input: sequence of word embeddings corresponding to the tokens of a given prefix

output: single vector

- Element-wise functions
 - e.g., just sum up all of the word embeddings!
- Concatenation
- Feed-forward neural networks
- Convolutional neural networks
- Recurrent neural networks
- Transformers (our focus this semester)

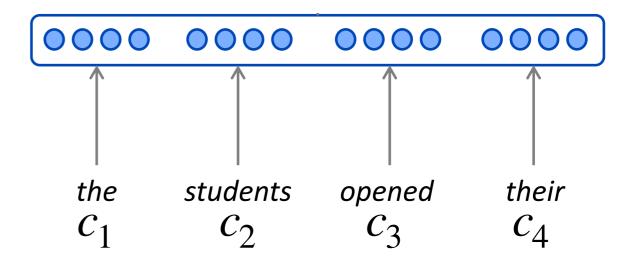
Let's look first at *concatenation*, an easy to understand but limited composition function



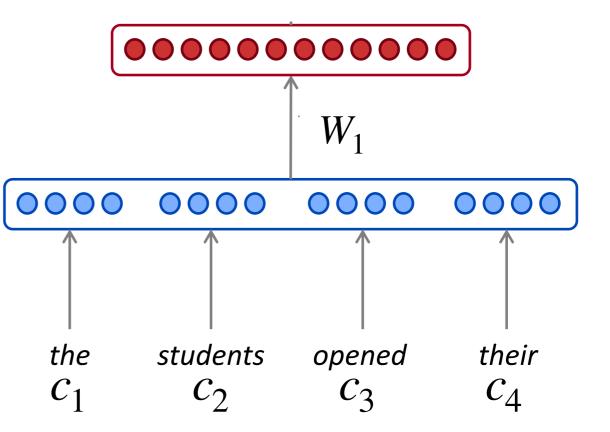
concatenated word embeddings

 $x = [c_1; c_2; c_3; c_4]$

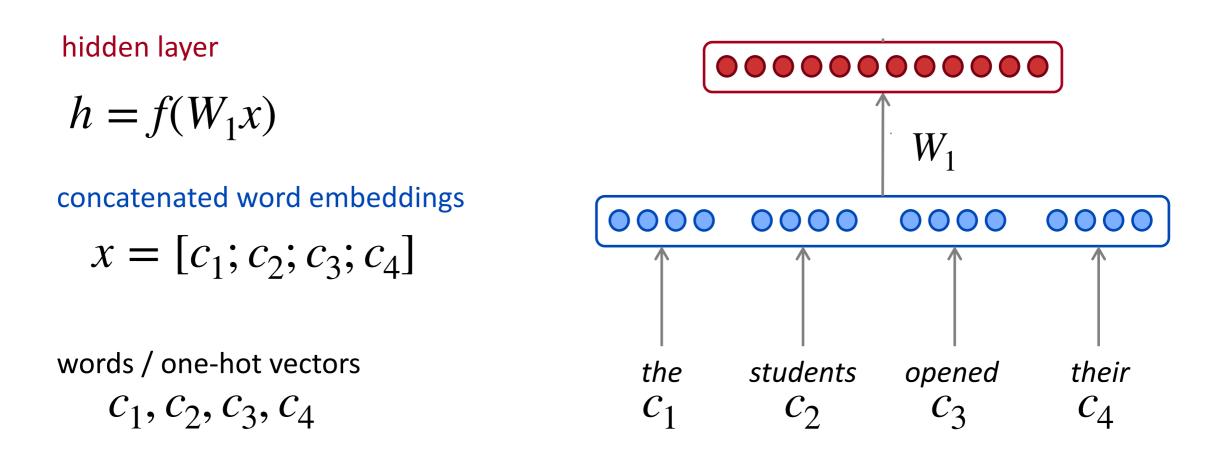
words / one-hot vectors



hidden layer $h = f(W_1x)$ concatenated word embeddings $x = [c_1; c_2; c_3; c_4]$ words / one-hot vectors c_1, c_2, c_3, c_4



f is a nonlinearity, or an element-wise nonlinear function.
 The most commonly-used choice today is the rectified linear unit (ReLu), which is just ReLu(x) = max(0, x).
 Other choices include tanh and sigmoid.



