

INTERACTIVE FEATURE RECOGNITION USING MULTI-PROCESSOR METHODS

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ABSTRACT

The availability of low-cost computational power is enabling development of increasingly sophisticated CAD software. Automation of design and manufacturing activities poses many difficult computational problems. Design is an interactive process and speed is a critical factor in systems that enable designers to explore and experiment with alternative ideas. As more downstream manufacturing activities are considered during the design phase, computational costs become problematic. Achieving interactivity requires a sophisticated allocation of computational resources in order to perform realistic design analyses and generate feedback in real time.

This paper presents our initial efforts to use distributed algorithms to recognize machining features from solid models of parts with large numbers of features and many geometric and topological entities. Our goal is to outline how significant improvements in computation time can be obtained using existing hardware and software tools. An implementation of our approach is discussed.

1. INTRODUCTION

The availability of low-cost computational power is enabling the development of increasingly sophisticated CAD software. Software tools designed to reduce time-consuming build-test-redesign iterations are becoming essential for increasing engineering quality and productivity. Examples include tools for finite element analysis, mechanism analysis, simulation, and rapid prototyping. Such tools have become crucial components in research on concurrent engineering and engineering design.

Automation of the design process and construction of such tools pose many difficult computational problems. In order to realize the advantages of concurrent engineering,

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more downstream engineering activities are considered during the design phase. As design is an interactive process, speed is a critical factor in systems that enable designers to explore and experiment with alternative ideas during the design stage. Achieving interactivity requires an increasingly sophisticated allocation of computational resources in order to perform design analyses and generate feedback in real time.

It is becoming increasingly evident that one necessary component of an automated design analysis tool is a subsystem for recognizing manufacturing features directly from a CAD or solid model. This problem has been the focus of extensive research over the last decade. Feature recognition is used for a variety of applications, including the generation of process plans [29], translation between design and manufacturing features, and production of redesign suggestions [5]. What has also become evident is that feature recognition, for realistic classes of parts with multiple and interacting feature interpretations, is computationally expensive. Hence, generating the features from a part may become a computational bottleneck within a design system. Further, existing feature recognition research has dealt exclusively with serial computer architectures.

In this paper we present our initial efforts toward developing a methodology for recognizing a class of machining features using a distributed, multi-processor algorithms. Feature recognition has been approached using a variety of techniques, some of which are easier to parallelize than others. In previous work [23], we described trace-based, serial algorithms for finding feature instances from solid model data. This current work indicates that trace-based feature recognition methodologies are particularly well suited for parallelization. The basic steps in this approach are:

1. **Task initialization.** Initialization is performed at four levels: (1) the features to be recognized; (2) the types of trace information used to construct the feature instances; (3) the geometry and topology of the traces;

and (4) simplification of the part geometry to reduce the costs to solid modeling operations.

2. **Task distribution.** Divide the problem using the task decomposition, isolating independent portions of the recognition problem and identifying a suitable computational resource for solving it.
3. **Synthesis of results.** Combine the results obtained by each separate processor into a global solution. This solution set can then be passed on to the application at hand—in the context of our previous work, this application is a subsystem for performing manufacturability analysis for machined parts [11, 12].

The benefits of applying this approach include:

- It increases the complexity of parts that are now computationally feasible. In the feature recognition area, serial approaches have experienced great difficulty when scaled to address complex, real-world parts, which have thousands of geometric and topological entities and several hundred interacting feature instances. This approach is best suited for parts in which there might be thousands of feature instances, but the individual features themselves are simple in structure. A distributed approach can put a greater number of such components within reach of existing computational tools.
- It makes use of existing commercial solid modeling tools directly. In this way, one does not require parallelized versions of common algorithms or the implementation of multi-threaded, multi-processor solid modeling systems.
- It enables interactive analysis and feedback. Recognition of the many alternative features can be done for complex parts in real time. This facilitates faster and more comprehensive analyses of manufacturability for the part at hand.
- It exploits the growing ubiquity and power of networked computing facilities to provide a flexible means of utilizing networked computational resources. Effective utilization of large collections of inexpensive processors enables applications to perform computationally intensive CAD/CAM activities efficiently and interactively.

2. RELATED WORK

The bibliography of work on multi-processor algorithms for solid modeling applications is limited but growing. Currently, most works have focused on parallel operations on CSG trees and other CSG representations of polygonal or polyhedral entities. Ellis *et al.* [7] have developed the Ray-Casting Engine: a hardware-implemented facility for sampling solids represented in CSG for a variety of purposes, including rendering and mass-property calculations. They outline how this special-case hardware makes possible brute-force solutions to difficult computational problems, such as spatial sweeping and offsetting.

Narayanaswami and Franklin [20] present a parallel multi-processor method for calculating the mass properties of polygonal CSG objects and outlined some extensions for applying the techniques to 3-D polyhedra. Banerjee *et al.* [2] have developed parallelized algorithms for evaluating CSG trees that operate with a fixed number of processors with shared memory.