output distribution

 $\hat{y} = \operatorname{softmax}(W_2h)$

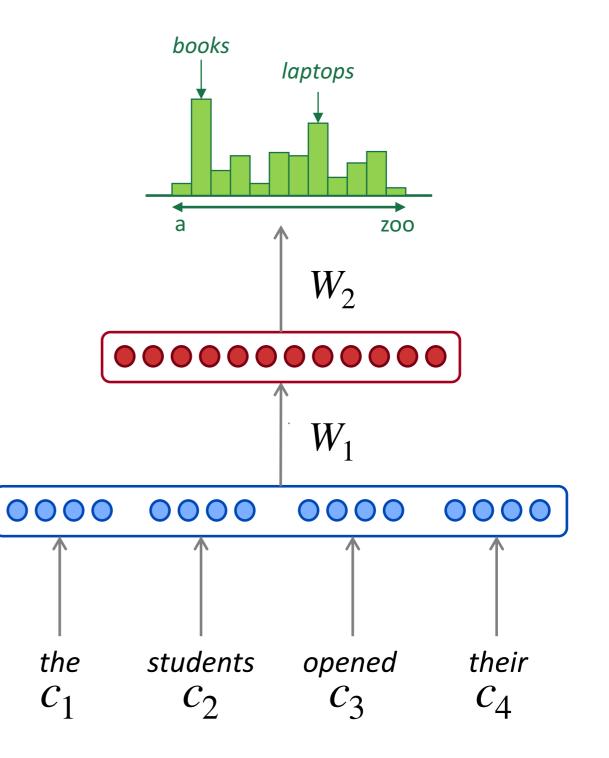
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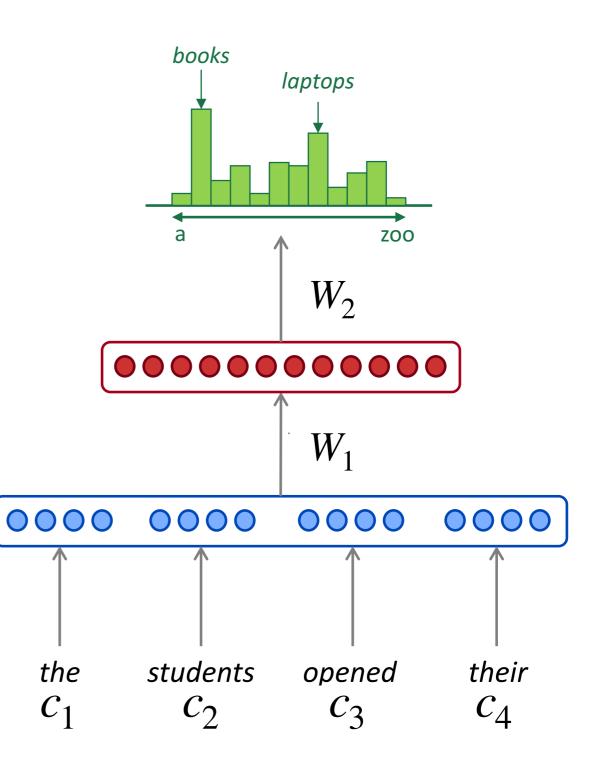
how does this compare to a normal n-gram model?

Improvements over *n*-gram LM:

- No sparsity problem
- Model size is O(n) not O(exp(n))

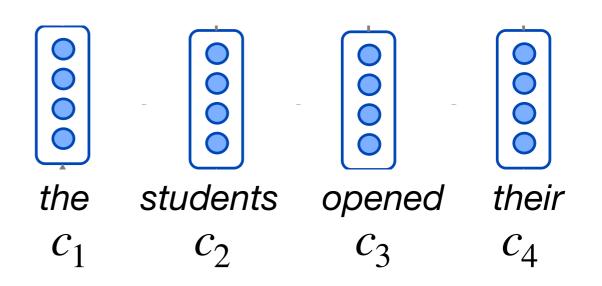
Remaining **problems**:

- Fixed window is too small
- Enlarging window enlarges W
- Window can never be large enough!
- Each C_i uses different rows of W. We don't share weights across the window.



Recurrent Neural Networks!

word embeddings

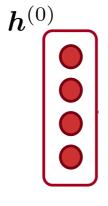


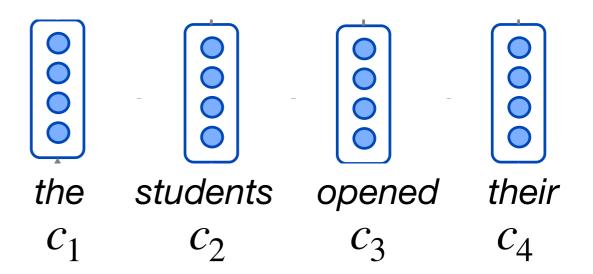
hidden states

$$h^{(t)} = f(W_h h^{(t-1)} + W_e c_t)$$

h⁽⁰⁾ is initial hidden state!