In the domain of boundary representation modeling, Karinthe *et al.* [17] have produced a parallel algorithm for performing boolean set operations on polygons and polygons with holes. In Almasi *et al.* [1], these techniques are extended to more general loops of edges.

Strip and Karasick [27] present techniques for performing solid modeling operations on a massively parallel SIMD (single instruction multiple data) computer. They provide a data structure for representation of solid models and a variety of parallel algorithms for implementing solid modeling operations. In addition, they present performance comparisons with serial implementations.

Existing work on recognition of features has dealt with exclusively serial computer architectures. These feature technologies are based heavily on the geometric and topological manipulation capabilities of solid modeling systems and deal predominantly with form or machining features. Much has been written on this topic in the literature and we will not attempt to mention all of this work here. We present below several of the more recent and relevant works.

The work of Henderson has continually brought new computational techniques to address the feature recognition problem. The work described in [14] was the first to apply expert systems to the feature recognition problem. Gavankar and Henderson [10] present techniques to identify protrusions and depressions in the boundary model of a part. More recently, Prabhakar and Henderson [22] described the use of neural networks to recognize and classify features. A strength of this approach is that it exploits the trainability of a neural net to incorporate new feature types. Further, neural nets have been demonstrated to be effective in classifying patterns in domains where there is "noise." This noise is in the form of incomplete or missing feature data lost due to feature intersections.

Graph-based algorithms have proven useful for extracting some classes of features. These methods fall into two categories: those based on graph search [6, 4] and those based on pattern matching [16, 21, 25]. A common difficulty for both categories of graph-based approaches is that the graph-based representations for solid models of parts are difficult to extend to the complex geometry and topology found in real industrial parts. Secondly, methods based on pattern matching and finding subgraph isomorphisms (a problem known to be NP-hard) are prone to combinatorial difficulties.

Chuang and Henderson [3] explore graph-based pattern matching techniques to classify feature patterns based on geometric and topological information from the part. Sakurai [26] provides for limited user-defined feature types with a graph-based feature recognition system. Efforts at Carnegie

Mellon University [21, 25] have employed graph grammars for finding features in models of injection molded parts. Recently, Corney and Clark [4] have employed graph-based algorithms to find general feature classes from $2\frac{1}{2}$ -dimensional parts.

Gadh and Prinz [9] were the first to describe techniques for combating the combinatorial costs of handling complex and realistic industrial parts (i.e. those with thousands of topological entities). They point out that, in such cases, traditional knowledge-based, decomposition, and pattern-matching techniques are computationally impractical because the fundamental algorithms (i.e. forward chaining in a frame-based reasoning system or subgraph pattern matching) are inherently exponential. Gadh and Prinz's method is to abstract an approximation of the geometric and topological information in a solid model and find shape features in the approximation. Their approach employs a differential depth filter to reduce the number of topological entities. A second pass maps the topological entities onto structures called "loops." In their work, features are defined using the higher-level loops as opposed to being defined as patterns in the boundary representation's geometry and topology. This approach significantly reduces the number of entities that need to be searched to build feature instances. While this kind of approach holds much promise for addressing combinatorial problems, it does not address how to extend the techniques to better handle interacting features and more non-linear (non-faceted) solid models.

Fields and Anderson [8] present an approach to feature recognition that overcomes some of the representation and efficiency problems common in previous work. Unlike pattern-based or decomposition-based recognition methodologies, they categorize sets of faces on the surface of the part into classes of general machining features: protrusions, depressions, and passages. The shapes within each class, while sharing many operational similarities, may vary in geometry and topology. For each of their feature classes, they present a linear-time algorithm.

Many aspects of the feature recognition problem are still open and active areas of research. Among these are: recognizing and representing interacting features [29], incremental recognition of features [18, 13], modeling alternative feature interpretations and completeness [19, 23], and reasoning about the manufacturability of features [11].

3. APPROACH TO FEATURE RECOGNITION

In this section we outline a basic feature recognition technique on which we will build our multiprocessor algorithms in Section 4. We have chosen to adopt a trace-based methodology for this purpose; the reasons for this choice shall become evident. Fundamentally, a trace-based approach to feature recognition attempts to reconstruct feature instances from the information that they contribute to the final CAD model of the product.

The work of Marefat and Kashyap [19] presented an early trace-based technique. They expanded on the work of Joshi and Chang [16], augmenting it with hypothesis testing tech-

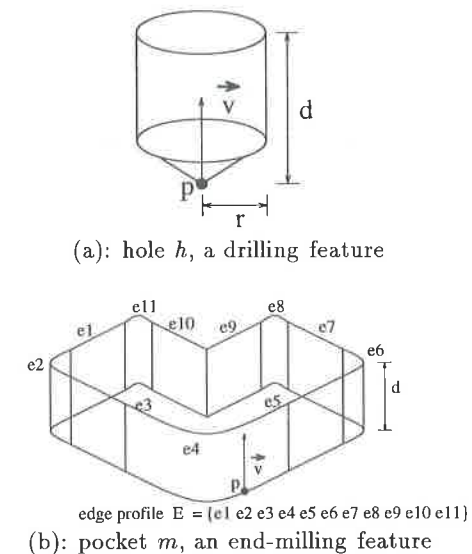


Figure 1: Examples of machining features

niques. In Marefat and Kashyap's method, information from the solid model is used to generate hypotheses about the existence of features. These hypotheses are tested to see if they give rise to valid feature instances.

Vandenbrande and Requicha [29] were the first to formalize trace-based (or hint-based) techniques for constructing features from information in a solid model. In the work of Vandenbrande, the traces are used to fill "feature frames" in a frame-based reasoning system. After filling frames with the trace information present in the part, the system classifies the partial frames and attempts to complete the frame information for those that appear promising using a variety of geometric reasoning and computational geometry techniques.

Regli *et al.* [24, 23] present an approach for guaranteeing completeness of a recognition algorithm; i.e., it describes how one can define a class of features and verify that a particular approach is capable of producing all features in that class. They present feature recognition as an algorithmic problem in which traces are found by traversing the geometry and topology of the part and then used to construct feature instances. They formally describe the behavior of their algorithm and calculate a general measure of its complexity. This approach has been employed for automated design analysis [11] and automated redesign [5].

Trace-based approaches have several advantageous properties that are just beginning to be exploited by researchers, including:

- Feature traces can be derived from a variety of design information such as tolerances, surface finish requirements, and functional information associated with surfaces. Traditional feature recognition methodologies often consider only the part's geometry and topology.
- Feature classes can be customized by users. Recognition routines for new features can be built by introduc-

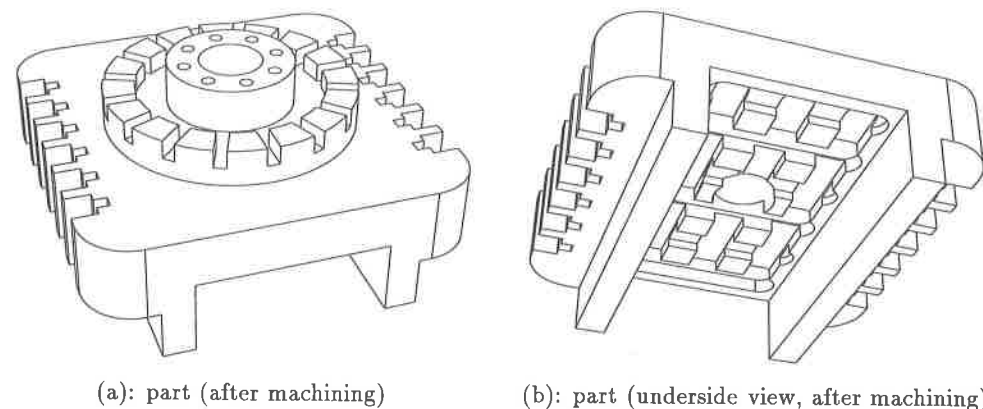


Figure 2: An example part.

ing traces for the new features and methods for building instances of the new features from these traces.

- Trace-based techniques can be adapted to recognize features from a variety of manufacturing domains. Existing feature recognition literature focuses primarily on machined parts, due in part to the fact that the functionality of solid modeling systems is well suited for manipulating volumes that describe material to be machined and decomposing these volumes into features.

Trace-based techniques also lend themselves well to parallelization, providing several levels at which to partition the problem. What might be less evident is that, in parallelizing the problem, one can make additional geometric and topological simplifications to independent problem subtasks to reduce their computational difficulty.

The remainder of this section will specify a common example domain of machined parts and some basic trace-based recognition techniques. Using this domain we present a multi-processor recognition methodology in Section 4.

3.1 Machining Features

A *machining feature*, M , is a parameterized volumetric template that represents the solid volume removed from a workpiece by a machining operation. An instance of a machining feature, f , is created by a specific machining operation with a single cutting tool in one tool setup. To perform a machining operation, one sweeps the tool along some trajectory. Only a portion of this swept volume corresponds to the volume of material that is to be removed by the machining feature. This volume is called *removal volume* of feature f .

Machining features are referred to in terms of the operations used to create them. For example, we say that the hole h in Figure 1(a) is an instance of a *drilling feature*. The pocket p in Figure 1(b) is an instance of an *end-milling feature* and is characterized by the edge profile bounding the area swept by the milling tool.

3.2 Machining Feature Recognition

The initial workpiece, S , is represented as a solid model of raw stock material to be acted upon by a set of machining operations. The machined part is a solid object, represented by a solid model of the part P , to be produced as a result of a finite set of machining operations. The *delta volume* is the regularized difference [15] of the initial workpiece and the part: $\Delta = S - * P$.