word embeddings





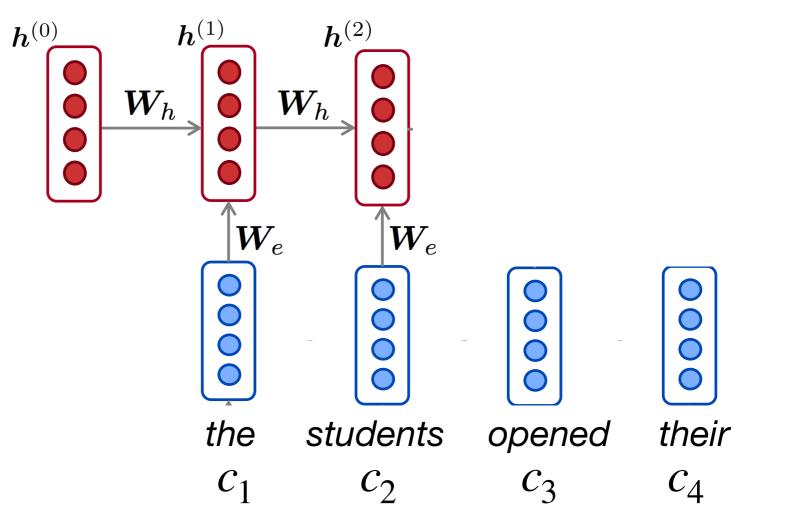
 $oldsymbol{h}^{(0)}$ $h^{(1)}$ hidden states \pmb{W}_h $h^{(t)} = f(W_h h^{(t-1)} + W_e c_t)$ h⁽⁰⁾ is initial hidden state! W_e \bigcirc word embeddings 0 0 \bigcirc C_1, C_2, C_3, C_4 students the opened their C_3 C_4 C_1 c_2

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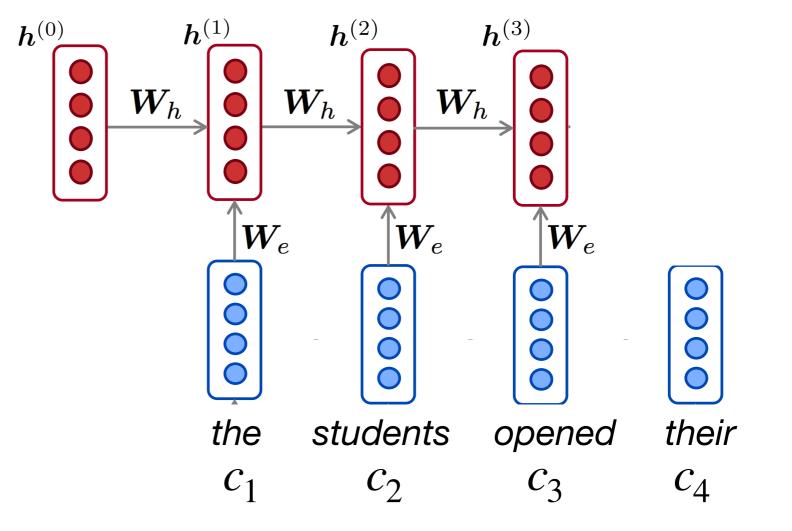


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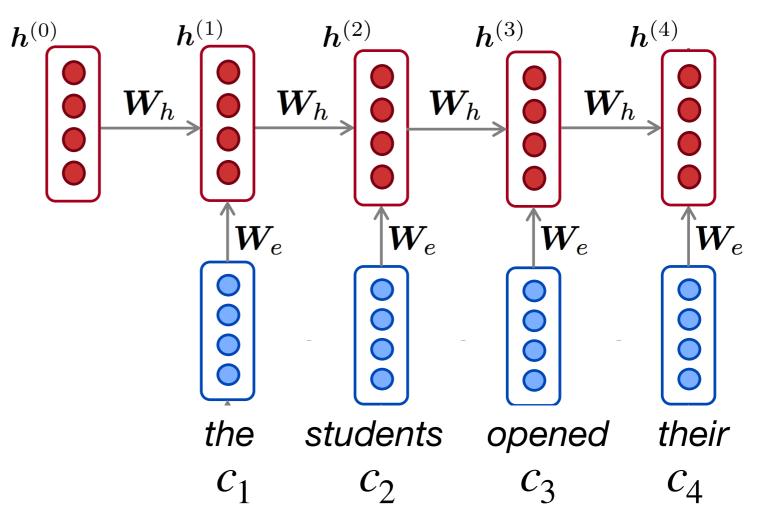