In general, there may be several alternative interpretations of the part as collections of machining features, each interpretation corresponding to a different way of manufacturing it. A *feature-based model* is a collection of features that models a single, unique interpretation of the part. The feature recognition problem can be defined as follows: given a collection of machining features, $\mathcal{M} = \{M_1, M_2, \dots, M_j\}$, a part P , and a piece of stock S , find the set \mathcal{F} of feature instances from \mathcal{M} recognized with P and S . The feature set \mathcal{F} is a finite set of features composed of the union of those features in the alternative feature-based models for the part [23].

3.3 Trace-based Recognition of Features

A *trace* represents the partial information in the solid model of the part produced by an instance of a feature. Intuitively, a trace t_M corresponds to the information contributed to the part by an instance of a feature of type M . The trace provides sufficient information for calculating the parameters of a feature instance f of type M . For example, one trace for the drilling feature in Figure 1(a) is the conical ending surface of the hole h . Similarly, a trace for the end-milling feature m in Figure 1(b) is its bottom surface.

The basic structure of a trace-based feature recognition system includes:

- Each feature type M in \mathcal{M} has associated with it set of traces $t_{M1}, t_{M2}, \dots, t_{Mk}$.
- There is a procedure $\mathcal{P}()$ such that $\mathcal{P}(t_{Mi})$ constructs, from the information in the solid model of the part and stock material, instances of features of type M capable of producing the trace t_{Mi} .

An outline for a generic algorithm for trace-based recognition of features can be presented as follows:

- Input a collection of feature types, \mathcal{M} , a solid model for the part P , and a solid model for the initial stock material S .
- From P and S , identify the set of all potential traces present, \mathcal{T} .
- For each potential trace t in \mathcal{T} do:
If t matches a t_{Mi} , call the procedure $\mathcal{P}(t_{Mi})$ and construct (if possible) feature instances, f_1, f_2, \dots, f_n of type M . Add these to the set of all feature instances, \mathcal{F} .

Example traces. As an illustration, the task of recognizing drilling and end-milling features can be accomplished using the following traces:

- drilling features*:
 - Trace 1: a convex conical surface in the delta volume as a conical ending surface describing the cutting tip of a drilling tool. This trace is used to build an instance of a drilling feature when only a portion of its ending tip surface remains on the boundary of the delta volume.
 - Trace 2: a convex cylindrical surface in the delta volume as a side surface created by a drilling operation. This trace is used to build instances of drilling features when a portion of their side surface remains on the boundary of the delta volume.
- end-milling features*
 - Trace 1: a planar surface in the delta volume as a surface created by the cutting tip of an end-mill. This trace is used to build instances of end-milling features when only a portion of their bottom surfaces are present on the boundary of the delta volume.

The next two traces are used to build instances of end-milling features when only a portion of their side surfaces are present on the boundary of the delta volume. In these cases, the end-milling features may extend completely through the stock material. Examples of such features include through pockets.

- Trace 2: a cylindrical surface in the delta volume as a surface created by the side cutting surface of an end-mill.
- Trace 3: a pair of non-parallel planar surfaces in the delta volume, as faces created by the side cutting surface of an end-mill.

A presentation of the details of the various procedures $\mathcal{P}(t_{Mi})$ for constructing feature instances from these traces is not central to the focus of this paper. Such algorithms

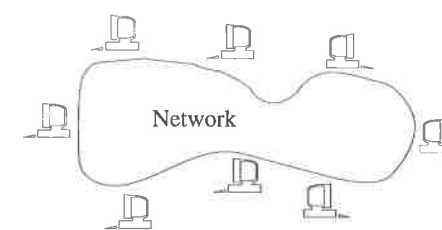


Figure 3: Internetworked computational resources.

have been developed in previous work, notably: Vandenberg [29] for drilling feature traces 1 and 2 and end-milling feature trace 1; and Regli *et al.* [24, 23] for all of the above traces.

4. APPROACH TO PARALLELIZATION

In the distributed computing paradigm, collections of autonomous computational resources are interconnected on a network, as illustrated in Figure 3 [28]. While these resources do not share main memory, they may share access to common devices such as peripherals, file systems, output devices, etc. Software systems can use the network and shared peripherals to exchange information among the autonomous resources.

In this section, we will apply distributed algorithms to the example problem domain from Section 3.

4.1 Motivations

The feature types and their traces each introduce natural partition lines along which the problem can be divided into independent subproblems to be solved by different processors.

As presented in Section 3.2, the final feature set \mathcal{F} contains all those feature instances from \mathcal{M} that are members of feature-based models of the part. \mathcal{F} contains all instances of the feature types in \mathcal{M} present in the given part. Note that for the features in \mathcal{M} , the act of recognizing a feature of type M_1 is independent of the recognition of a feature of type M_2 —hence the feature instances of type M_1 can be calculated separately from those of type M_2 . For instance, in the example domain presented in Section 3, the fact that a particular drilling feature f is a member of some feature-based model does not alter the existence of any end-milling features.

Secondly, the set of traces \mathcal{T} (from the generic algorithm in Section 3.3) introduces an additional level for partitioning the problem. Recall that for each feature type M in \mathcal{M} , there is a collection of traces $t_{M1}, t_{M2}, \dots, t_{Mk}$ for building instances of features of type M . One can decompose the problem of finding all features of type M using the traces, handling each trace t_{Mi} on a different processor.

One observation is that this may introduce some redundancy; i.e., it may be possible to find the same feature instance f in different ways using different traces. There are two possible approaches to handling this redundancy. One

method is to delete duplicate features while building the final feature set \mathcal{F} . A second approach, and the one that we will employ, is to handle the traces capable of producing equivalent feature instances together on the same processor and remove duplicates as they are found. This introduces another level of parallelization by dividing the set of traces found into independent subsets. In this way redundancies are addressed at the level at which they occur, thus simplifying the task of building the final feature set \mathcal{F} .

Parallelizing feature recognition produces other, less obvious benefits. In particular, a large portion of the costs in a feature recognition system are due to the complexity of geometric computations and geometric reasoning. When isolating independent problem subtasks, one can make geometric and topological simplifications that identify the information in the original part needed to build and verify the feature instances. In this way, many of the subproblems may require only a fraction of the information present in the solid models of the original part and stock.

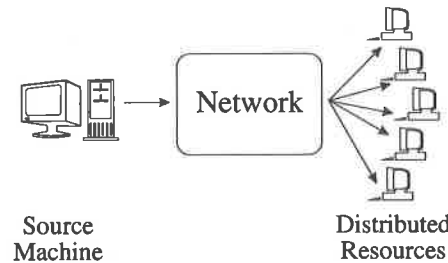


Figure 4: Source machine distributing tasks to clients.

4.2 Distributed Methodology

For the example domain in Section 3, our approach is to have a central computing resource act as a server to set up the problem and transmit subtasks to client machines distributed on the network, as illustrated in Figure 4. Each of the individual client processors is given an independent portion of the particular global feature recognition problem.

A distributed algorithm. Recalling the serial trace-based algorithm of Section 3.3, we present an outline for a multi-processor trace-based feature recognition system. There are two main components to this system: a server algorithm and a client algorithm. The server algorithm is presented as follows:

Server algorithm.

1. Input a collection of feature types, \mathcal{M} , a solid model for the part P , and a solid model for the initial stock material S . Initialize $\mathcal{F} = \emptyset$.
2. For each feature type M in \mathcal{M} do
 - (a) Fork a new process on a free resource
 - (b) For each trace type t_{Mi} for feature type M do

- i. Find the set $T_{t_{Mi}}$ of instances of traces of type t_{Mi} .
 - ii. Decompose the set $T_{t_{Mi}}$ into independent subtasks, $\tau_1, \tau_2, \dots, \tau_j$.
 - iii. For each τ_i do
 - A. Decompose the part P using the τ_i . Result P' .
 - B. Fork a new process on a free resource to call the client recognition algorithm on P' .
 - iv. Let $F_{t_{Mi}}$ be the set of features returned by the client.
3. $\mathcal{F} = \mathcal{F} \cup_{t_{Mi}} F_{t_{Mi}}$.
 4. Remove duplicate features from \mathcal{F} .
 5. Return \mathcal{F} .

The client algorithm, to be invoked by the server on multiple computational resources, is presented below:

Client algorithm.

1. Input a feature type, M , a trace type, t_{Mi} , a set of instances of T of trace t_{Mi} , and solid models for the part P' , and the stock material S .
2. Simplify the solid model of the part P' . Result P'' .
3. Call $\mathcal{P}(t_{Mi})$ to build feature set $F_{t_{Mi}}$.
4. return $F_{t_{Mi}}$.

To implement this client-server algorithm, three technical areas must be addressed:

Task Initialization. There are four levels at which the recognition problem is initialized:

- *Types of features to be recognized:* different feature types (in this example drilling and end-milling) are considered by separate computing resources, as discussed in Section 4.1.
- *Types of feature traces:* different traces for each of the feature types are considered by separate computing resources, as discussed in Section 4.1.
- *Trace decomposition:* given a specific feature type and a trace for recognizing it, decompose the set of instances of this trace to independent subsets to subdivide the recognition task. This is discussed in Section 4.3.1.
- *Part simplification:* given a specific feature type and a trace for recognizing it, alter the geometric and topological information in the solid model of the part to reduce its complexity. This is discussed in Section 4.3.2.

Specific details are given in Section 4.3.

Task Distribution. Once tasks are initialized, the next phase is to distribute the individual tasks to the available computing resources. This is done by invoking a client feature recognition procedure for each separate task; each task to be performed on its own processor.

In the example domain in Section 3, distributing tasks is straightforward. This becomes more complex when bounds are placed on the number of available computing resources.

Synthesis of Results. Each separate client procedure, upon termination of its portion of the recognition task, transmits its results back to the server machine. The features returned are then integrated into an overall solution. In this domain, recombining results requires building the final feature set as the union of those feature sets returned by each client machine.