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output distribution

 $\hat{y} = \operatorname{softmax}(W_2 h^{(t)})$

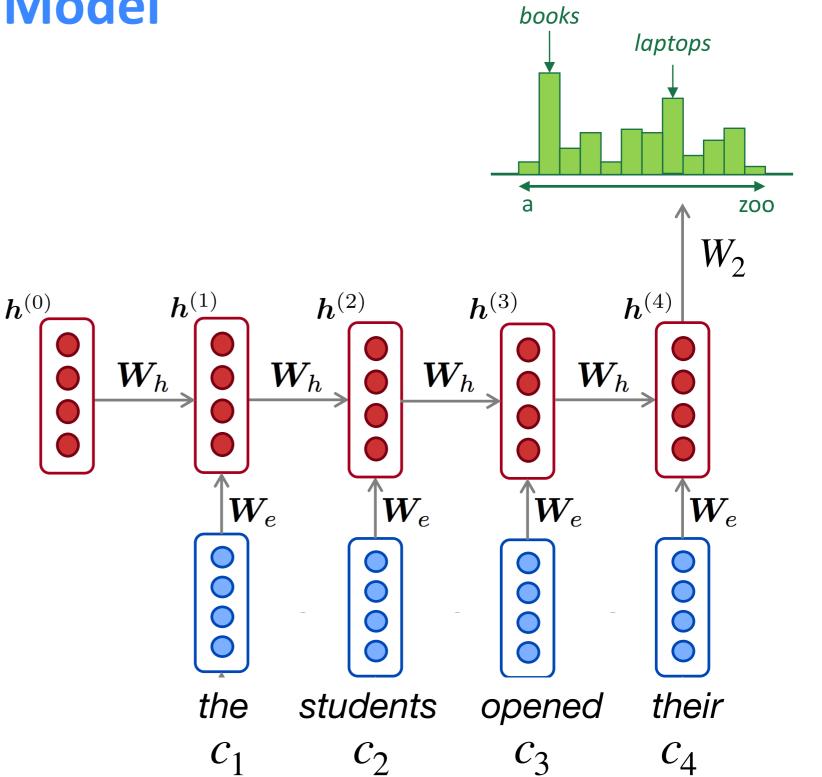
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word embeddings

 c_1, c_2, c_3, c_4



 $\hat{\boldsymbol{y}}^{(4)} = P(\boldsymbol{x}^{(5)}|\text{the students opened their})$

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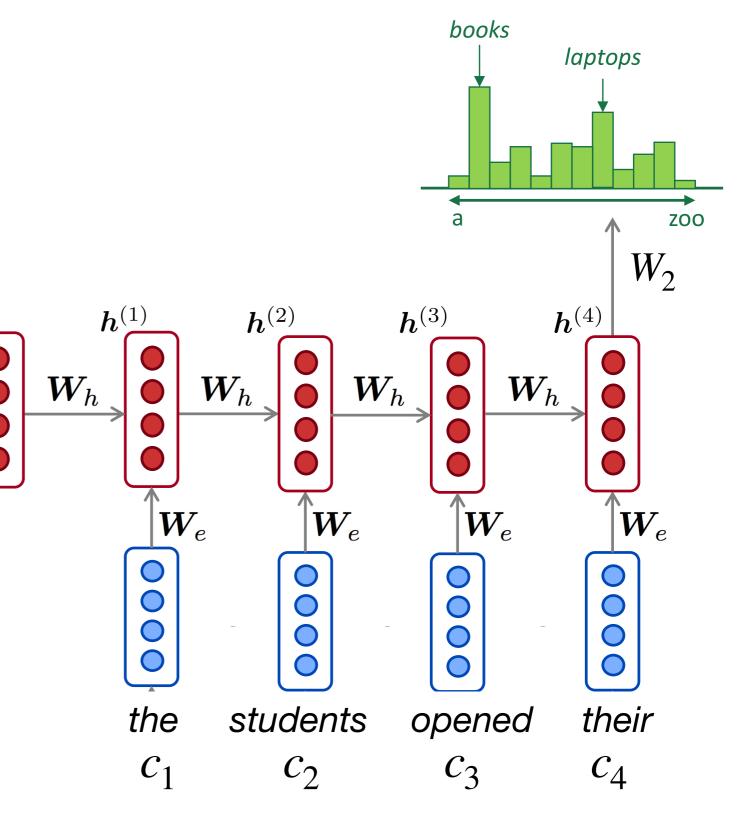
why is this good?

RNN Advantages:

- Can process any length input
- Model size doesn't increase for longer input
- Computation for step t can (in theory) use information from many steps back
- Weights are shared across timesteps → representations are shared

RNN **Disadvantages**:

- Recurrent computation is slow
- In practice, difficult to access information from
- __many steps back



 $m{h}^{(0)}$

Be on the lookout for...

- Next lecture on **backpropagation**, which allows us to actually train these networks to make reasonable predictions
- Next week, we'll focus on the Transformer architecture, which is the most popular composition function used today