However, the fact that this example domain lends itself well to building an overall solution from the separate subtasks may not generalize to other manufacturing domains. For example, this phase might include additional computations such as modeling feature interactions, eliminating redundant features, or identifying compound features or feature groups.

4.3 An Example of Task Initialization

The task initialization stage groups feature information and isolates traces to be handled by separate computing resources. There are four levels of task decomposition.

For illustration purposes, we shall assume there is no limit on our computational resources. When there is a bound on the number of processors available, the task decomposition or the distribution of the task may vary to more efficiently partition the problem. In our implementation (discussed in Section 5), we distribute the tasks evenly over the available processors.

The decomposition by feature type and decomposition by trace, as noted before, are straightforward. In developing techniques for part decomposition and simplification, one is faced with a trade off between the sophistication of techniques and their computational costs. Using very sophisticated techniques to maximize the ability of each individual processor to produce useful feature instances in a minimal amount of time might increase the computational overhead to a degree that mitigates the benefits of parallelization. In choosing the following conditions, we have picked decompositions and simplifications that are computationally cheap. While it is certainly possible to present more complex decomposition criteria, an important consideration is that the conditions themselves cannot be more complex than the original recognition problem. If the decomposition conditions are themselves costly, the overhead considerations might eliminate any of the speedup benefits we hope to achieve using a multi-processor approach.

The remainder of this section discusses the decomposition of part geometry and topology and techniques for part simplification.

4.3.1 Trace Decomposition

A given feature instance might be created from any one of several traces it leaves in the part. The objective of this phase is to collect all of the trace information capable of producing equivalent or identical feature instances. While

we will only consider geometric and topological information in this paper, this decomposition can be extended to include other data (i.e., tolerances, surface properties, etc.).

We present a four-step decomposition for the geometric and topological information in the part. The conditions are based on properties of the traces for constructing feature instances. There may be other conditions that provide an equivalent means of arriving at a task decomposition with the desired properties. Decomposition of the geometry and topology based on feature types and traces proceeds as follows:

1. Drilling traces 1 and 2:
Group together convex cylindrical and conical faces with equivalent axes.
2. End-milling trace 1:
Group together all coplanar faces. In the example illustrated in Figure 5(b), six disjoint planar part faces are grouped to be handled together on the same processor. This grouping collects all faces sharing the same underlying surface.
3. End-milling trace 2:
Group convex cylindrical surfaces with equivalent axis directions.
4. End-milling trace 3:
Group planar surfaces with normals perpendicular to a common vector; i.e., for each grouping there is a vector v such that, for all surfaces s_i and s_j in the grouping, $\text{normal}(s_i) \cdot v = \text{normal}(s_j) \cdot v = 0$. Note that some surfaces may be present in more than one group.

The above decomposition group those traces from the part which might produce equivalent feature instances. In this way, redundancies can be eliminated at the subprocess level and later recombination of results.

4.3.2 Part Simplification

The objective of this step is to reduce the amount of data that must be considered by each processor to a minimum amount sufficient to construct feature instances from the traces it has been given. In this way, one can reduce each processor's operation costs during feature recognition. For example, one can reduce the number of geometric and topological entities while still retaining the information required to construct feature instances from the particular trace—thus eliminating complex part geometry not effecting the feature trace being considered.

We simplify the solid models of the part and stock based on the trace information and feature types. In each case, the geometry and topology of the model for the part P is simplified to P' as follows:

1. Drilling trace 1:
Given a cylindrical surface c in the delta volume of radius r , P' contains all the portions of P that lie within r of the axis of c .
2. Drilling trace 2:
Given a conical surface c in the delta volume with a maximum radius r and located at point d , P' contains

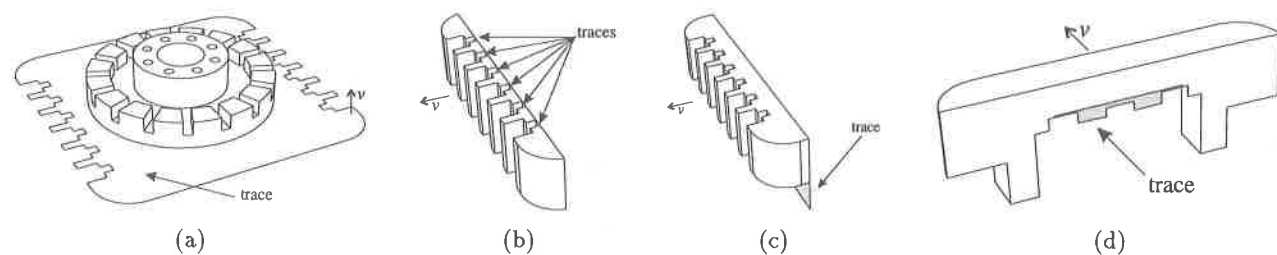


Figure 5: Four end-milling recognition subtasks and their simplified part information for the example part in Figure 2.

all the portions of P that lie within r of the axis of c and in the half-space above d .

3. End-milling trace 1:

Given a planar surface p in the delta volume with a root point d and normal vector v , P' contains all the portions of P that lie in the half-space defined by d and v .

4. End-milling traces 2 and 3:

No simplifications are made for these traces. Finding these types of end-milling feature instances might require consideration of information from the entire part, and sophisticated simplifications in this case would be costly.

Figure 5 shows four illustrations of part simplification for end-milling trace 1. In the figure, the planar faces are being considered as traces indicating potential bottom surfaces of several end-milled features; vector v denotes the orientation of the potential feature. In each case, the trace information is used to eliminate the portion of the part lying below the trace—information that does not get considered when building a feature instance in direction v . Note that in making this rudimentary simplification the number of geometric and topological entities to be considered is greatly reduced.

4.4 Potential for Computational Improvement

We can expect the speedup to be no more than a factor of K , where K is the number of processors available. In reality, the task decomposition to set up parallelization incurs some added cost, as does the recombination of results at the end. These additions are negligible, however, when compared with the costs incurred to perform the recognition process on the subproblems.

Within a trace-based methodology, as outlined in Section 3.3, the overall complexity of recognition depends on two factors: the difficulty in generating the set T of potential traces, and the complexity of the methods for generating feature instances from traces.

A rough upper bound on the size of T can be computed from the model of the part and the types of traces by counting the number of geometric and topological entities. The complexity of the feature construction routines is more difficult to assess and is where the majority of the computational costs occur. Much of this cost is due to geometric queries and reasoning operations used to find the parameters of feature instances. While there is no authoritative

reference on the general complexity of solid modeling operations such as booleans, sweeps, and the like, the consensus is that these operations account for the majority of the computational cost during feature recognition [29]. The complexity of boolean operations appears to lie between $O(n^2)$ and $O(n^4)$ or $O(n^5)$ time, depending on the particular configuration of geometric entities and many implementation-specific details.

The fact that these basic solid modeling routines are at least quadratic in the size of the model implies that small reductions in the number of entities in the model translate into large reductions in computational effort.

In the next section, we provide rough estimates of both the speedup factor and the reduction in the number of geometric and topological entities achieved by this approach.

5. IMPLEMENTATION AND EXAMPLES

A proof-of-concept implementation of this distributed feature recognition methodology, dubbed *F-Rex*, has been done in C++ using version 3.0.1 of the AT&T C++ compiler from SUN Microsystems running on networked SUN SPARCstations. *F-Rex* employs version 1.5.1 of Spatial Technologies' ACIS[®] solid modeling system and version 3.14 of the NIH C++ Class Library developed at the National Institutes of Health. Additional tools include Ithaca Software's HOOPS[®] Graphics System and the Tcl/Tk embeddable command language and user interface toolkit from the University of California at Berkeley.

F-Rex is the feature recognition subsystem for IMACS, an interactive manufacturability analysis tool under development at the University of Maryland's Institute for Systems Research. One of the fundamental goals of IMACS is to provide interactive feedback and redesign suggestions to the user. We hope to use multi-processor algorithms to provide IMACS with a means of avoiding computational bottlenecks.

F-Rex runs on a cluster of SUN workstations; processes communicate over the Internet using UNIX-based and TCP/IP protocol-based network software utilities and shared disk storage. The geometric computations required for task initialization are implemented with direct C++ calls to the ACIS kernel; distributed processes are invoked using UNIX remote shell commands; and the resulting feature set is generated by examining the features produced by each processor and eliminating redundancies.

The data for the examples below has been collected using six processors, one SPARCStation model 10, one model 2, and 4 IPX models. In this version of the implementation, when the number of tasks is greater than 6, the tasks are distributed evenly over the available processors.

These timing results represent the elapsed clock and CPU times and are not absolute measures of the intrinsic difficulty of the feature recognition problem—this example domain is not directly comparable to those of other feature recognition research efforts. Further, there are hidden costs in the implementation not directly related to the recognition of feature templates (such as feature accessibility analysis) and these algorithms and their implementation can certainly be improved and optimized. The results are intended to provide a rough indication of the time-lag experienced by the user of the system. More significant than any precise calculation of elapsed time is the speedup factor between the serial and parallelized algorithms. Measurements of elapsed CPU time are summarized in the table in Figure 7.

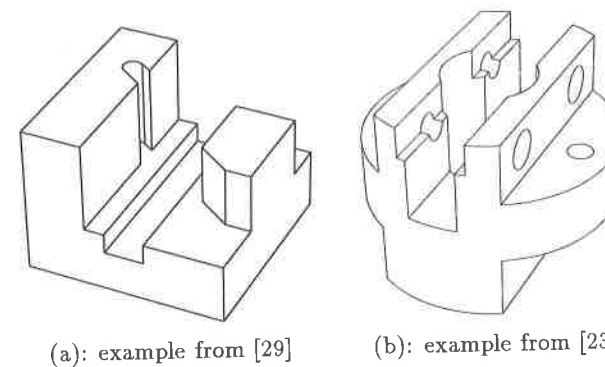


Figure 6: Two example parts addressed in previous literature.

Example	Serial	Distributed	
		Set Up	Recognition
1	53.59s	0.96s	9.79s
2	126.90s	1.23s	6.39s
3	> 1920.0s	19.41s	701.47s

Figure 7: Table of elapsed CPU times for each example.

Example 1. The example part in Figure 6(a), taken from [29], contains 21 part faces. Vandenbrande and Requicha [29] report identifying 7 features (3 slots, 3 open pockets, and a step) in two and a half minutes on a SUN 4/360. The OOFF system [29] handles a wide variety of machining features and process planning constraints; hence it is not directly comparable to the approach outlined in this paper. It does, however, provide a general indication

of the computational costs required to recognize features in relatively straightforward parts.

Running in serial on the SPARC 10, *F-Rex* finds 1 drilling and 8 end-milling features in approximately 1 minute. In parallel on 6 processors, it takes approximately 3 seconds to set up the decomposition and 12 seconds to recognize the features. Using the simplification techniques, the number of geometric and topological entities that had to be considered was reduced by 22%.

Example 2. The example part in Figure 6(b) is a socket taken from [23]. This part, when machined from a cylindrical piece of stock material, has 37 faces in the delta volume. There are 12 drilling and 20 end-milling features in its feature-based models that can be produced with the traces given above. In serial running on the SPARC 10, *F-Rex* system identifies these 32 feature instances in approximately 65-70 seconds. When run distributedly, using 6 processors, *F-Rex* takes 10 seconds to set up the decomposition and approximately 12-16 seconds to identify the features. In this case, simplification resulted in a 35% reduction in the number of geometric and topological entities that had to be considered.

Example 3. The example part in Figure 2 is a shuttle intended to move along a guideway, with many of the feature instances added to reduce weight. The solid model of this part contains 281 faces. In serial, it takes over one hour to find the more than 100 feature instances. When running distributedly, *F-Rex* takes 2 minutes to set up the task decomposition and approximately 32 minutes to find the features. In this case, simplification resulted in a 43% reduction in the number of geometric and topological entities that had to be considered.

6. CONCLUSIONS

Concurrent engineering and product design are pushing more downstream manufacturing issues into the design phase. The need to build effective and interactive design and analysis tools to address these needs is making efficient and sophisticated allocation of computational resources increasingly important.

Use of a multi-processor architecture can provide a large increase in computational power by exploiting the available computing resources. The benefits of migrating to a multi-processor architecture include an increase in the complexity of feasible mechanical designs and the ability to produce real-time feature data for complex parts.

Discussion of Results. Our preliminary results confirm that performance gains can certainly be made through effective parallelization of algorithms. However, it is difficult to assess what a typical speedup factor will be. We suspect that the considerable variation in our experiments between parallel and serial speedup can be traced to the complexity of the parts themselves. The example part in Figure 6(a) has only one curved surface, while that in Figure 2 contains many dozens. A more general analysis of speedup factors would require testing the software against a set of benchmark parts of varying degrees of complexity.

We believe that parallelized trace-based feature recognition is highly suitable for parts in which the feature instances themselves are relatively simple, but numerous. It is not as well suited to problems where the feature instances themselves have very complex geometric configurations.

Contributions. In this paper we have presented our initial work toward an approach for performing trace-based feature recognition using a distributed multi-processor architecture. We present a commonly addressed collection of features and illustrate how to identify a task decomposition of the recognition problem. The task decomposition is used then to divide the work among several distributed computing resources whose individual results are integrated into a unified solution for the part at hand. This kind of approach shows promise for domains of complex parts containing, possibly, thousands of features instances, but for which the structures of the feature instances themselves are relatively simple.

Future Work. Application of distributed algorithms to solid modeling and problems in engineering design and analysis holds immediate promise for enhancing existing CAD tools. We hope that this work motivates more research into how to effectively migrate current solid modeling applications toward a distributed computing framework. In the future, as distributed computing technologies become more accessible, algorithms that coordinate efforts between autonomous and geographically diverse computing resources will be commonplace in the modern manufacturing enterprise.

Making this transition will require changes to the underlying architecture of solid modeling systems, their data structures, and algorithms to exploit multi-processor computing. In addition, as engineering software applications built on top of modelers continue to grow in complexity, obtaining performance improvements increasingly will involve distributed algorithms.

We anticipate that this new distributed feature recognition technology will increase the complexity of mechanical parts within the reach of traditional feature recognition systems and will reduce the computational bottlenecks they pose. This will enable more sophisticated design analyses and, in turn, aid in building an environment that will allow designers to create high-quality products that can be manufactured more economically—thus reducing the need for redesign, lowering product cost, and shortening lead times.

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Solid models for the example parts in this paper can be obtained through the World Wide Web at URL <http://www.cs.umd.edu/~regli/distrib/paper.html>.

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